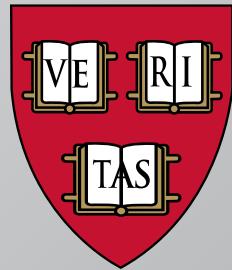


Simultaneous multiphoton absorption in rutile (TiO_2) across the half-bandgap

Christopher C. Evans, Jonathan D. B. Bradley,
Erwin A. Martí-Panameño and Eric Mazur



Photonics West 2012
January 26, 2012



Introduction

TiO₂ Material Properties

Large ultrafast nonlinearity: 30 x silica

High index of refraction: 2.5

Wide bandgap: 3.1 eV

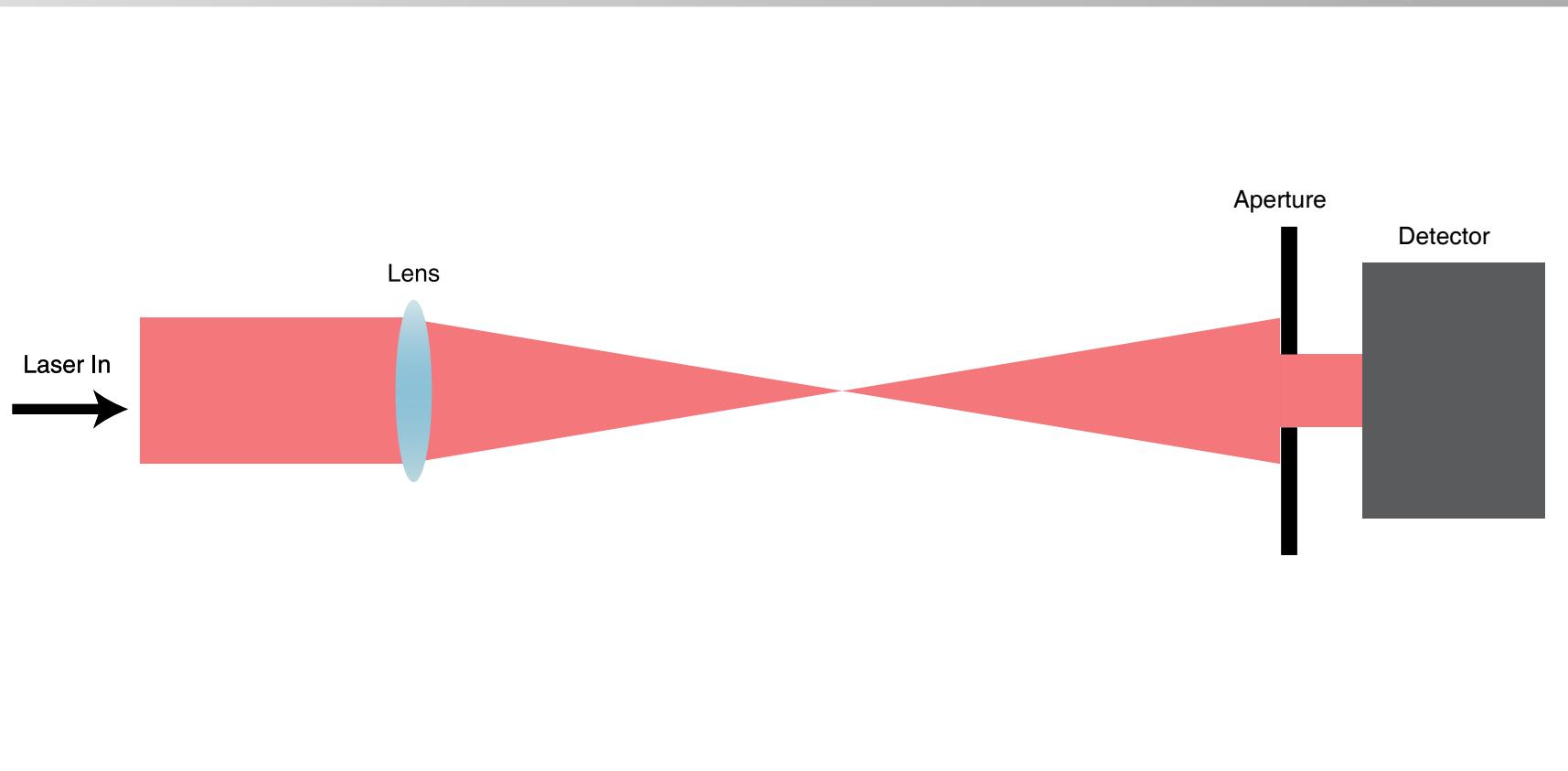
Low two-photon absorption: ≥ 800 nm

Several polymorphs:

Rutile, Anatase, Brookite and Amorphous

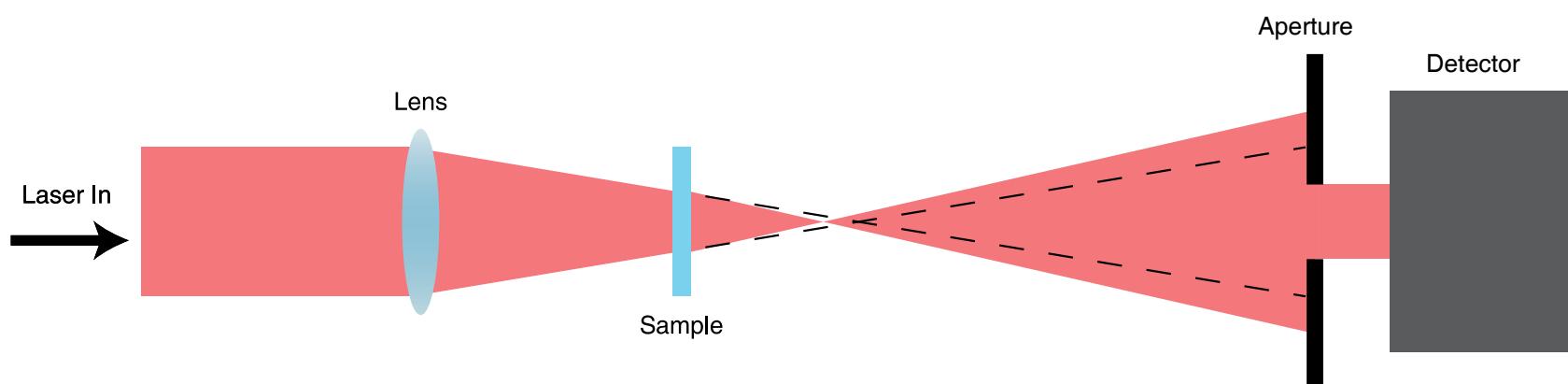
Introduction

Nonlinear material properties: z-scan



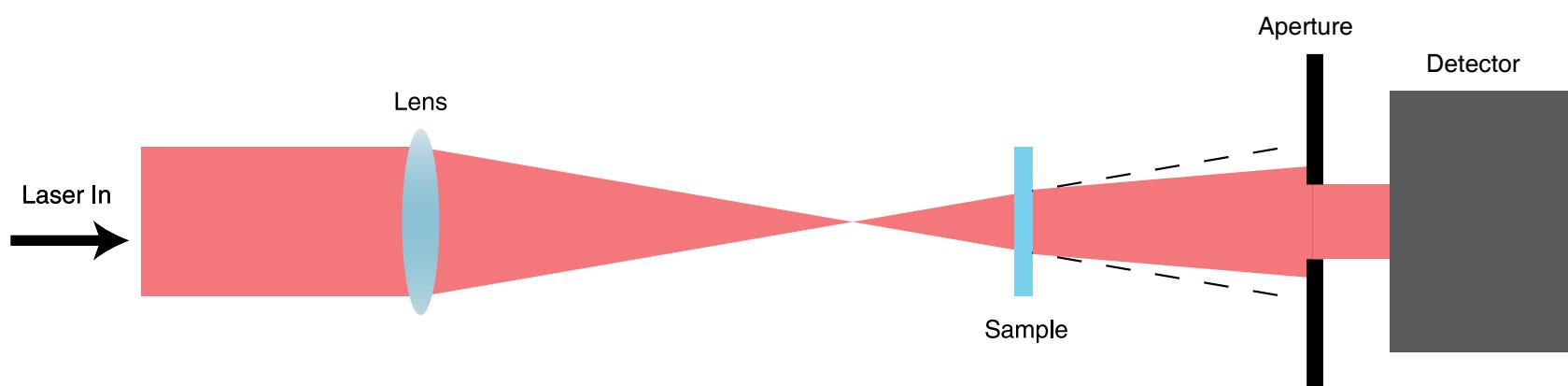
Introduction

Nonlinear material properties: z-scan



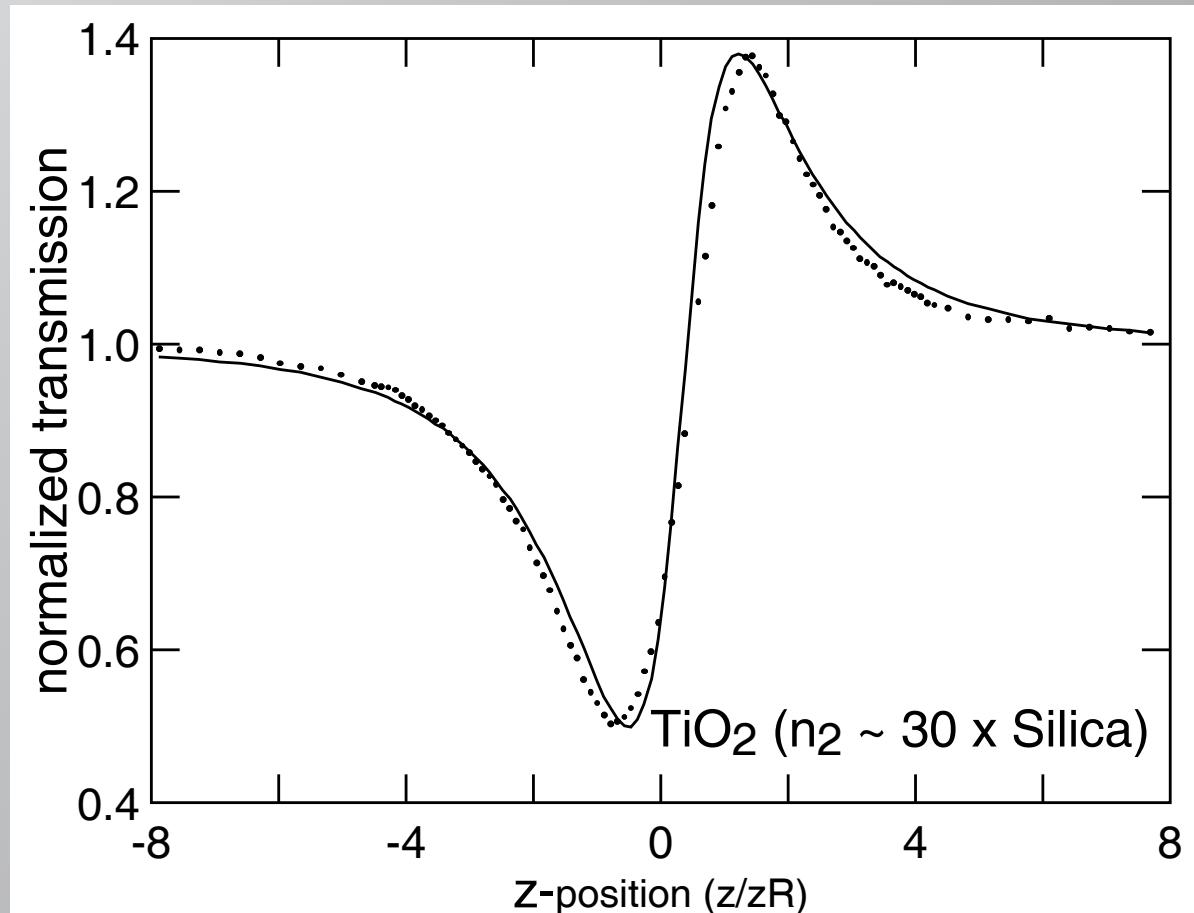
Introduction

Nonlinear material properties: z-scan



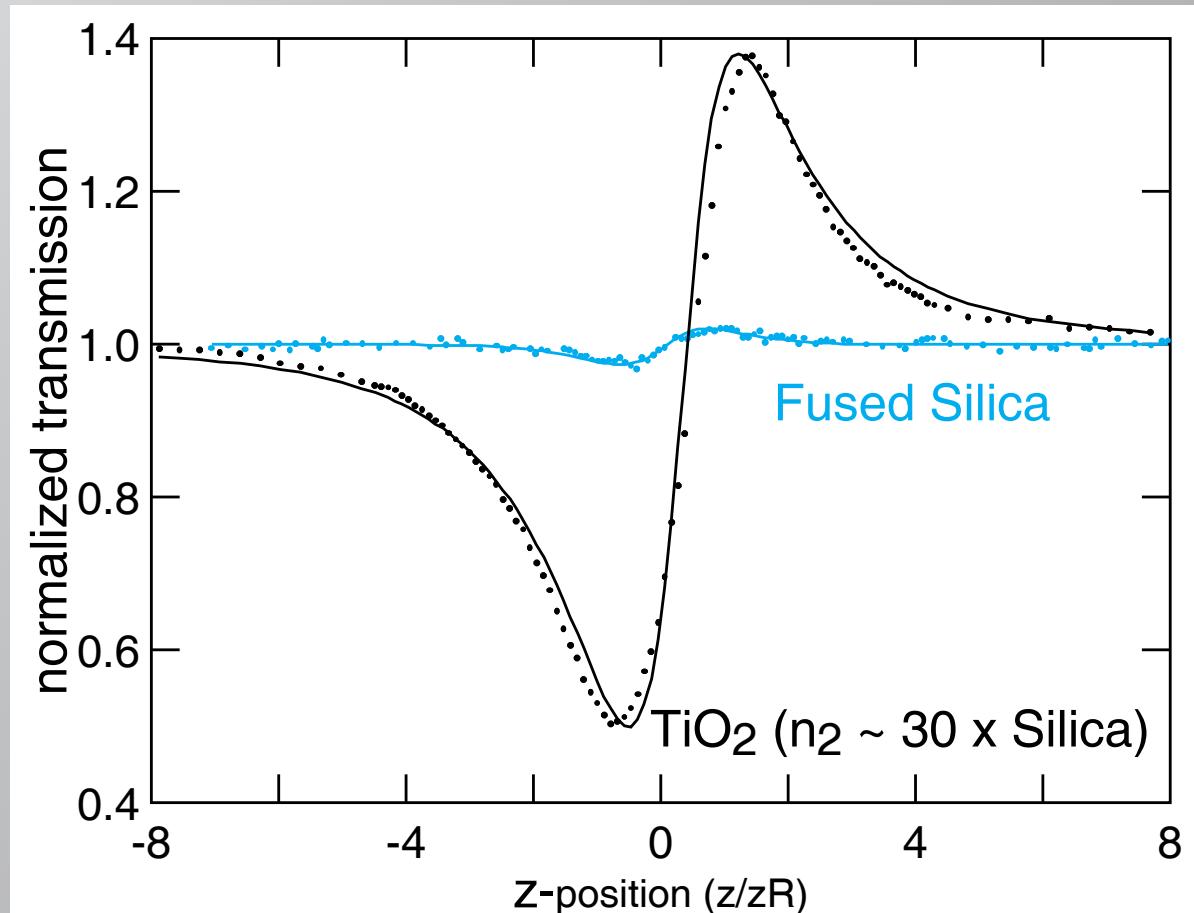
Introduction

Nonlinear refraction (n_2 at 800 nm)



Introduction

Nonlinear refraction (n_2 at 800 nm)

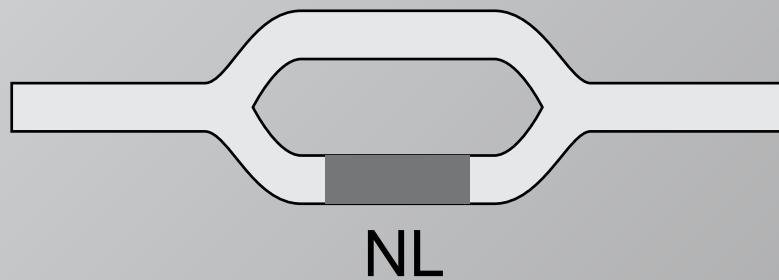


Introduction

high nonlinearity \neq working device

Introduction

$$n = n_0 + n_2 I$$



Introduction

high nonlinearity \neq working device

Full modulation requires at least
a 2π nonlinear phase shift

Introduction

high nonlinearity \neq working device

Full modulation requires at least
a 2π nonlinear phase shift

$$\phi_{NL} = \frac{2\pi n_2}{\lambda} IL$$

Introduction

high nonlinearity \neq working device

Full modulation requires at least
a 2π nonlinear phase shift

$$\phi_{NL} = \frac{2\pi n_2}{\lambda} IL$$

$$\phi_{NL} = \frac{2\pi n_2}{\lambda} \int_0^L I(z) dz$$

Introduction

high nonlinearity \neq working device

Full modulation requires at least
a 2π nonlinear phase shift

$$\frac{n_2}{\beta\lambda} > 1$$

$$\frac{n_2 I_0}{\alpha\lambda} > 1$$

Introduction

high nonlinearity \neq working device

Full modulation requires at least
a 2π nonlinear phase shift

$$\frac{n_2}{\beta\lambda} > 1$$

two-photon
absorption

figure of merit

$$\frac{n_2 I_0}{\alpha\lambda} > 1$$

one-photon
absorption

figure of merit

Introduction

high nonlinearity \neq working device

Full modulation requires at least
a 2π nonlinear phase shift

$$\frac{n_2}{\beta\lambda} > 1$$

material
limit

$$\frac{n_2 I_0}{\alpha\lambda} > 1$$

“fabrication”
limit

Introduction

$$\frac{n_2 I_0}{\alpha \lambda} > 1$$

1PA FOM

$$\frac{n_2}{\beta \lambda} > 1$$

2PA FOM

$$\frac{n_2}{\gamma \lambda I_0} > 1$$

3PA FOM

Introduction

$$\frac{n_2 I_0}{\alpha \lambda} > 1$$

1PA FOM

$$\frac{n_2}{\beta \lambda} > 1$$

2PA FOM

$$I_{\max}^{\text{3PA}} = \frac{n_2}{\gamma \lambda}$$

3PA FOM

Outline

Experimental

Modeling

Analysis

Conclusions

Experimental

Single crystal rutile samples:

Floating-zone method

1-mm thick

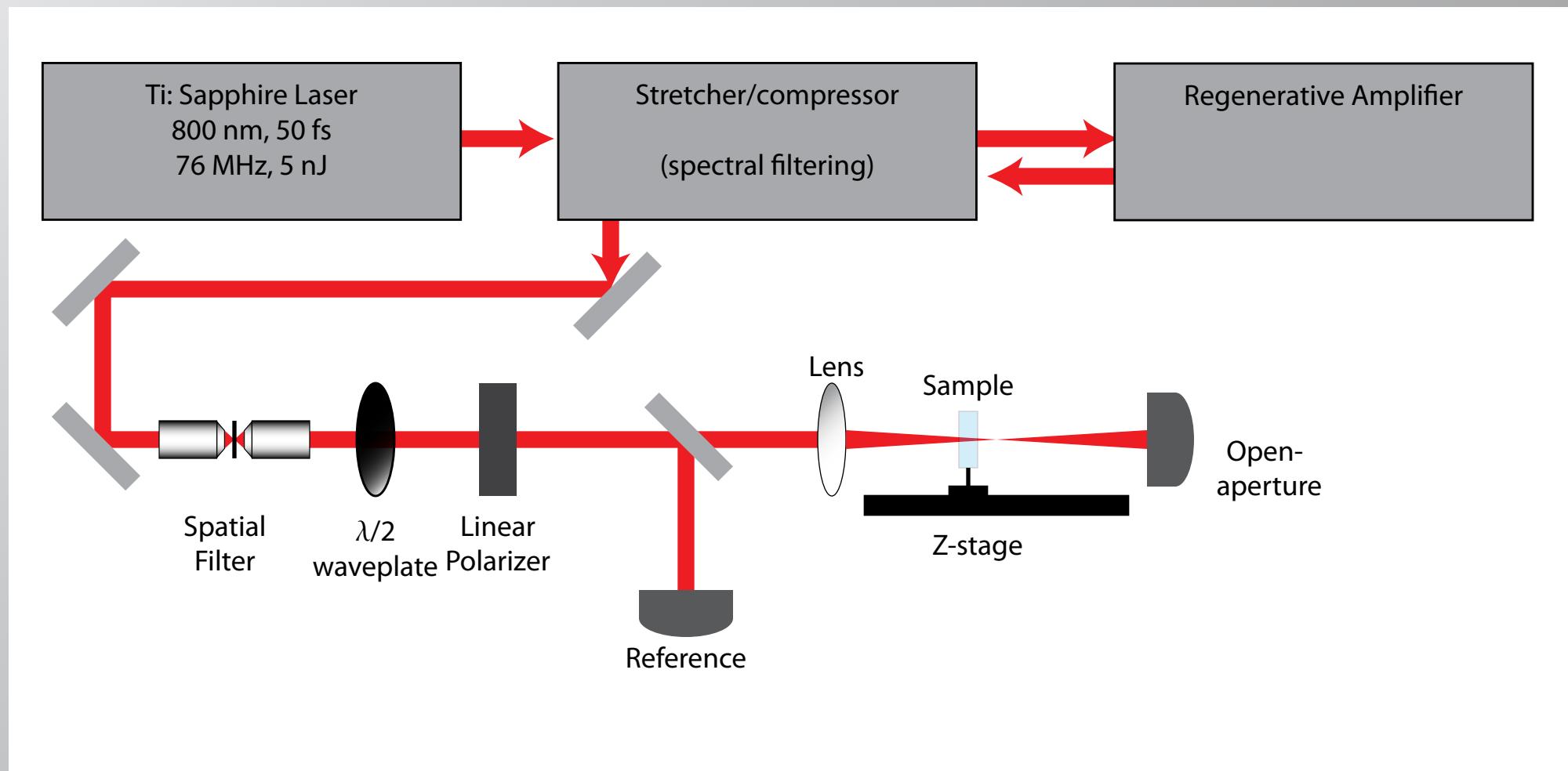
Two-cuts:

(001)-cut, $E \perp c$ only

(100)-cut, $E \perp c$ and $E \parallel c$

Experimental

Experimental setup



Experimental

Laser Parameters

λ_0 (nm)	$2\hbar\omega$ (eV)	$\Delta\lambda$ (nm)	τ (fs)
774	3.20	4	290
813	3.05	10	174
800	3.10	30	50

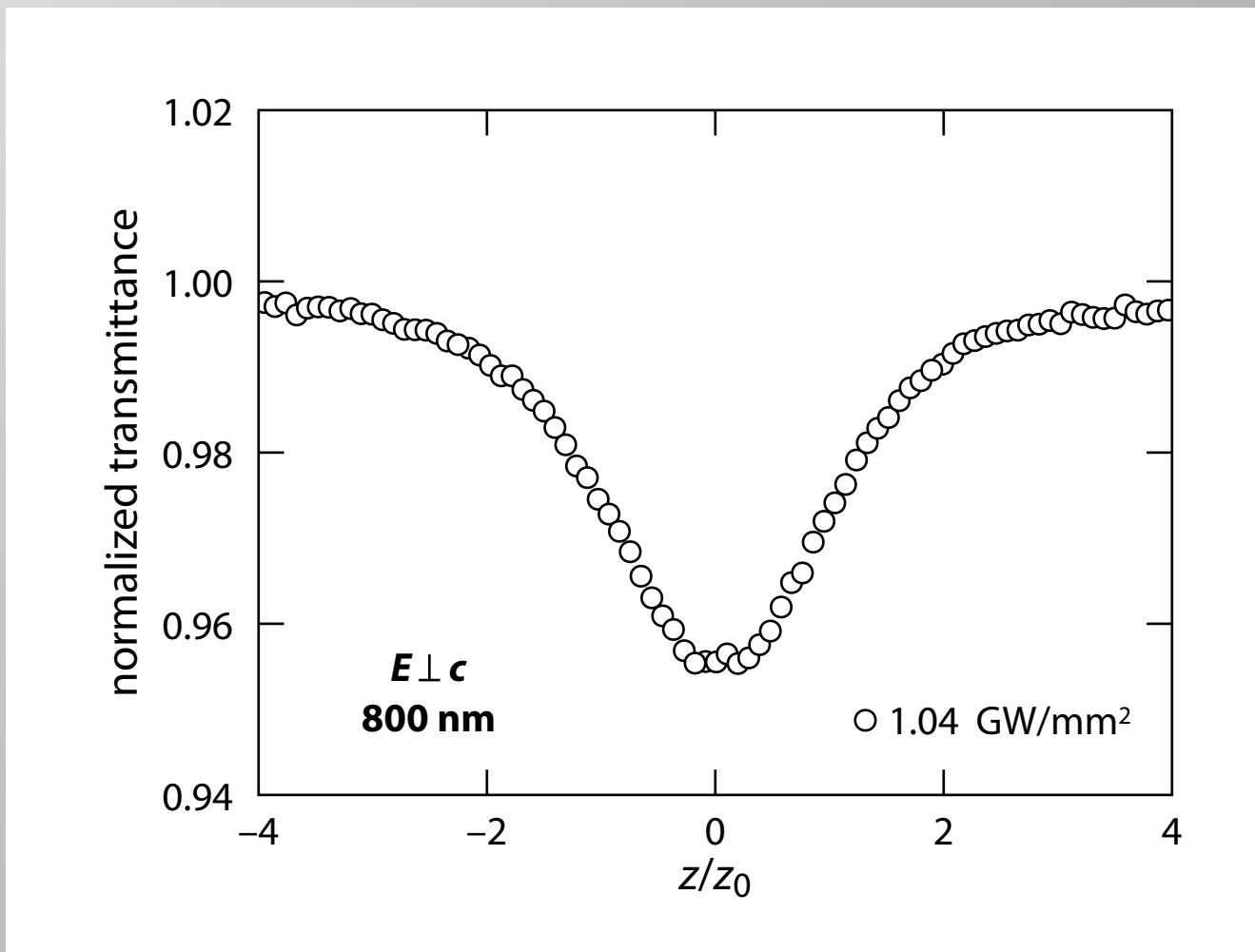
Experimental

Laser Parameters

λ_0 (nm)	M^2	w_{x0}/w_{y0}	$I_{0,\max}$ (GW/mm ²)
774	< 1.13	0.78	0.21
813	< 1.18	0.92	0.32
800	< 1.06	0.95	1.04

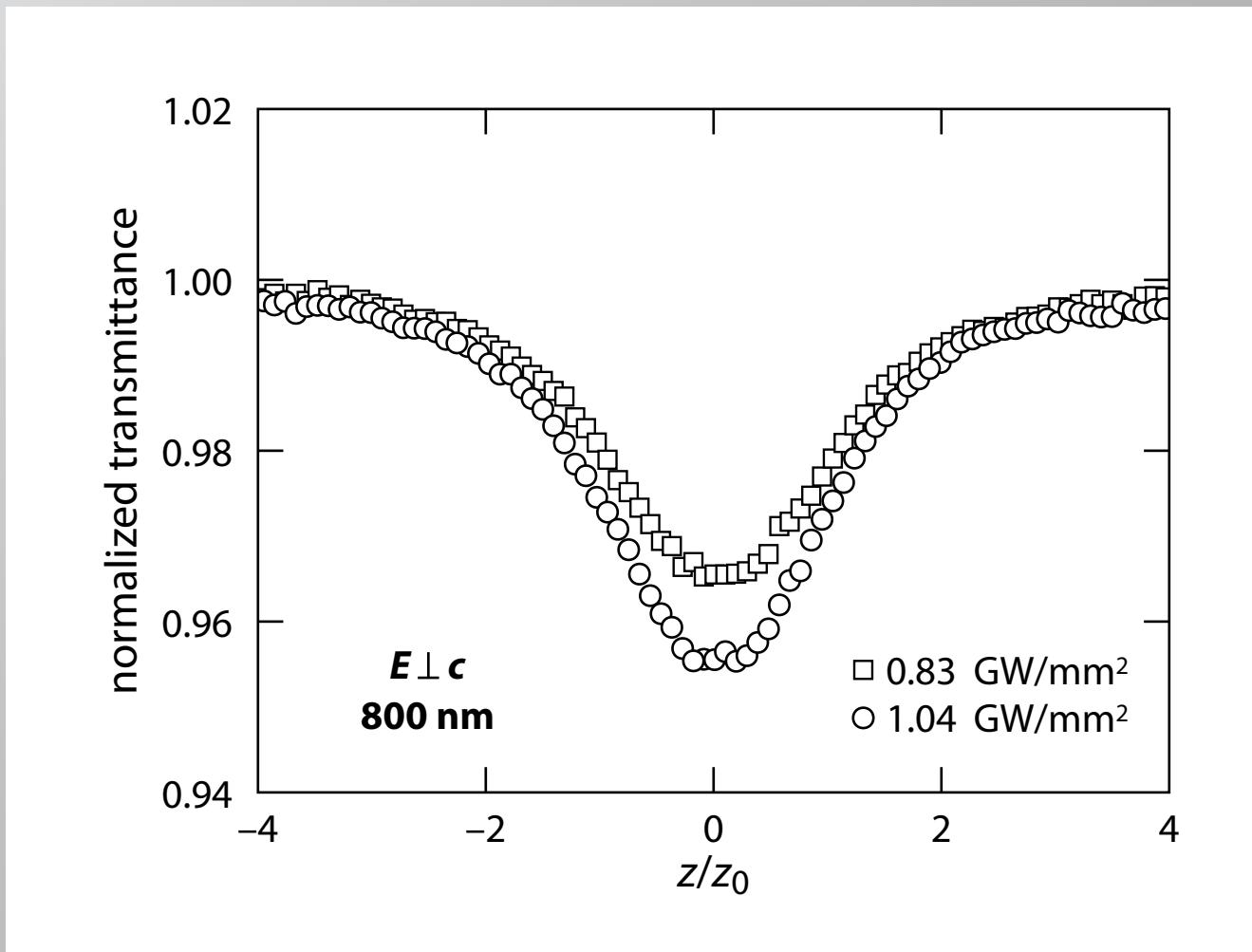
Experimental

Open aperture Z-scan of rutile



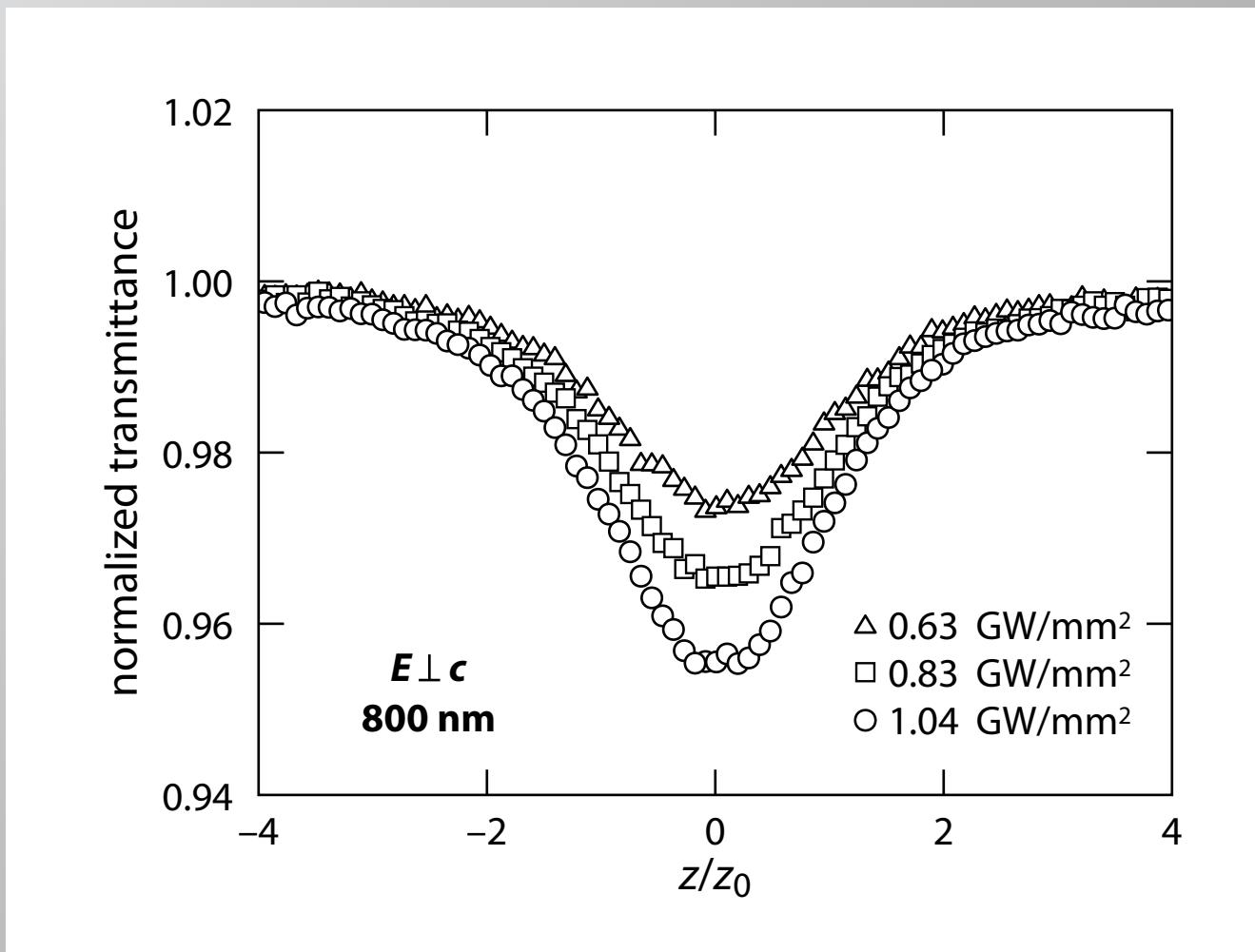
Experimental

Open aperture Z-scan of rutile



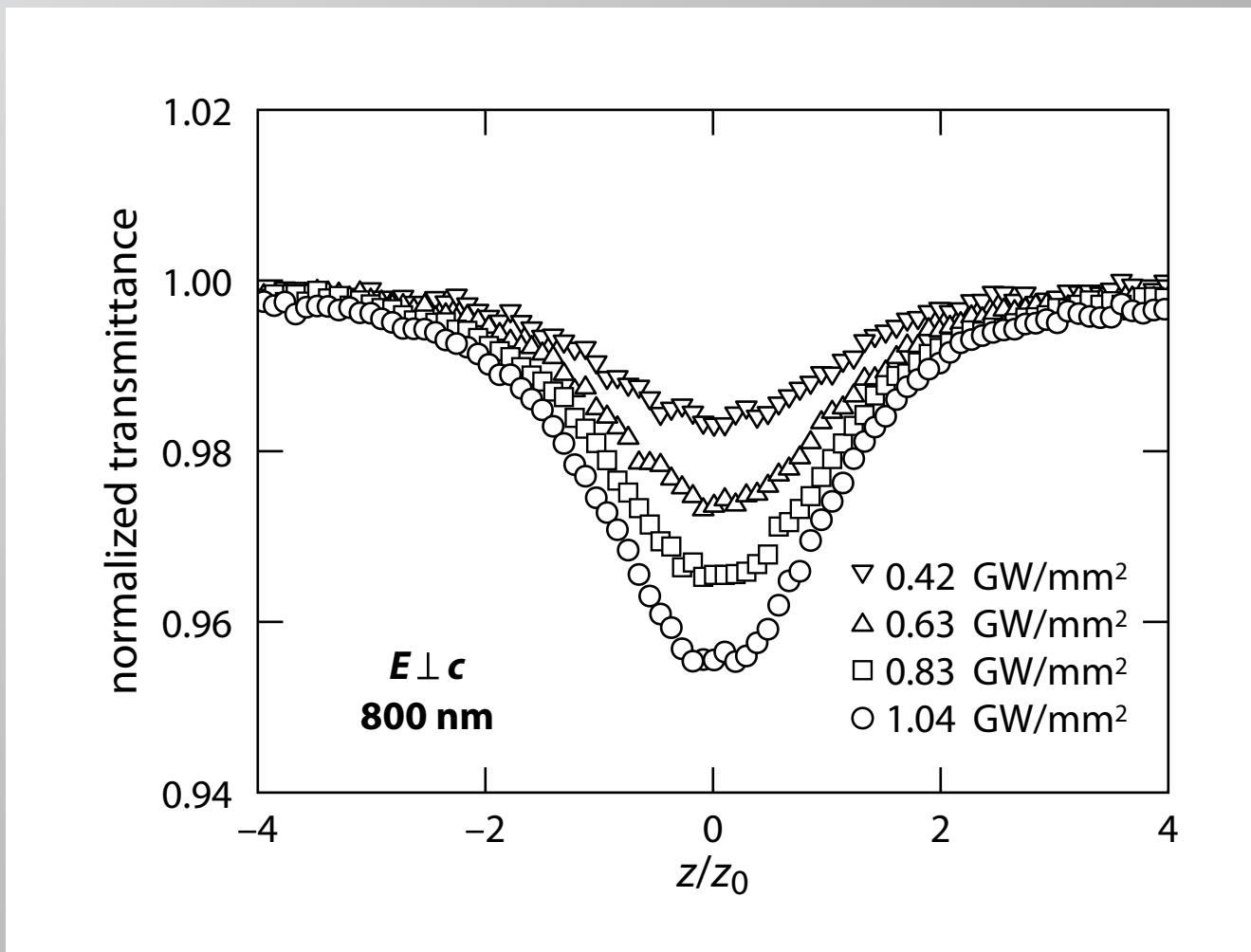
Experimental

Open aperture Z-scan of rutile



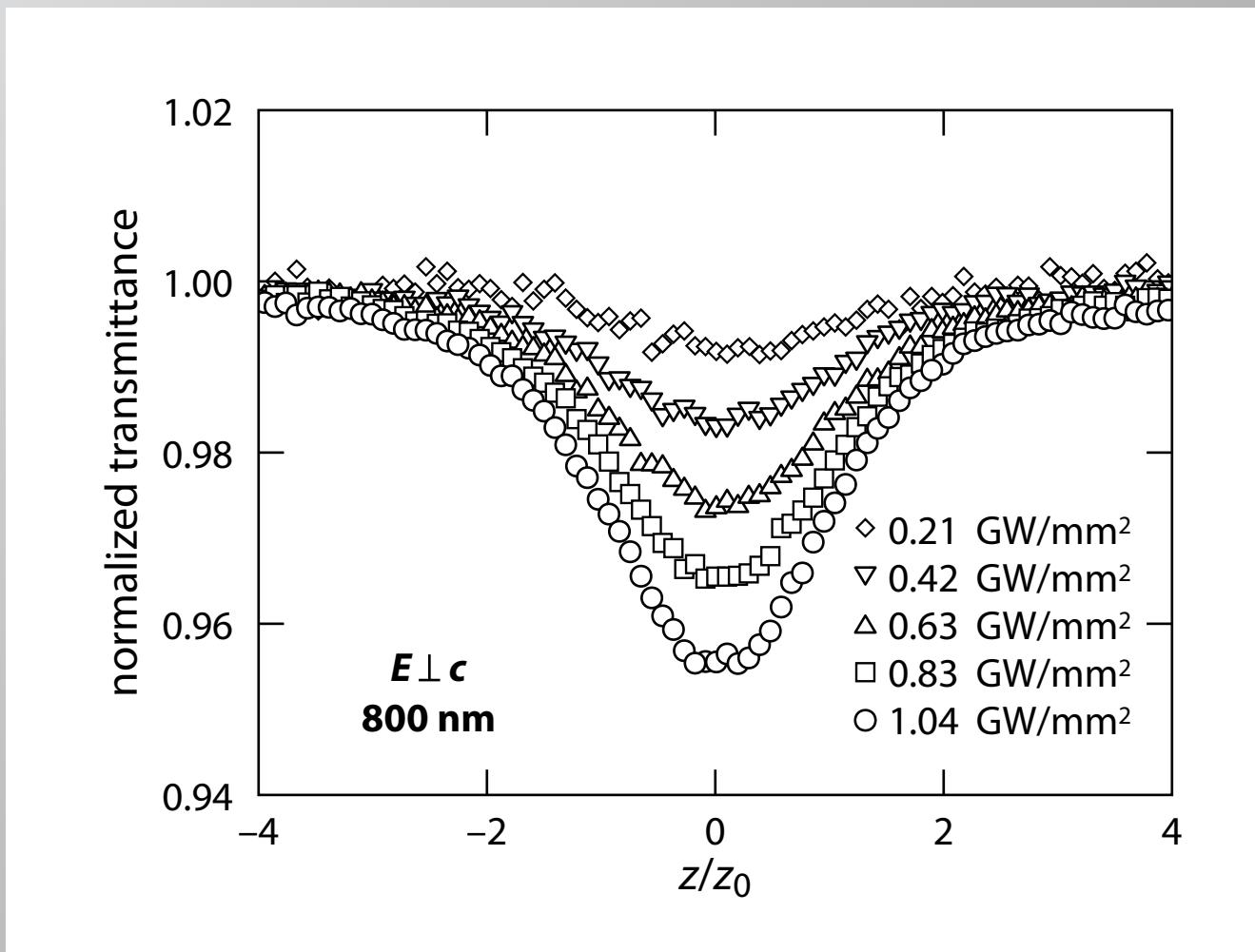
Experimental

Open aperture Z-scan of rutile



Experimental

Open aperture Z-scan of rutile



Outline

Experimental

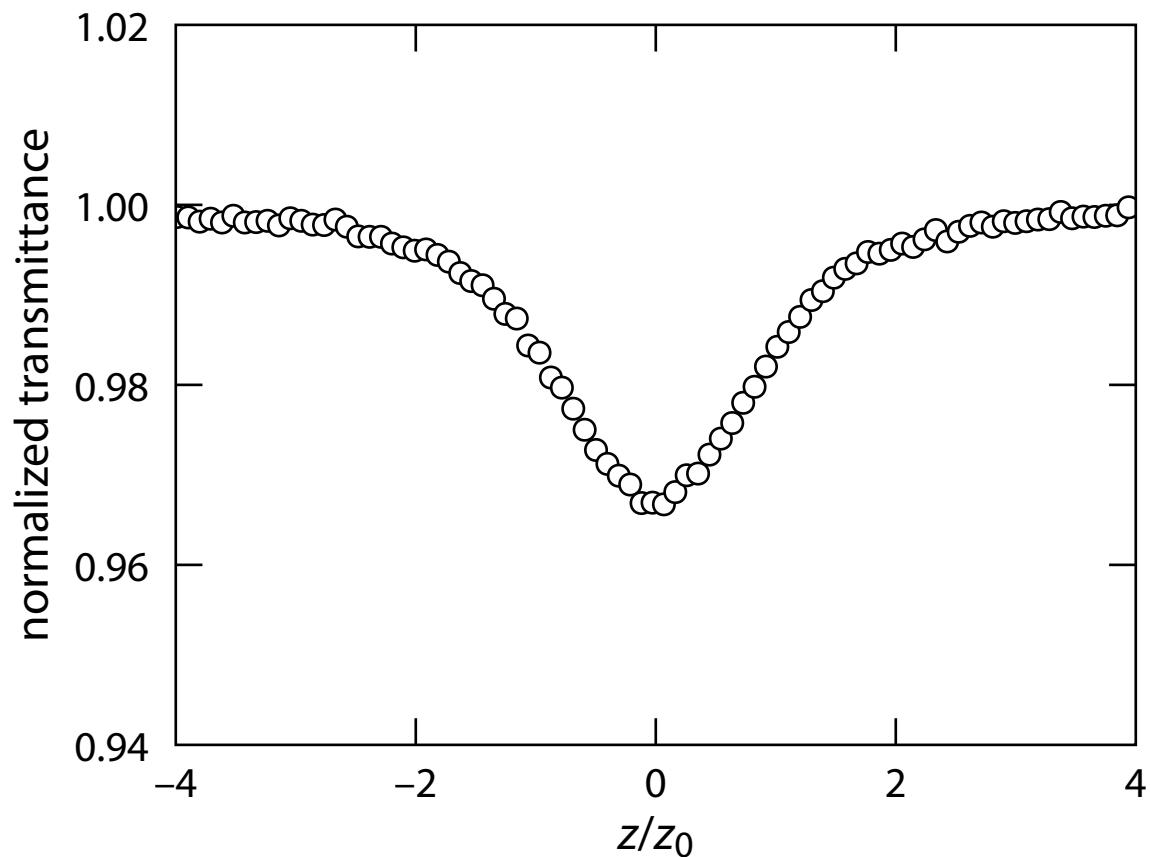
Modeling

Analysis

Conclusions

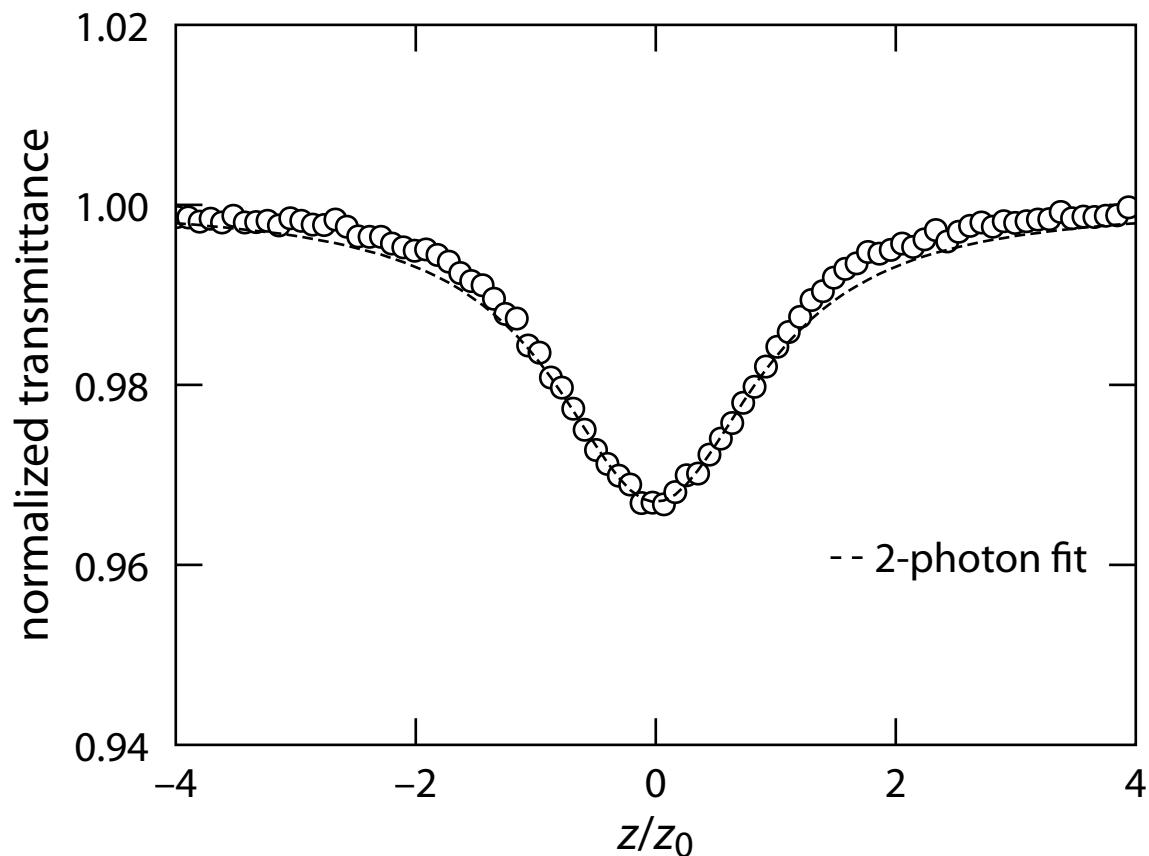
Modeling

Open aperture Z-scan of rutile



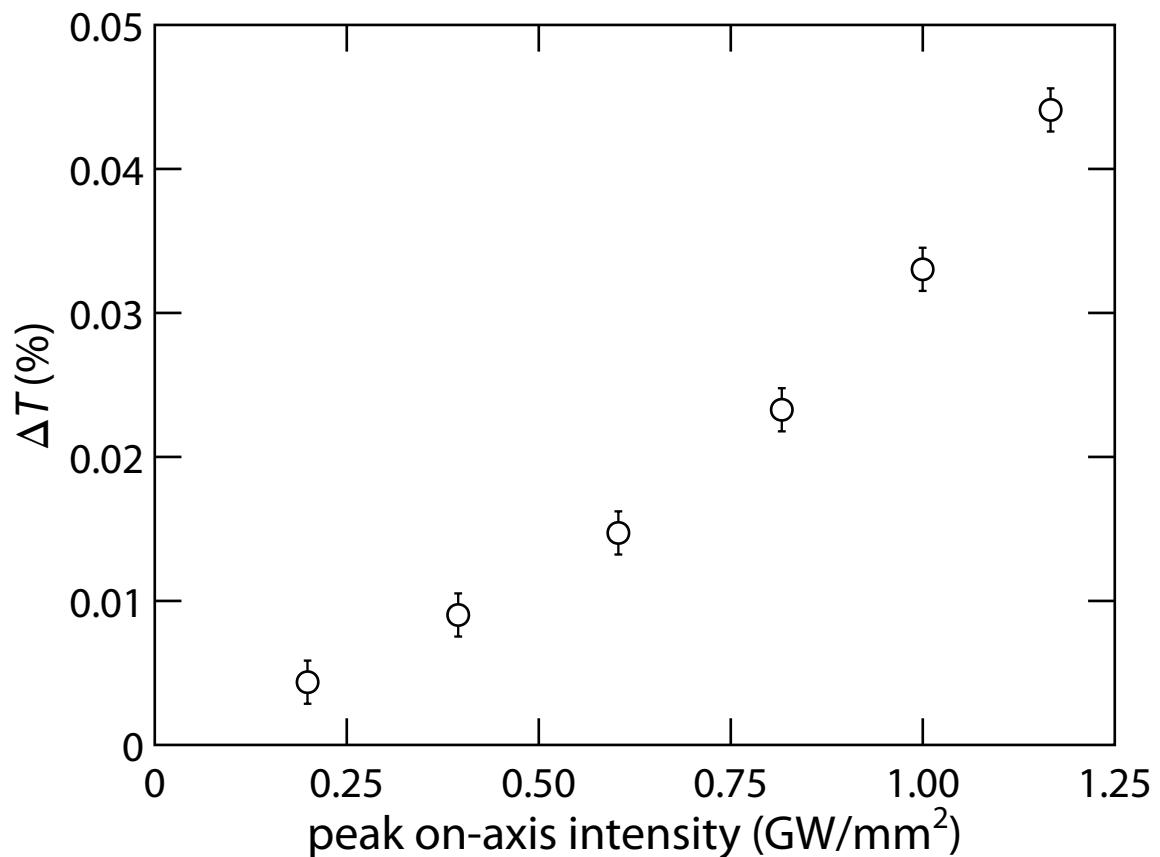
Modeling

Open aperture Z-scan of rutile



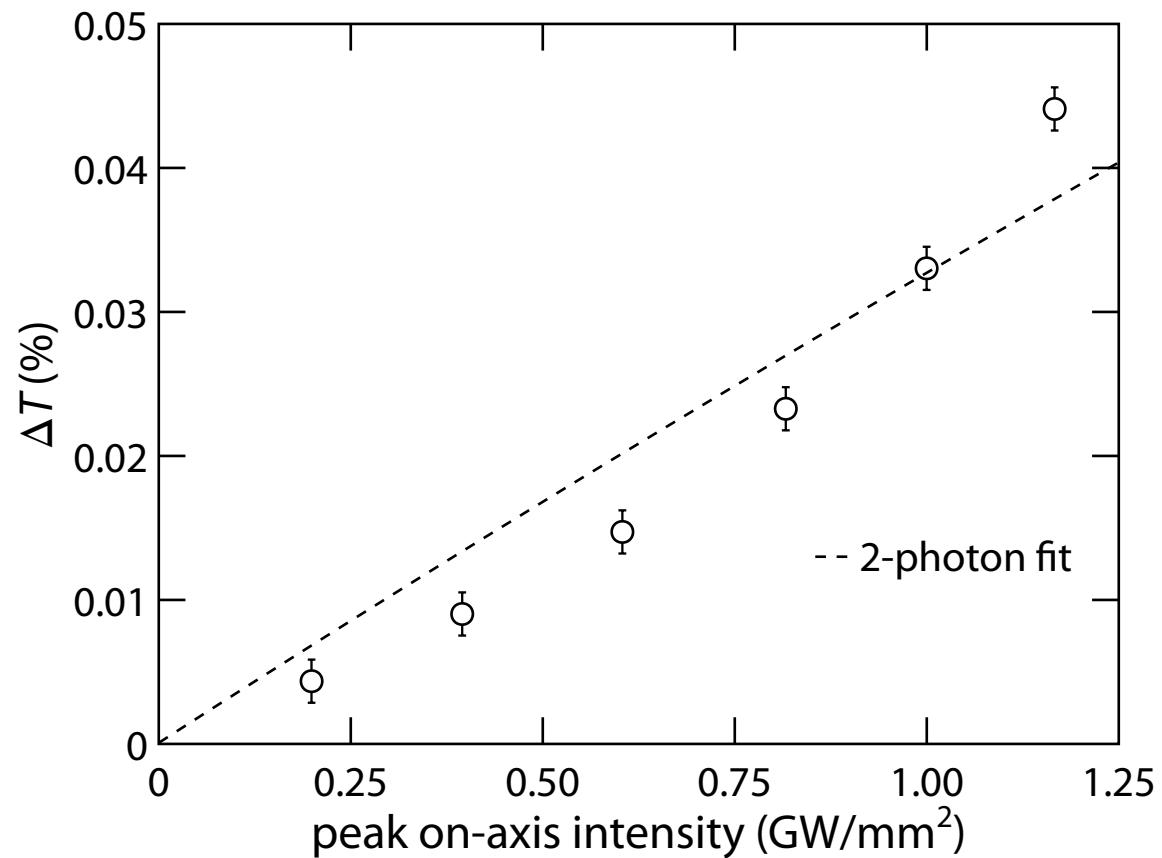
Modeling

Open aperture Z-scan of rutile



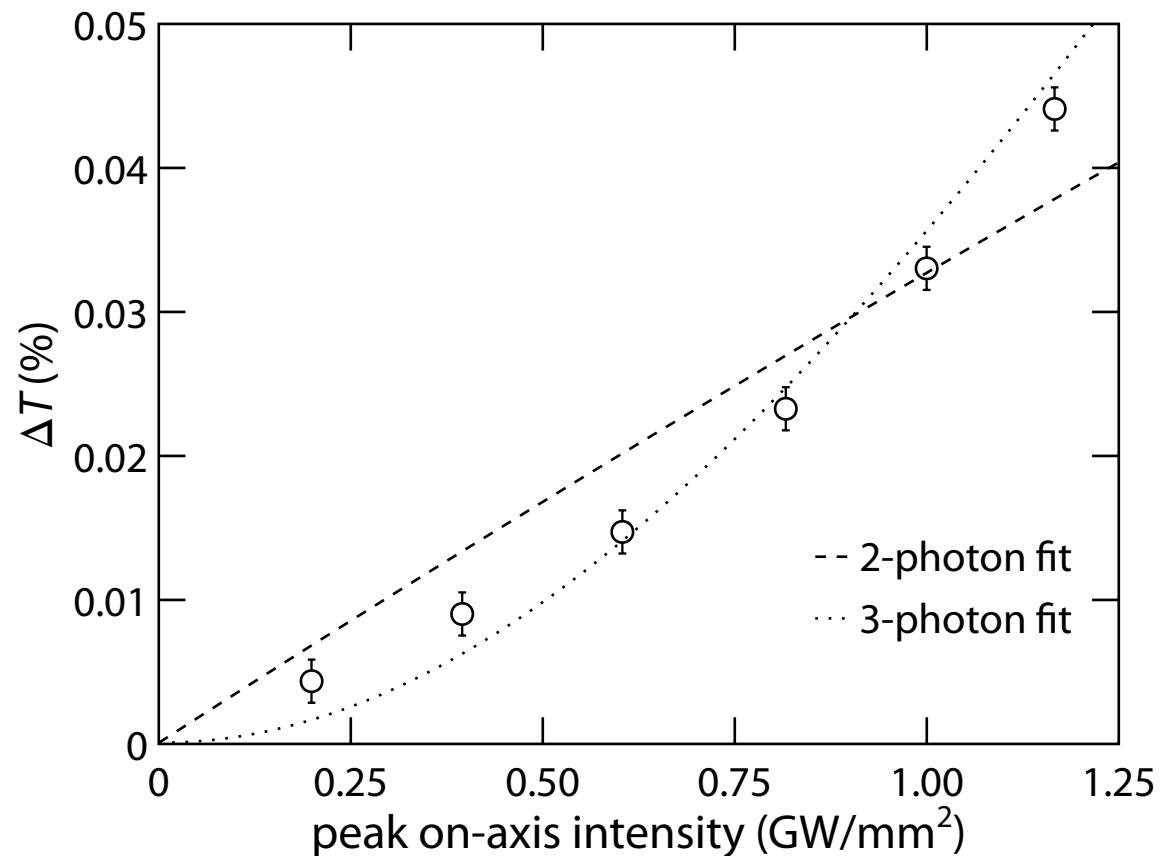
Modeling

Open aperture Z-scan of rutile



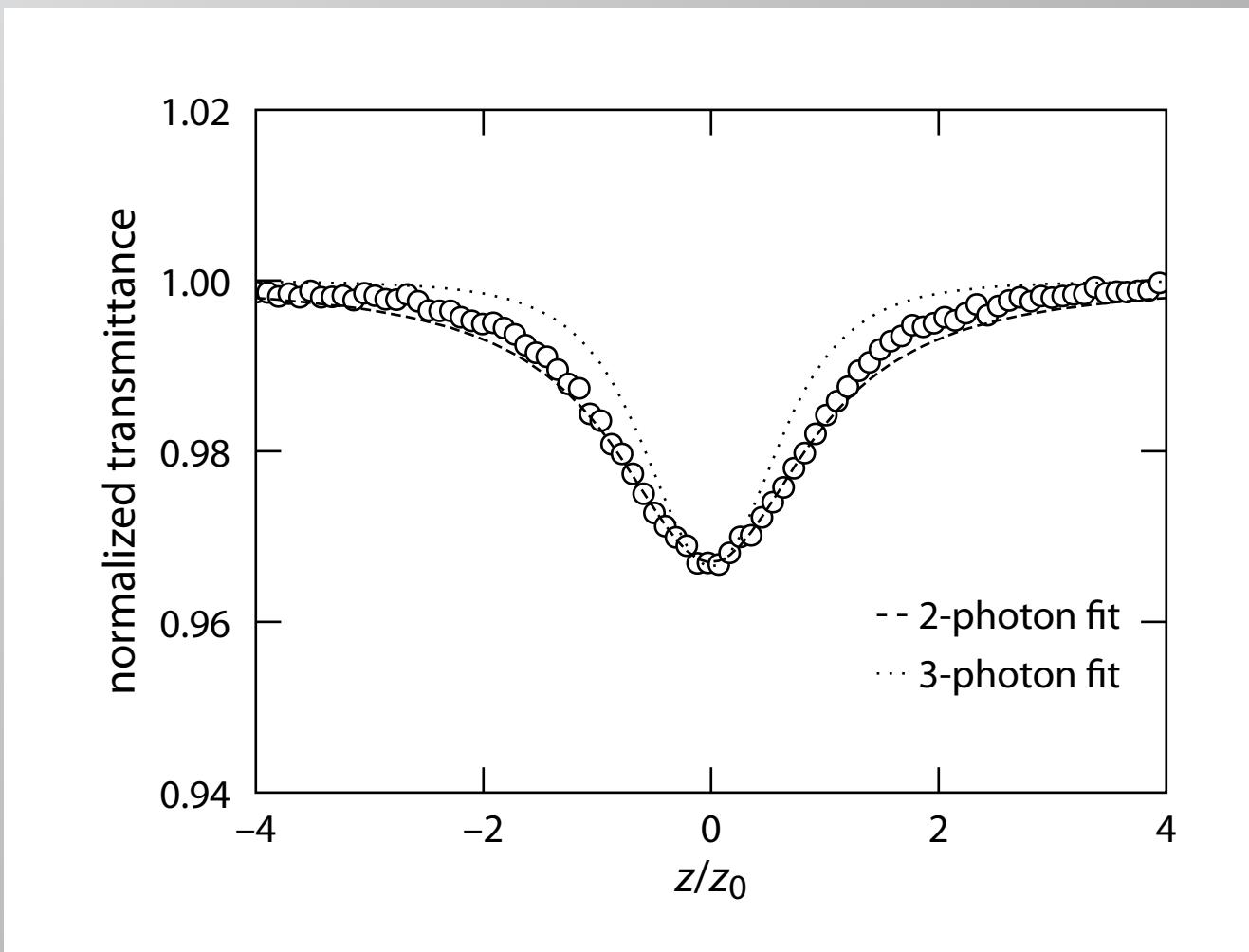
Modeling

Open aperture Z-scan of rutile



Modeling

Open aperture Z-scan of rutile



Modeling

Mixed multiphoton model

$$I_{in}[x, y, z, P(t)] = \frac{2P(t)}{\pi w_x(z)w_y(z)} \exp\left[-\frac{2x^2}{w_x^2(z)} - \frac{2y^2}{w_y^2(z)}\right]$$

Modeling

Mixed multiphoton model

$$I_{in}[x, y, z, P(t)] = \frac{2P(t)}{\pi w_x(z)w_y(z)} \exp\left[-\frac{2x^2}{w_x^2(z)} - \frac{2y^2}{w_y^2(z)}\right]$$

$$w_x(z) = \sqrt{{w_{x0}}^2 + \left(\frac{M_x^2 \lambda_0}{\pi w_{x0}}\right)^2 (z - z_{x0})^2}$$

Modeling

Mixed multiphoton model

$$I_{in}[x, y, z, P(t)] = \frac{2P(t)}{\pi w_x(z)w_y(z)} \exp\left[-\frac{2x^2}{w_x^2(z)} - \frac{2y^2}{w_y^2(z)}\right]$$

$$w_x(z) = \sqrt{{w_{x0}}^2 + \left(\frac{M_x^2 \lambda_0}{\pi w_{x0}}\right)^2 (z - z_{x0})^2}$$

$$\alpha(I) = \alpha_0 + \beta I + \gamma I^2$$

Modeling

Mixed multiphoton model

$$I_{in}[x, y, z, P(t)] = \frac{2P(t)}{\pi w_x(z)w_y(z)} \exp\left[-\frac{2x^2}{w_x^2(z)} - \frac{2y^2}{w_y^2(z)}\right]$$

$$w_x(z) = \sqrt{{w_{x0}}^2 + \left(\frac{M_x^2 \lambda_0}{\pi w_{x0}}\right)^2 (z - z_{x0})^2}$$

$$\alpha(I) = \alpha_0 + \beta I + \gamma I^2$$

$$\frac{dI}{dz'} = -\alpha(I)I$$

Modeling

Mixed multiphoton model

$$I_{in}[x, y, z, P(t)] = \frac{2P(t)}{\pi w_x(z)w_y(z)} \exp\left[-\frac{2x^2}{w_x^2(z)} - \frac{2y^2}{w_y^2(z)}\right]$$

$$w_x(z) = \sqrt{{w_{x0}}^2 + \left(\frac{M_x^2 \lambda_0}{\pi w_{x0}}\right)^2 (z - z_{x0})^2}$$

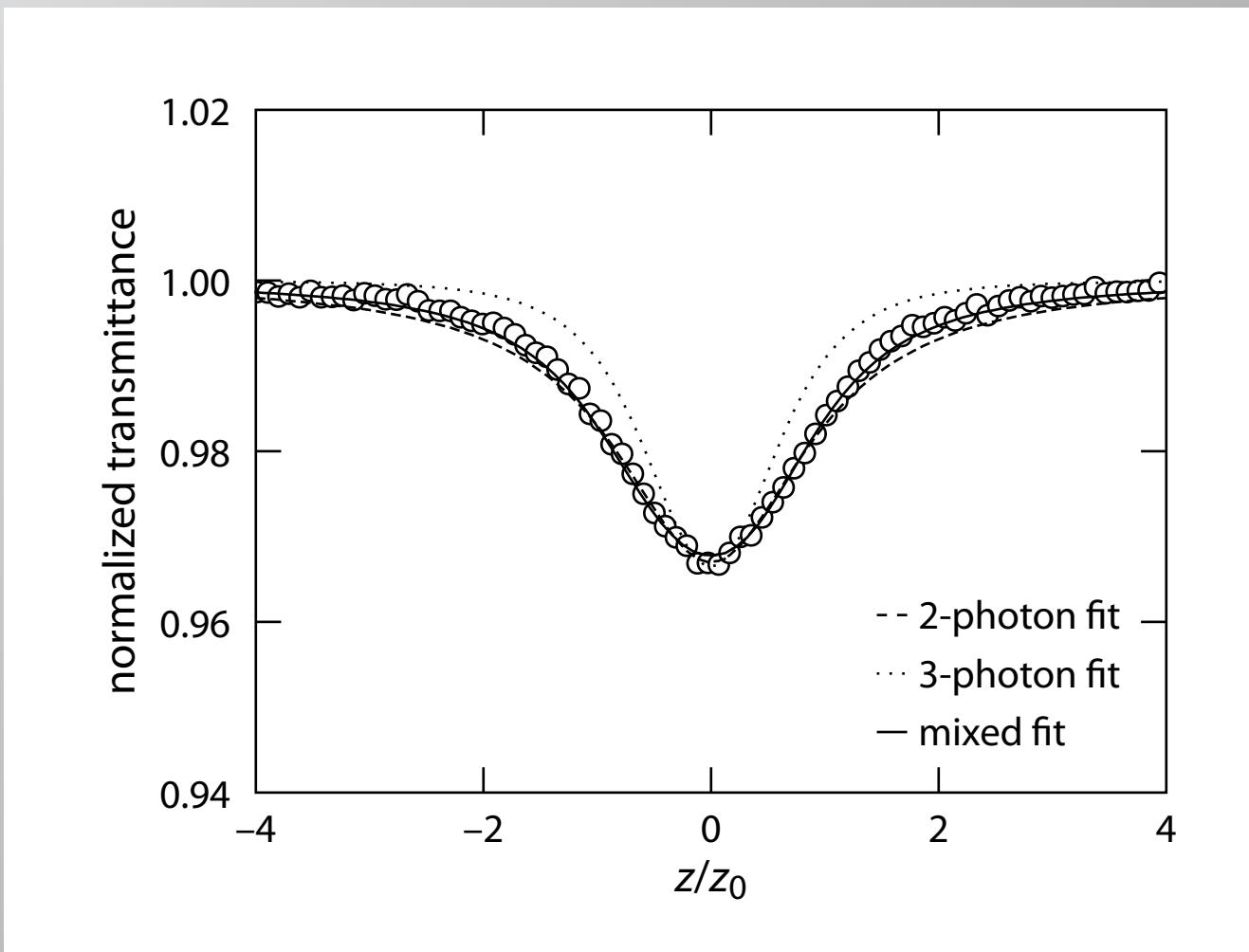
$$\alpha(I) = \alpha_0 + \beta I + \gamma I^2$$

$$\frac{dI}{dz'} = -\alpha(I)I$$

$$T(z) = \frac{\int P(t)T[z, P(t)]dt}{\int P(t) dt} = \frac{E_{out}(z)}{E_{in}}$$

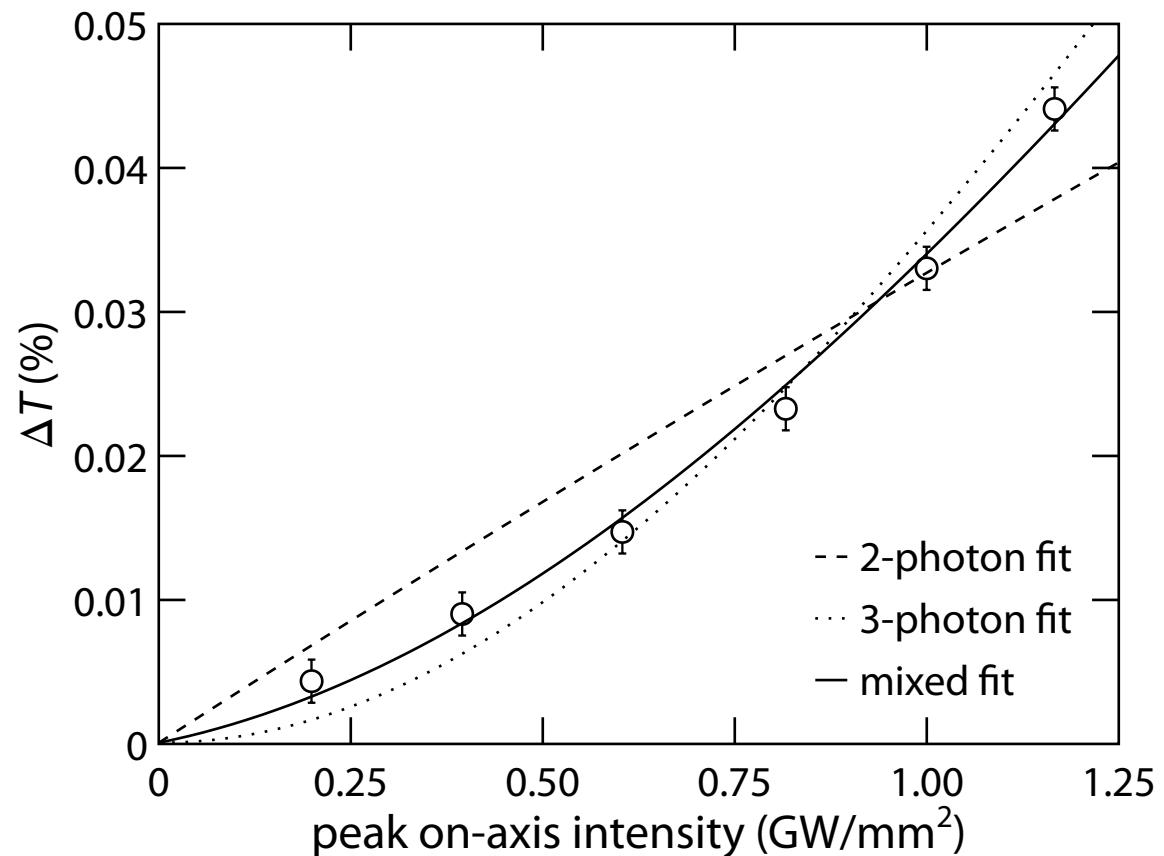
Modeling

Open aperture Z-scan of rutile



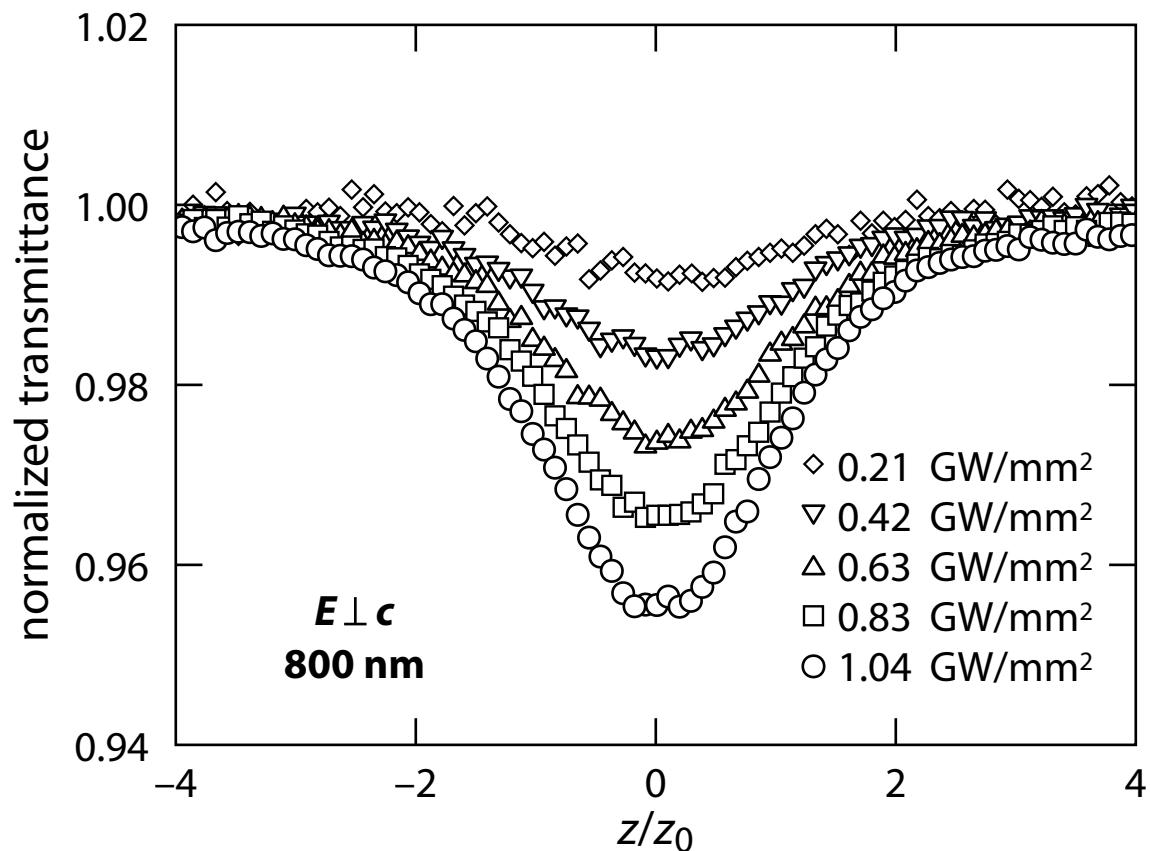
Modeling

Open aperture Z-scan of rutile



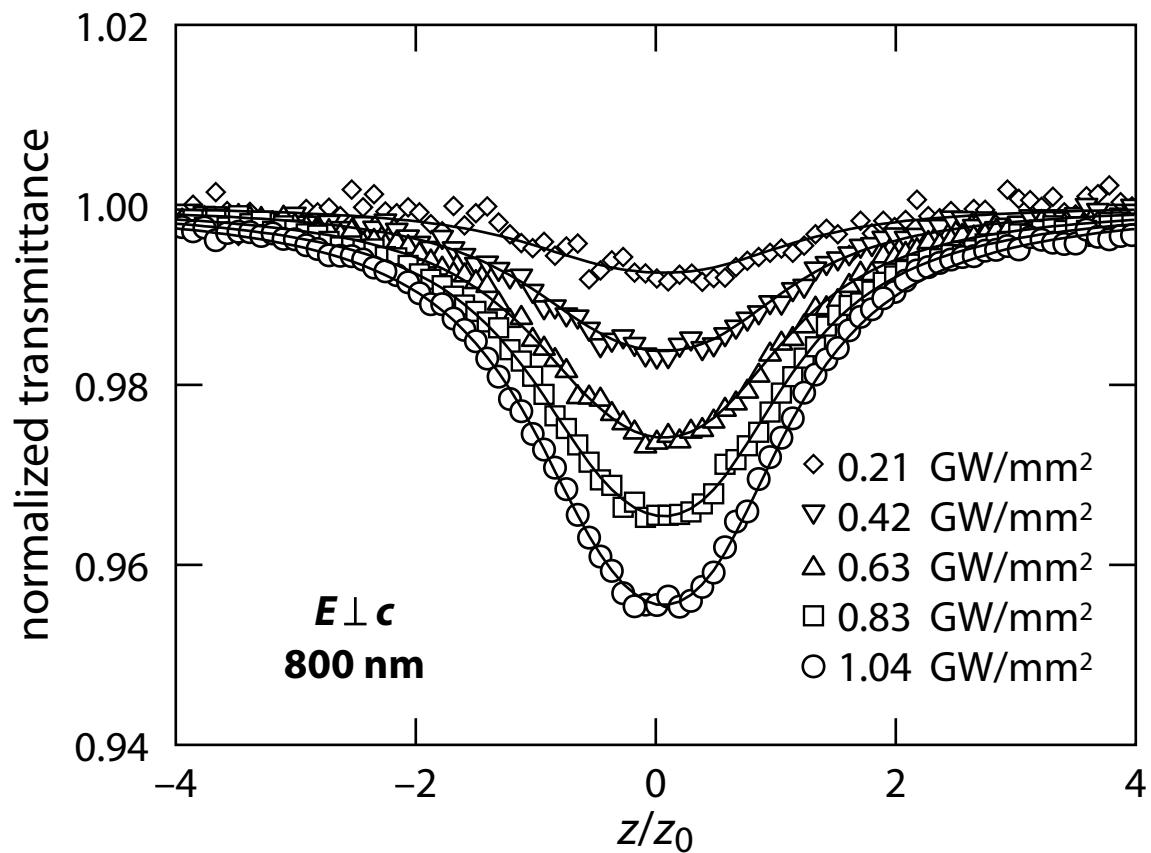
Modeling

Fitting method



Modeling

Fitting method



Outline

Experimental

Modeling

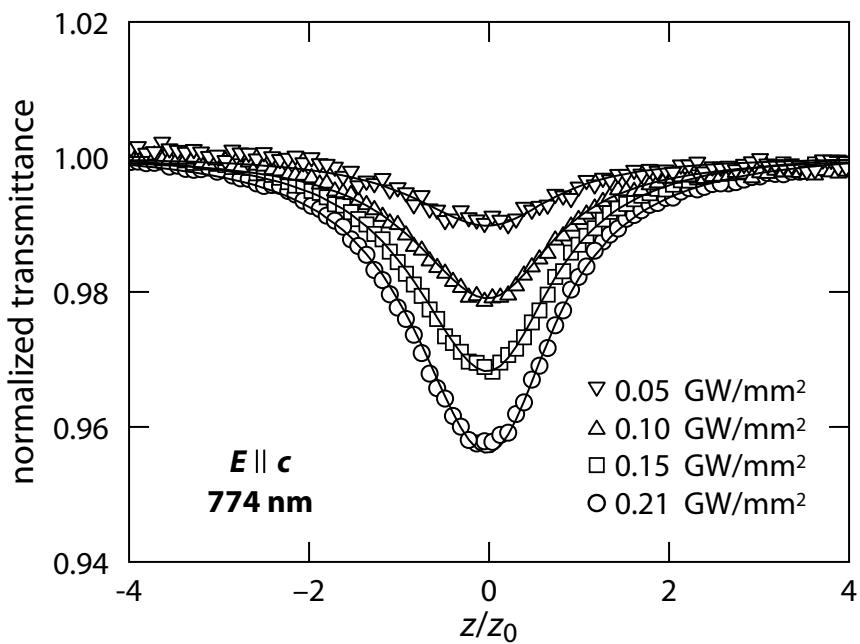
Analysis

Conclusions

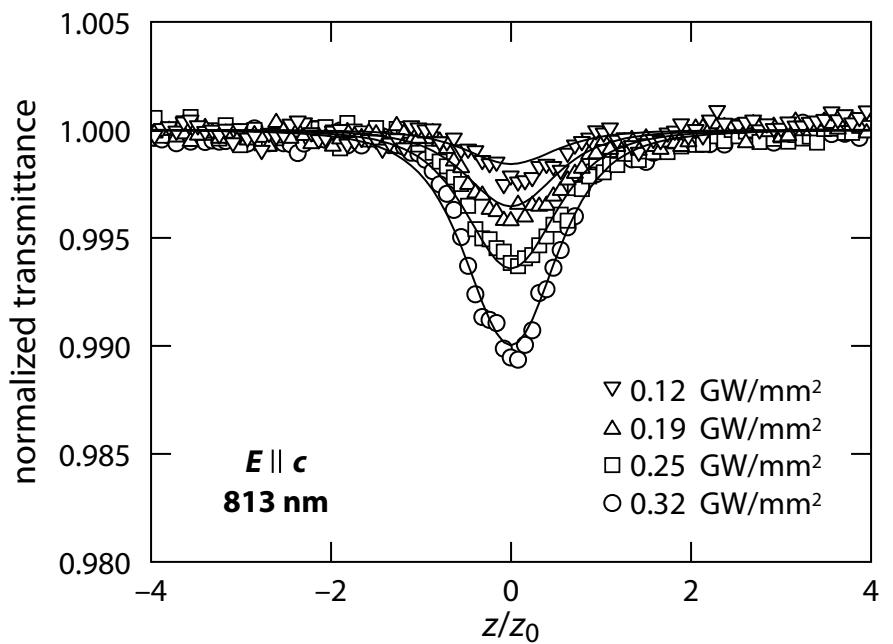
Analysis

$E \parallel c$

$2\hbar\omega=3.2$ eV



$2\hbar\omega=3.05$ eV



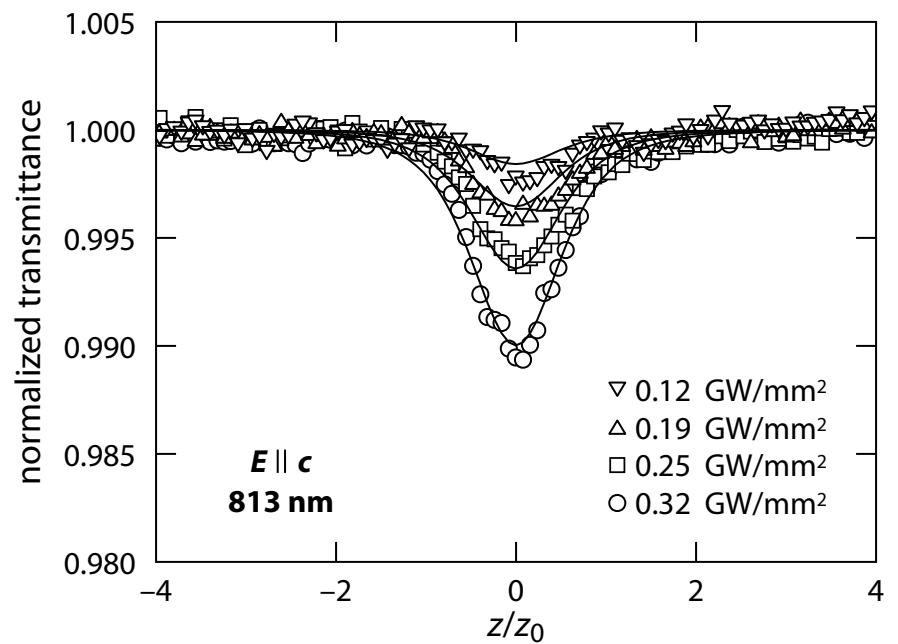
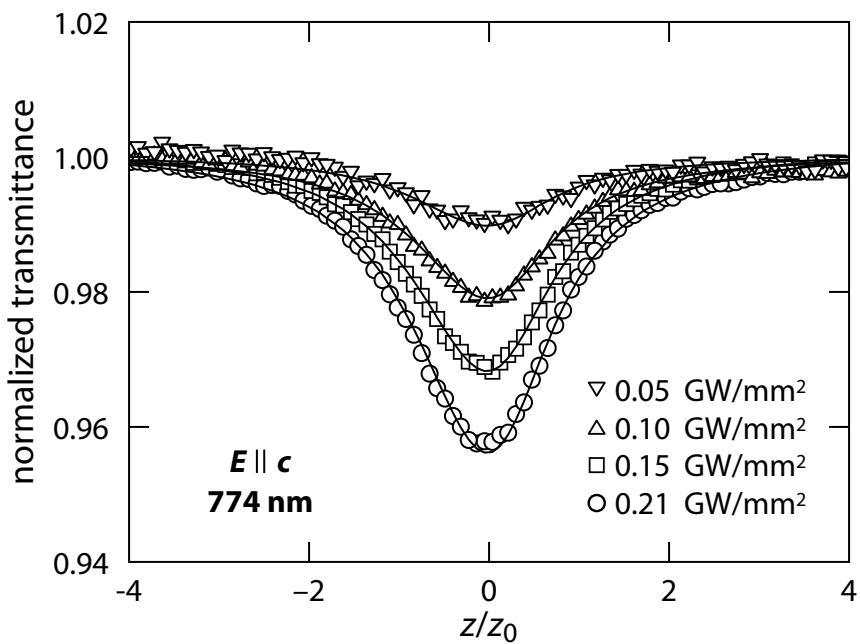
Analysis

$E \parallel c$

$2\hbar\omega=3.2$ eV

3.1 eV

$2\hbar\omega=3.05$ eV



Analysis

Fitting Results

extraordinary polarization ($E \parallel c$)

λ_0 (nm)	$2\hbar\omega$ (eV)	β (mm/GW)	γ (mm ³ /GW ²)
774	3.20	0.89	1.8
813	3.05	<10 ⁻⁷	0.9
$\pm 15\%$		factor of 2	

Analysis

Fitting Results

extraordinary polarization ($E \parallel c$)

λ_0 (nm)	$2\hbar\omega$ (eV)	β (mm/GW)	γ (mm ³ /GW ²)
774	3.20	0.89	1.8
813	3.05	<10 ⁻⁷	0.9
$\pm 15\%$			factor of 2

We can see the indirect bandgap at 3.1 eV

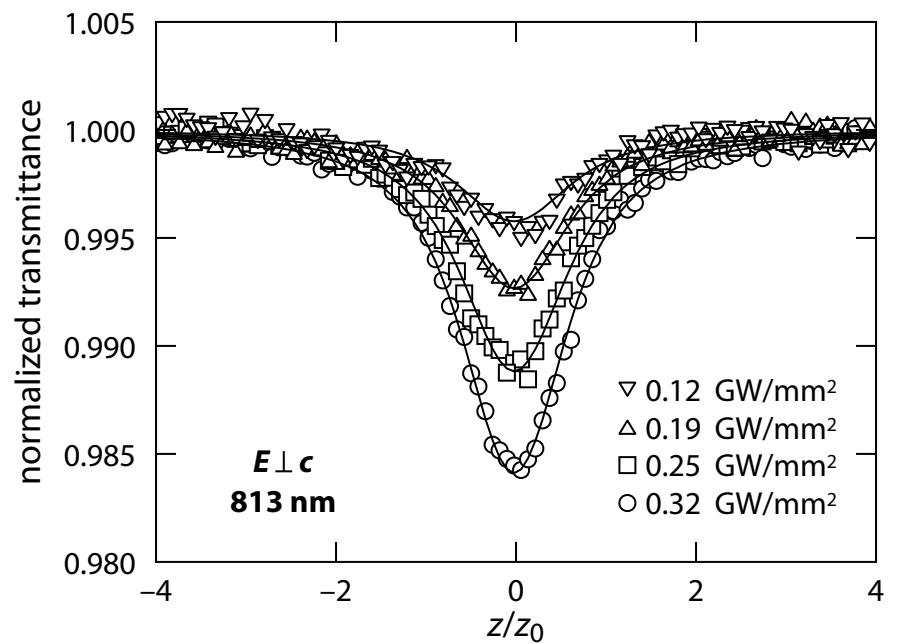
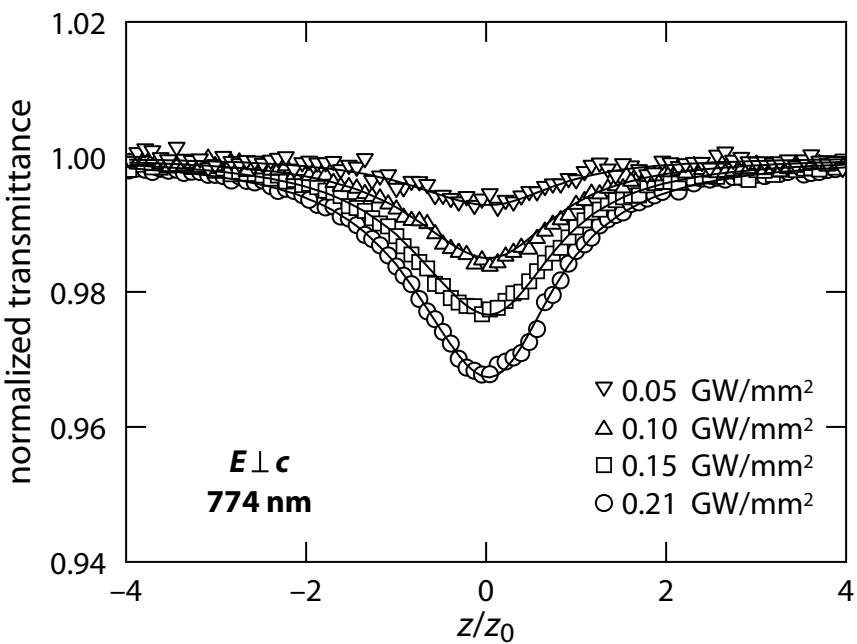
Analysis

$E \perp c$

$2\hbar\omega=3.2$ eV

3.1 eV

$2\hbar\omega=3.05$ eV



Analysis

Fitting Results

ordinary polarization ($E \perp c$)

λ_0 (nm)	$2\hbar\omega$ (eV)	β (mm/GW)	γ (mm ³ /GW ²)
774	3.20	0.54	1.1
813	3.05	0.08	0.8

$\pm 15\%$ factor of 2

Direct forbidden bandgap at 3.062 eV

K. Watanabe and K. Inoue, Phys. Rev. B 41, 7957-7960 (1990).

Analysis

Fitting Results

extraordinary polarization ($E \parallel c$)

λ_0 (nm)	$2\hbar\omega$ (eV)	β (mm/GW)	γ (mm ³ /GW ²)	$\frac{n_2}{\beta\lambda}$
774	3.20	0.89	1.8	1.1
813	3.05	<10 ⁻⁷	0.9	>10 ⁶
$\pm 15\%$			factor of 2	

Analysis

Fitting Results

ordinary polarization ($E \perp c$)

λ_0 (nm)	$2\hbar\omega$ (eV)	β (mm/GW)	γ (mm ³ /GW ²)	$\frac{n_2}{\beta\lambda}$
774	3.20	0.54	1.1	1.9
813	3.05	0.08	0.8	12.1

$\pm 15\%$ factor of 2

Analysis

Fitting Results

extraordinary polarization ($E \parallel c$)

λ_0 (nm)	$2\hbar\omega$ (eV)	β (mm/GW)	γ (mm ³ /GW ²)	$\frac{n_2}{\beta\lambda}$	I_{\max}^{3PA} (GW/mm ²)
774	3.20	0.89	1.8	1.1	0.57
813	3.05	<10 ⁻⁷	0.9	>10 ⁶	1.10

$\pm 15\%$

factor of 2

Analysis

Fitting Results

ordinary polarization ($E \perp c$)

λ_0 (nm)	$2\hbar\omega$ (eV)	β (mm/GW)	γ (mm ³ /GW ²)	$\frac{n_2}{\beta\lambda}$	I_{\max}^{3PA} (GW/mm ²)
774	3.20	0.54	1.1	1.9	0.93
813	3.05	0.08	0.8	12.1	1.20

$\pm 15\%$

factor of 2

Conclusions

Two- and three-photon absorption in rutile

Two-photon absorption is below 1 mm/GW

Three-photon absorption is below $2 \text{ mm}^3/\text{GW}^2$

Negligible 2PA at 813 nm for E_{llc}

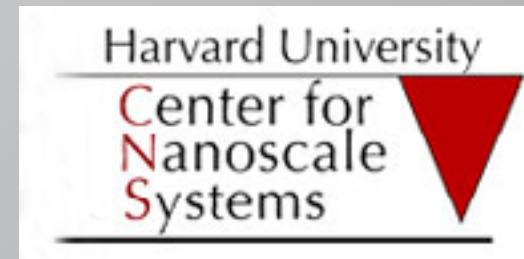
Conclusions

Two-photon figures of merit greater than 12
for $\lambda_0 > 813$ nm.

Three-photon absorption limits peak intensity
to ~ 0.50 GW/mm².

Rutile is a promising for all-optical switching
for wavelengths greater than 800 nm.

Funding provided by:



Chris Evans



Jon Bradley



Erwin Martí



Eric Mazur

Any questions?

**C. C. Evans, J. D. B. Bradley, E. A. Martí-Panameño, and E. Mazur,
“Mixed two- and three-photon absorption in bulk rutile (TiO_2) around 800 nm,”
Opt. Express 20, 3118-3128 (2012).**



Chris Evans



Jon Bradley



Erwin Martí



Eric Mazur