# **Peer Instruction**



TAS

# @eric\_mazur

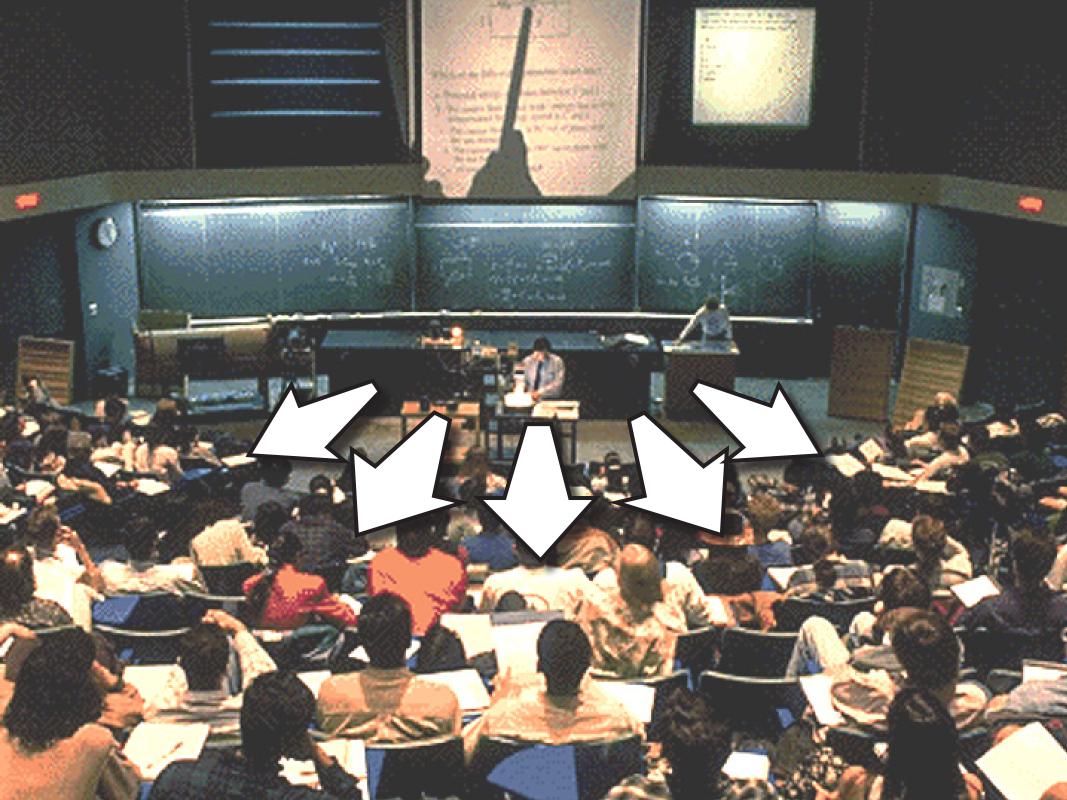
Workshop for Experienced Physics & Astronomy Faculty College Park, MD, 18 March 2016













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# 1. transfer of information

# 1. transfer of information

# 2. assimilation of that information

# 1. transfer of information (in class)

# 2. assimilation of that information

# 1. transfer of information (in class)

# 2. assimilation of that information (out of class)

# Should focus on THIS!

1. transfer of information (i)

# 2. assimilation of that information (out of class)

#### 1. transfer of information (in class)

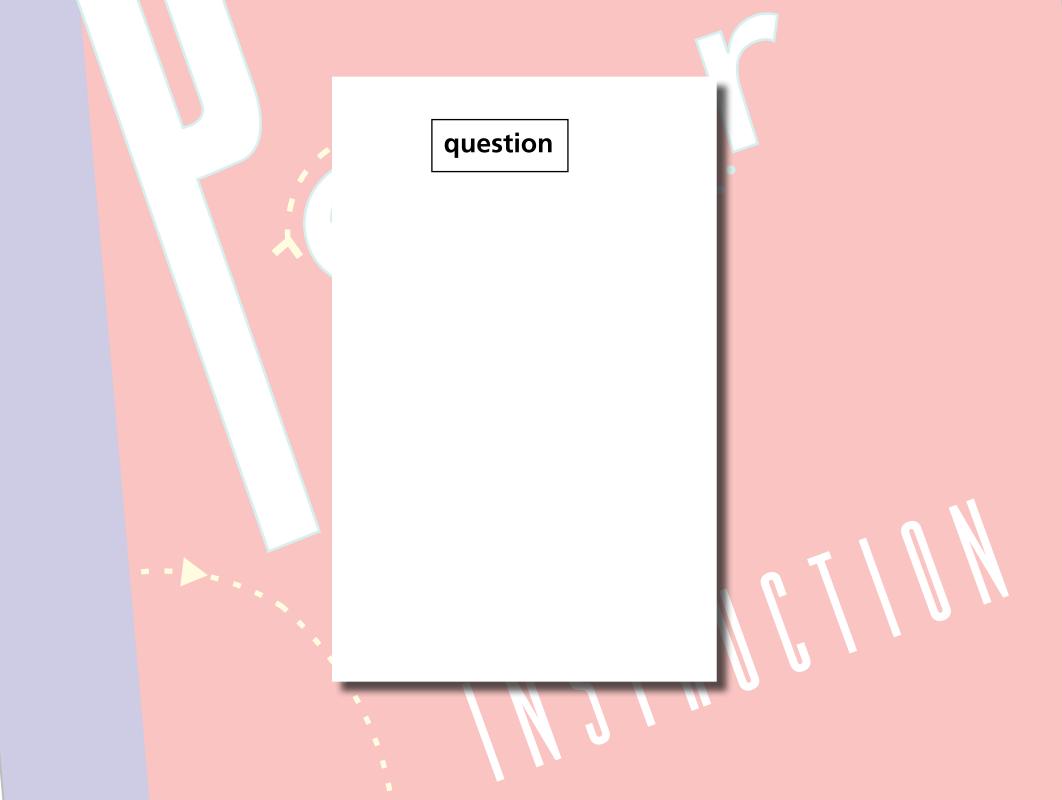
# 2. assimilation of that information (out of class)

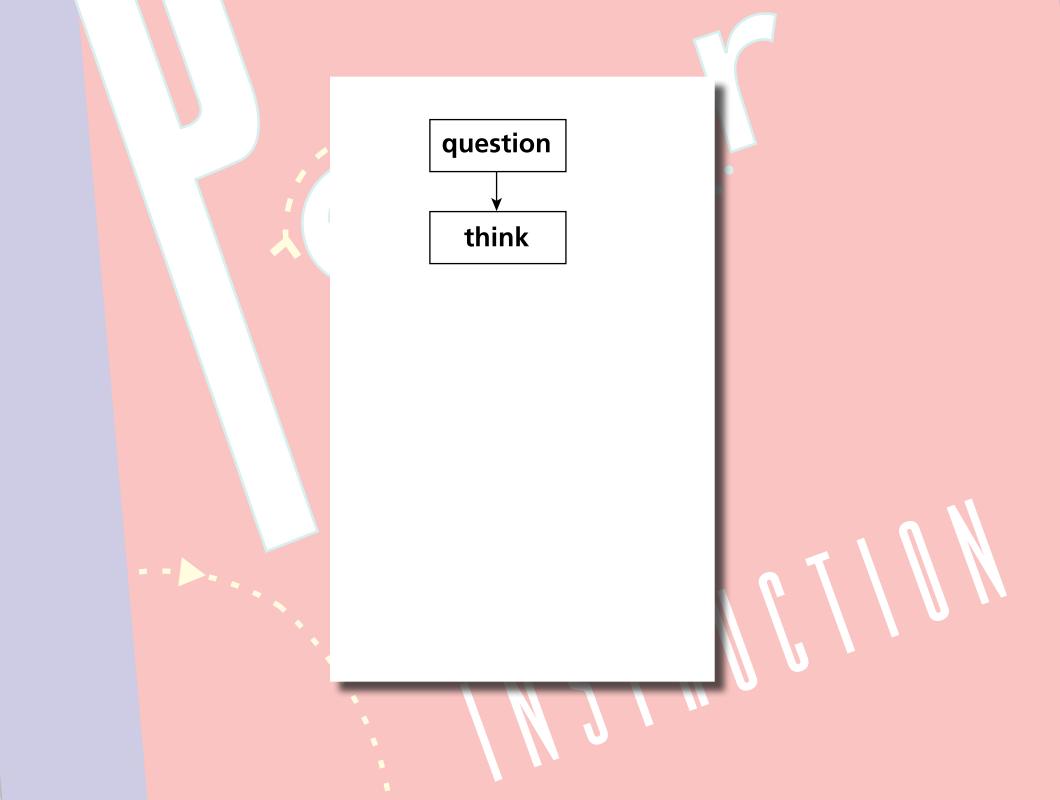
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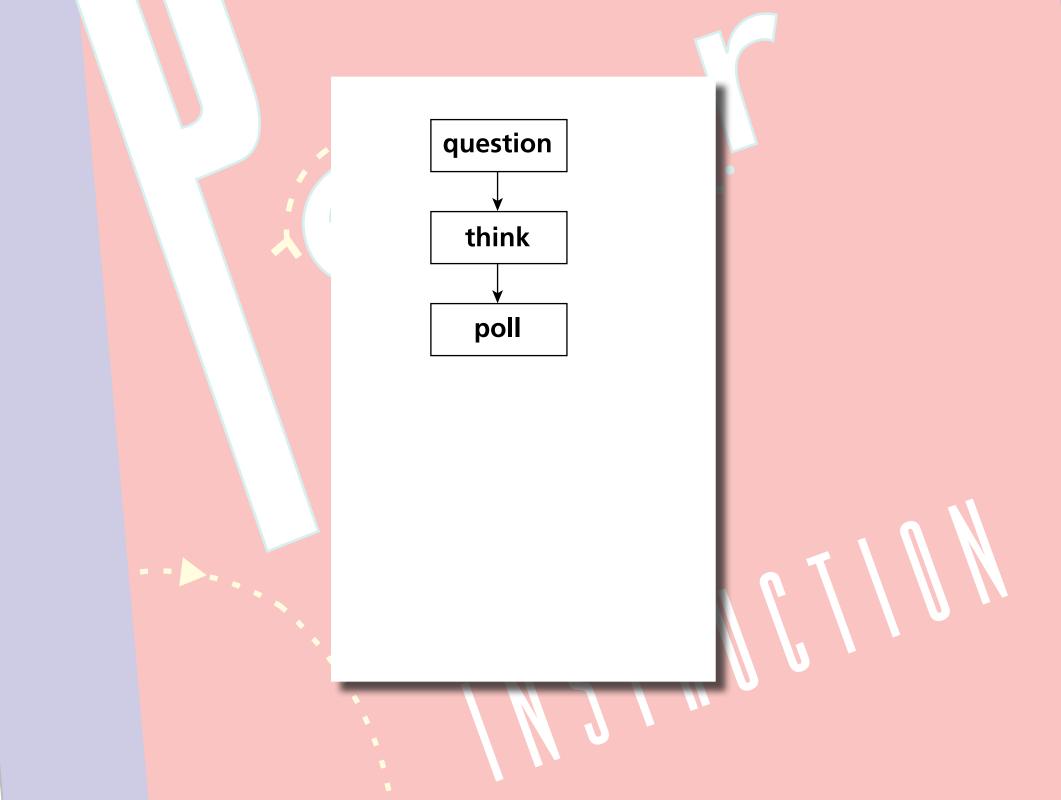
# 2. assimilation of that information (in class)

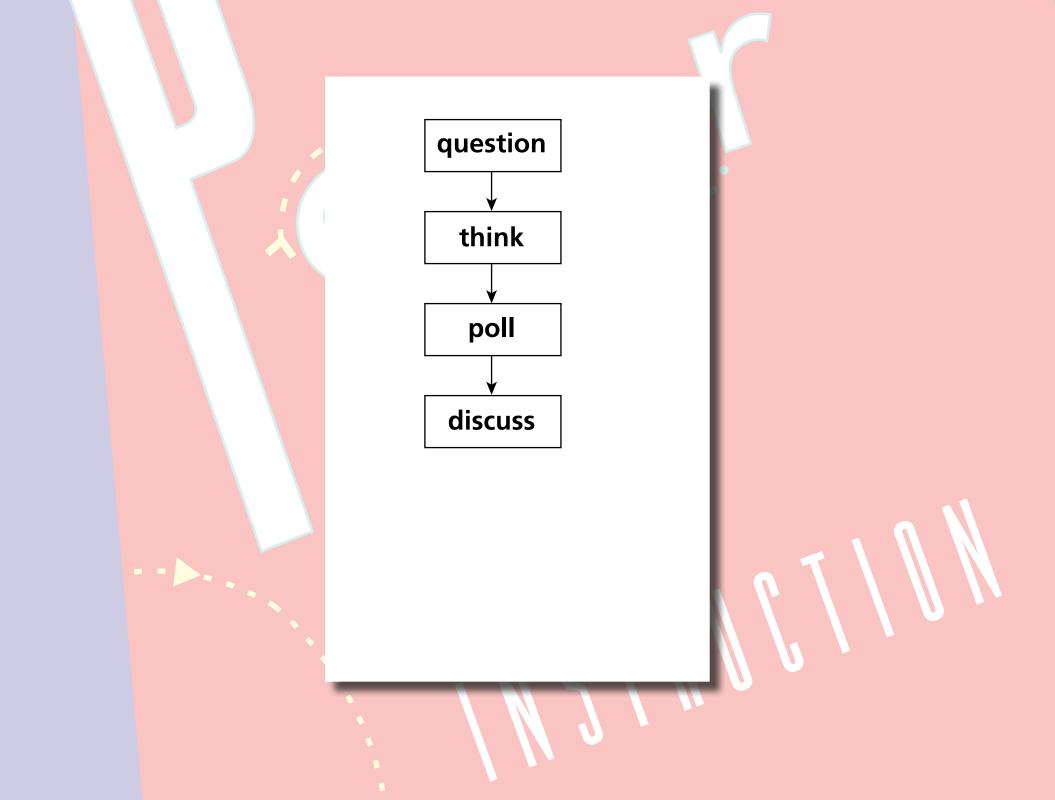
### **1. transfer of information (out of class)**

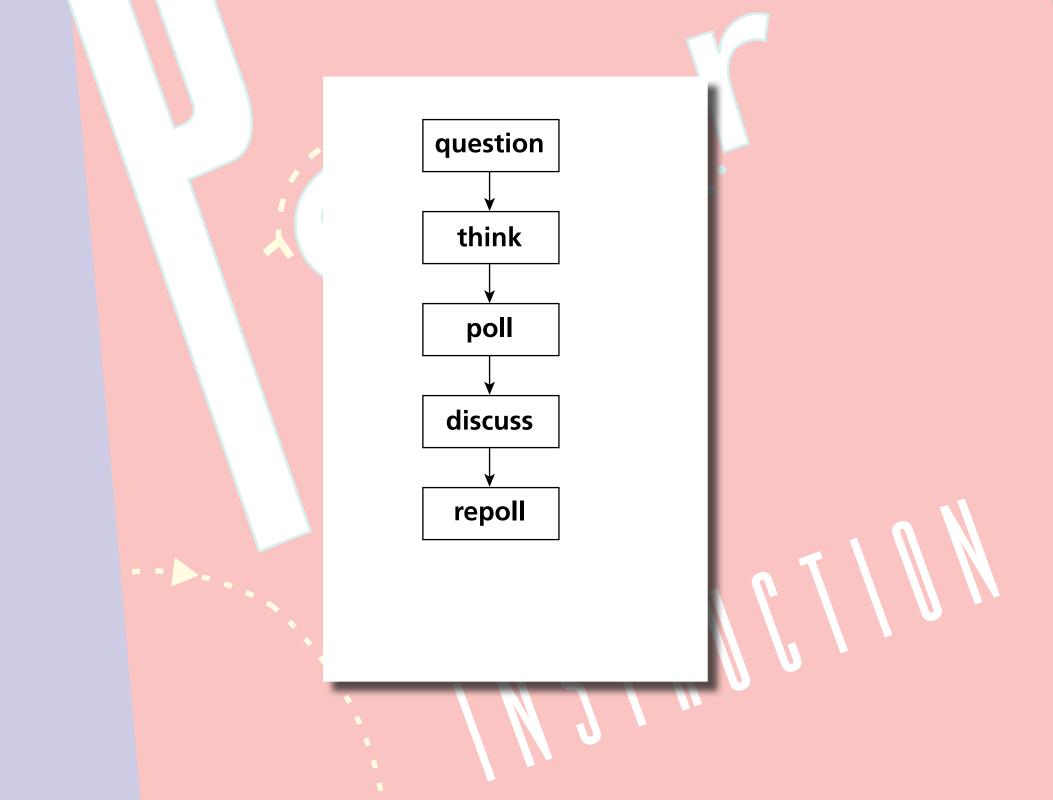
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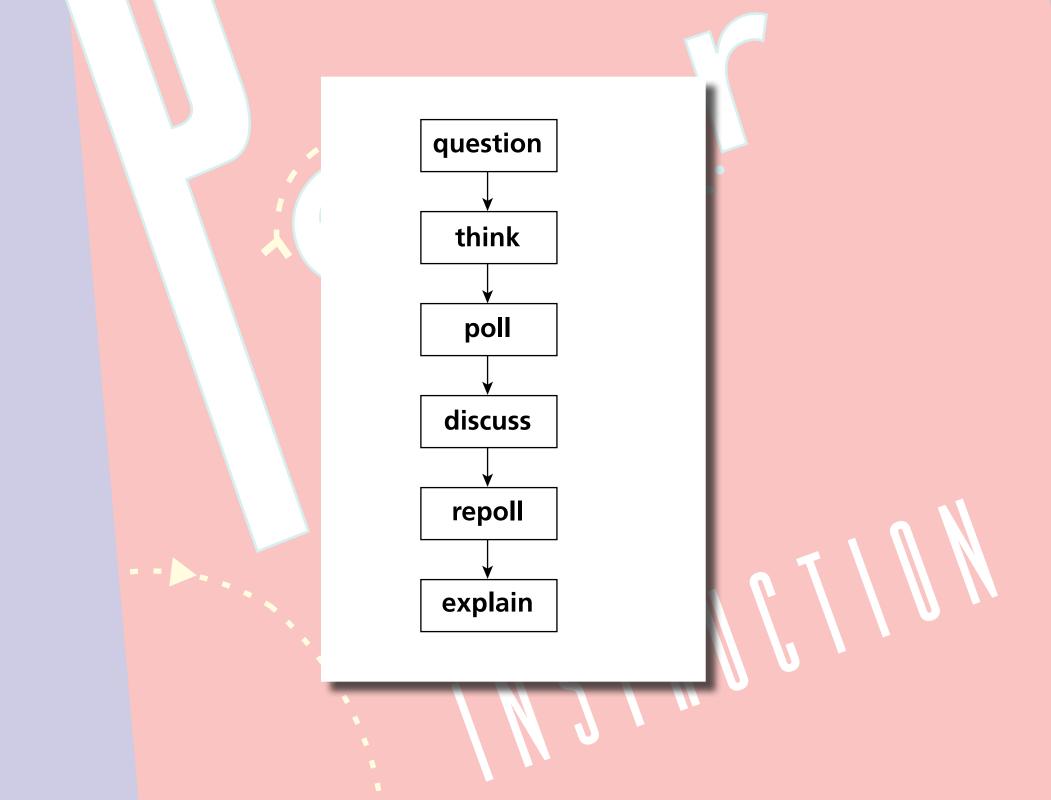


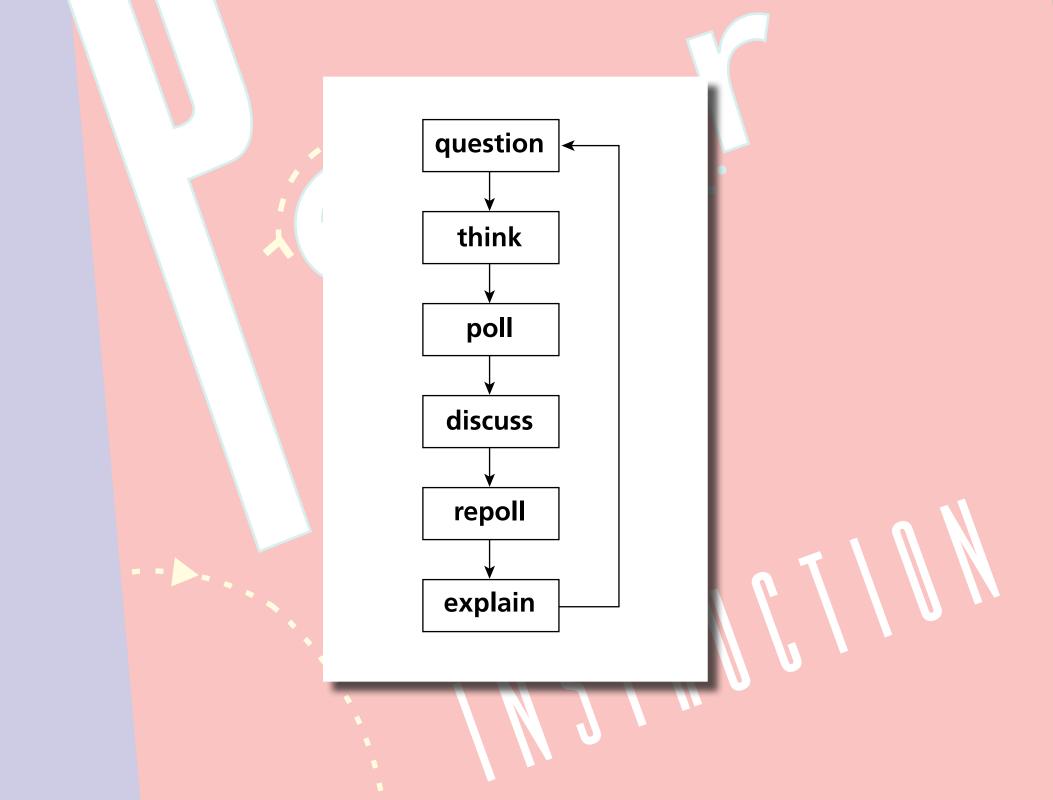


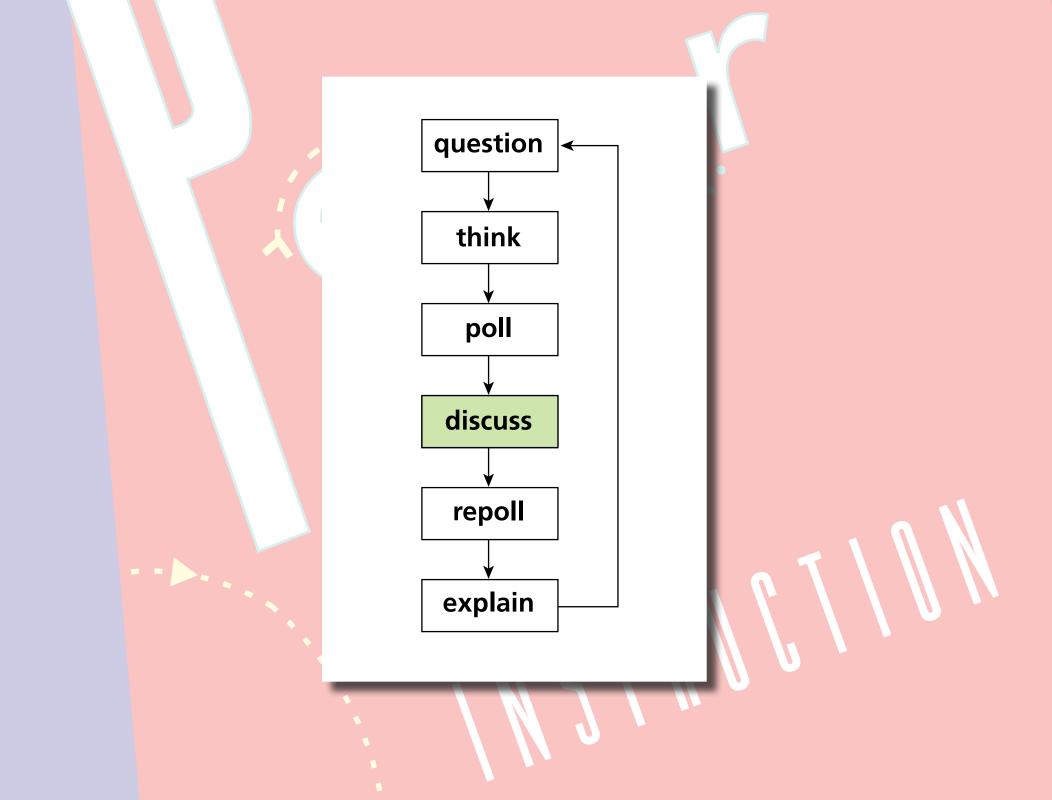


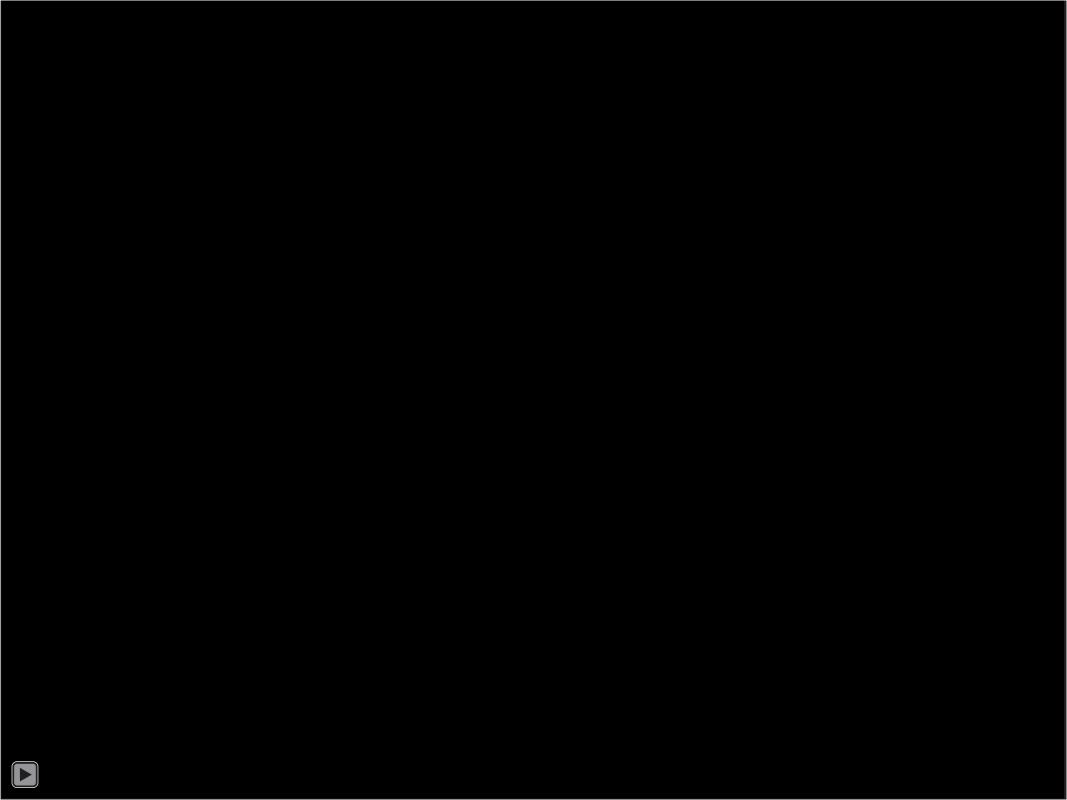




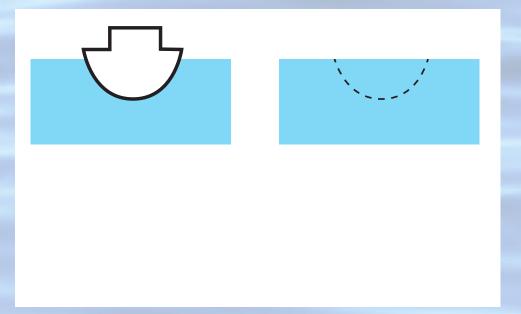




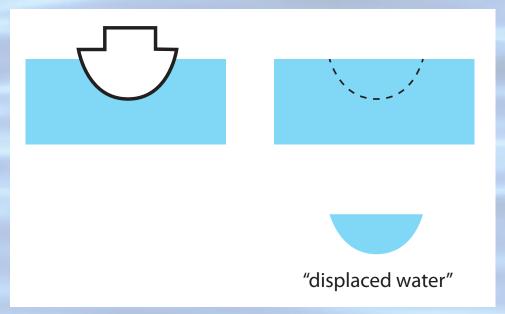




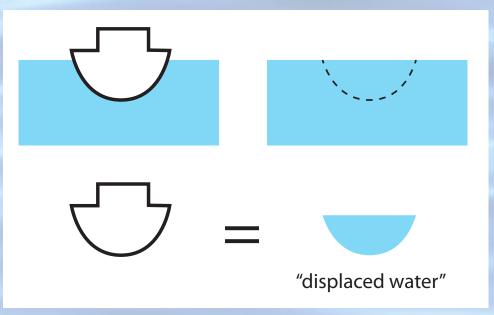
# **Archimedes Principle**



The volume of displaced fluid is equal to the volume of the submerged portion of the object.



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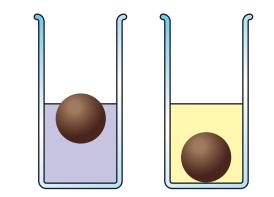


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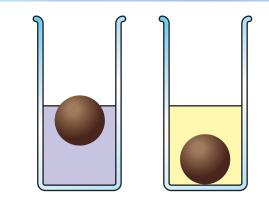
The volume of displaced fluid is equal to the volume of the submerged portion of the object.

"displaced water"

Consider an object that floats in water, but sinks in oil. When the object floats in water, most of it is submerged.

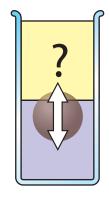


Consider an object that floats in water, but sinks in oil. When the object floats in water, most of it is submerged.



If we slowly pour the oil on top of the water so it completely covers the object, the object

moves up.
 stays in the same place.
 moves down.



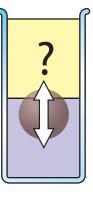
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# he water so it completely



# Before I tell you the answer, let's analyze what happened.

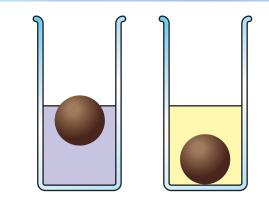
1. made a commitment

made a commitment
 externalized your answer

- 1. made a commitment
- 2. externalized your answer
- 3. moved from the answer/fact to reasoning

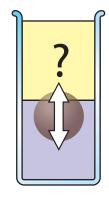
- 1. made a commitment
- 2. externalized your answer
- 3. moved from the answer/fact to reasoning
- 4. became emotionally invested in the learning process

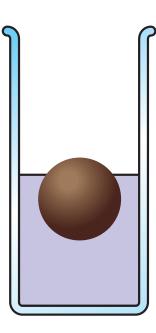
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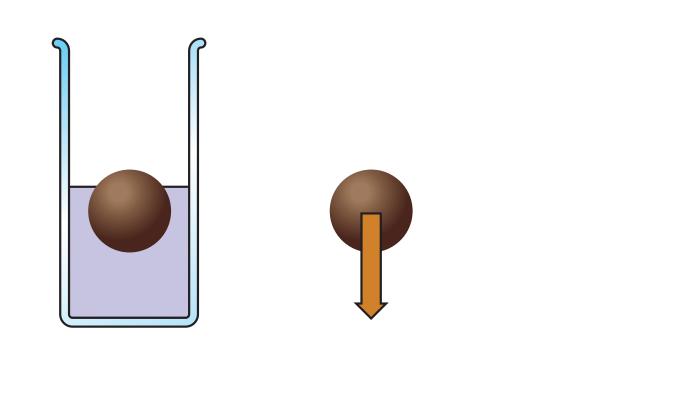


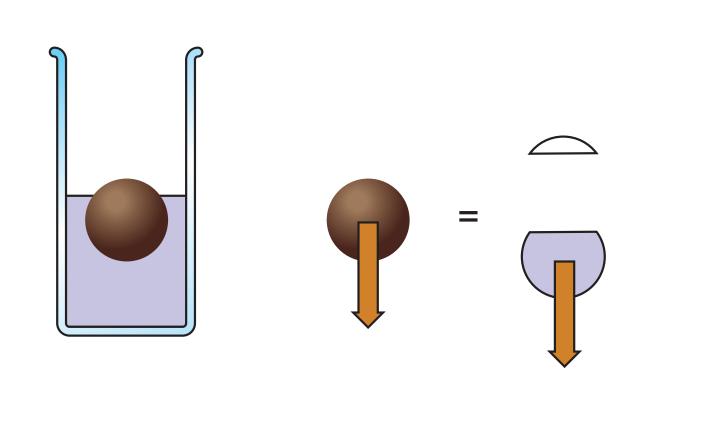
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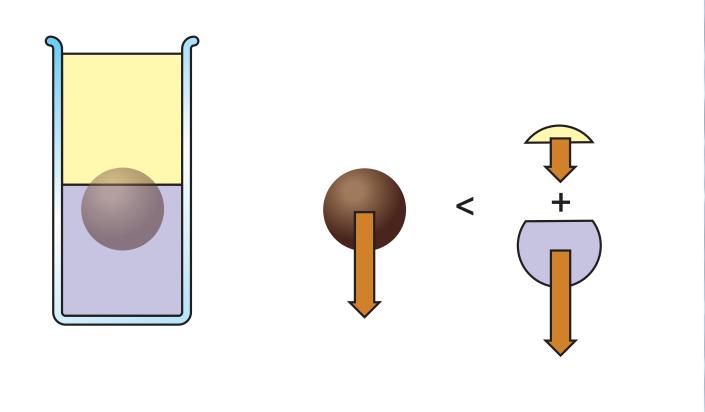
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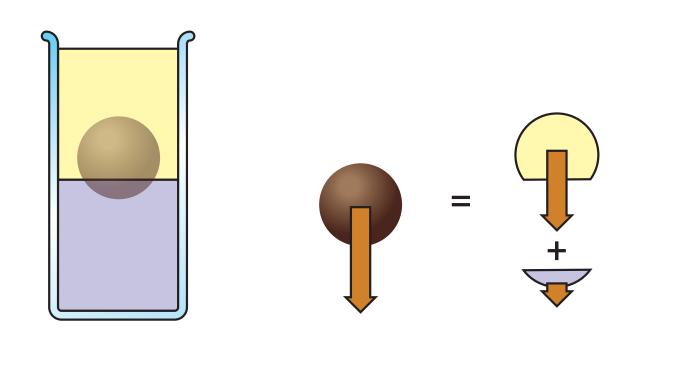


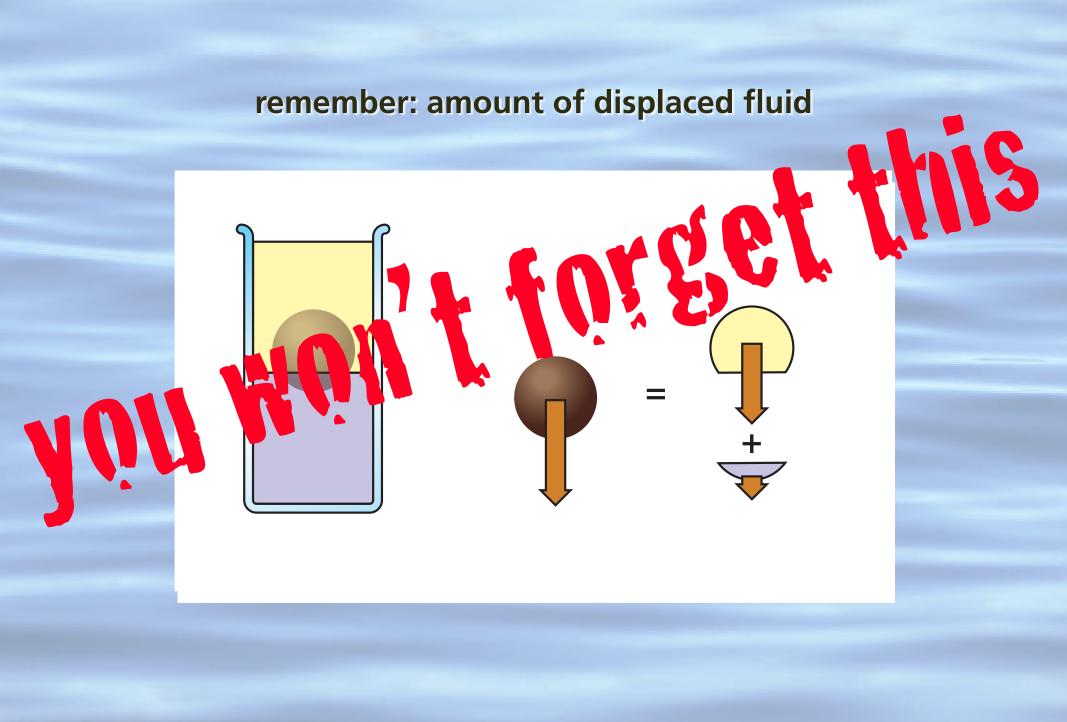








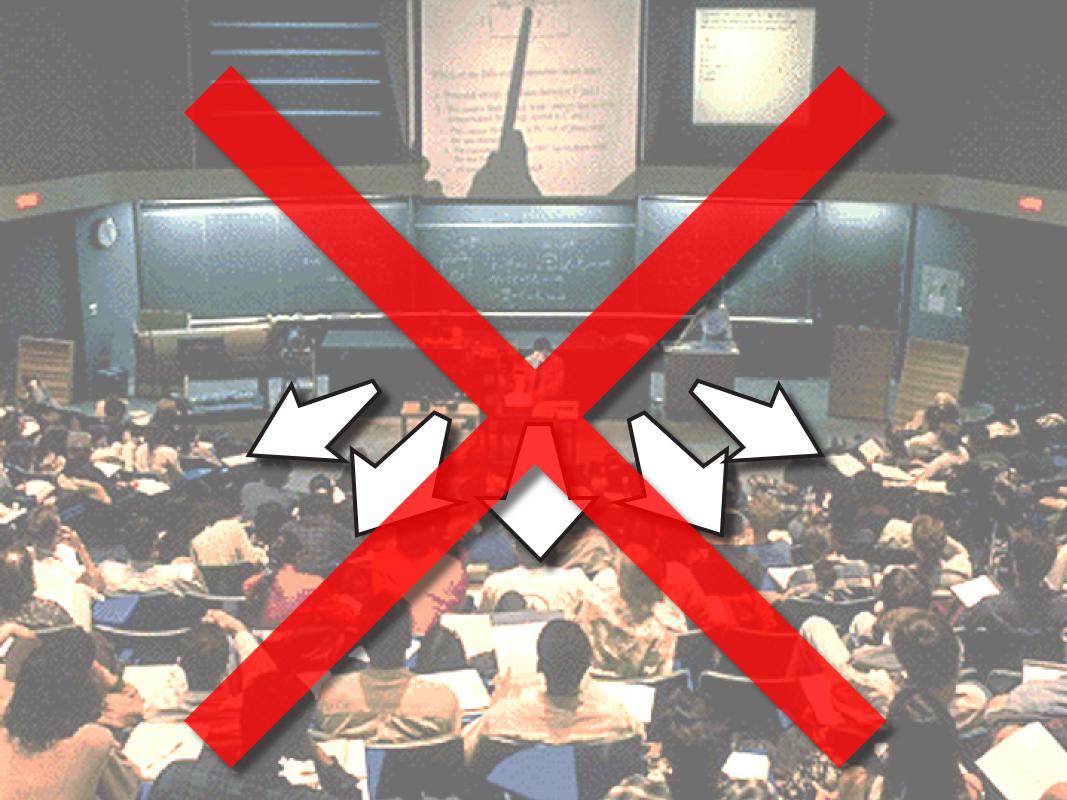














### how to effectively transfer information outside classroom?





transfer pace set by video

• viewer passive

viewing/attention tanks as time passes

isolated/individual experience



# we're simply moving this outside classroom!



### transfer pace set by reader

• viewer active



isolated/individual experience & no real accountability

### want:

# every student prepared for every class

### want:

# every student prepared for every class

(without additional instructor effort)

# Solution

# turn out-of-class component

# also into a social interaction!

# every student prepared for every class

The ideas of a second s

nathematical expression of this

I can also fold the flake in hal



tion symmetry, occurs when one hall of an object is the mirror image of the other half. The equilateral triangle in Figure 1.4 possesses reflection symmetry about the three shown in Figure 1.4b. If you imagine folding the trian-

ie same when you open your eyes, and you can't tell that studying must therefore mathematically exhibit symmetry it has been rotated. The triangle is said to have rotational under translation in time; in other words, the mathematical

be split in two so that one half is the mirror image of the

Exercise 1.3 Change is no change

1.2 SYMMETRY 5

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#### 76

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Figure 4.2 Low-friction track and carts used in the experiments described



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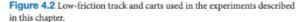
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CEPTS

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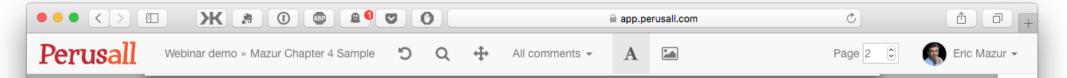


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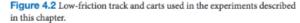
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highlighting

ice

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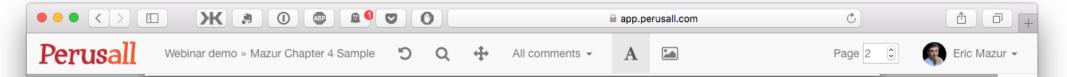


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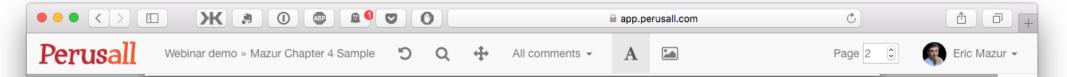
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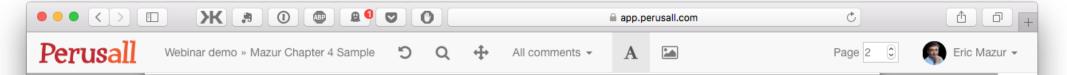
No friction at all seems impossible. Isn't there always some friction in any real case.

You may wonder whether it is possible to make surfaces that have no friction at all, such that an object, once given a shove, continues to glide forever. There is no totally frictionless surface over which objects slide forever, but there are ways to minimize friction. You can, for instance, float an object on a cushion of air. This is most easily accomplished with a low-friction track-a track whose surface is dotted with little holes through which pressurized air blows. The air serves as a cushion on which a conveniently shaped object can float, with friction between the object and the track all but eliminated. Alternatively, one can use wheeled carts with low-friction bearings on an ordinary track. Figure 4.2 shows low-friction carts you may have encountered in your lab or class. Although there is still some friction both for low-friction tracks and for the track shown in Figure 4.2, this friction is so small that it can be ignored during an experiment. For example, if the track in Figure 4.2 is horizontal, carts move along its length without slowing down appreciably. In other words:

### In the absence of friction, objects moving along a horizontal track keep moving without slowing down.

Another advantage of using such carts is that the track constrains the motion to being along a straight line. We can then use a high-speed camera to record the cart's position at various instants, and from that information determine its speed and acceleration.

**4.1** (*a*) Are the accelerations of the motions shown in Figure 4.1 constant? (*b*) For which surface is the acceleration largest in magnitude?



### 76 CHAPTER 4 MOMENTUM

In the preceding two chapters, we developed a mathematical framework for describing motion along a straight line. In this chapter, we continue our study of motion by investigating inertia, a property of objects that affects their motion. The experiments we carry out in studying inertia lead us to discover one of the most fundamental laws in physics—conservation of momentum. Figure 4.2 Low-friction track and carts used in the experiments described in this chapter.



### 4.1 Friction

Picture a block of wood sitting motionless on a smooth wooden surface. If you give the block a shove, it slides some distance but eventually comes to rest. Depending on the smoothness of the block and the smoothness of the wooden surface, this stopping may happen sooner or it may happen later. If the two surfaces in contact are very smooth and slippery, the block slides for a longer time interval than if the surfaces are rough or sticky. This you know from everyday experience: A hockey puck slides easily on ice but not on a rough road.

**Figure 4.1** shows how the velocity of a wooden block decreases on three different surfaces. The slowing down is due to *friction*—the resistance to motion that one surface or object encounters when moving over another. Notice that, during the interval covered by the velocity-versus-time graph, the velocity decrease as the block slides over ice is hardly observable. The block slides easily over ice because there is very little friction between the two surfaces. The effect of friction is to bring two objects to rest with respect to each other—in this case the wooden block and the surface it is sliding on. The less friction there is, the longer it takes for the block to come to rest

No friction at all seems impossible. Isn't there always some friction in any real case.



Enter your comment or question and press Enter

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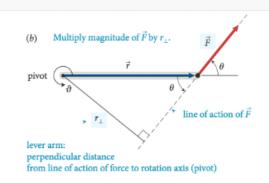
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action of the force and the axis of rotation. So, the torque caused by a force exerted on an object is the product of the magnitude of the force and its lever arm distance. It can be written equivalently as  $rF_{\perp}$  and as  $r_{\perp}F$ .

Like other rotational quantities, torque carries a sign that depends on the choice of direction for increasing  $\vartheta$ . In Figure 12.4, for example, the torque caused by  $\vec{F}_1$  about the pivot tends to rotate the rod in the direction of increasing  $\vartheta$  and so is positive; the torque caused by  $\vec{F}_2$  is negative. The sum of the two torques about the pivot is then  $r_1F_1 + (-r_2F_2)$ . As we've seen, the two torques are equal in magnitude when the rod is balanced, and so the sum of the torques is zero. When the sum of the torques is not zero, the rod's rotational acceleration is nonzero, and so its rotational velocity and angular momentum change.

In the situations depicted in Figures 12.4 and 12.5 we used the pivot to calculate the lever arm distances. This is a natural choice because that is the point about which the object under consideration is free to rotate. However, torques also play a role for stationary objects that are suspended or supported at several different points and that are not free to rotate—for example, a plank or bridge supported at either end. To determine what reference point to use in such cases, complete the following exercise.

### Exercise 12.1 Reference point

Consider again the rod in Figure 12.4. Calculate the sum of the torques about the left end of the rod.

**SOLUTION** I begin by making a sketch of the rod and the three forces exerted on it, showing their points of application on the rod (Figure 12.6).

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Group 1's comments -

The lever arm distances must now be determined relative to the left end of the rod. The lever arm distance of force  $\vec{F}_1$  to this point is zero, and so the torque caused by that force about the left end of the rod is zero. If I choose counterclockwise as the positive direction of rotation,  $\vec{F}_2$  causes a negative torque about the left end of the rod; the force  $\vec{F}_{pr}^c$  exerted by the pivot causes a positive torque about the left end of the rod. The lever arm distance of  $\vec{F}_2$  about the left end of the rod is  $r_1 + r_2$ ; that of  $\vec{F}_{pr}^c$  is  $r_1$ . Because the rod is at rest, the magnitude of the force exerted by the pivot is equal to the sum of the forces  $\vec{F}_1$ and  $\vec{F}_2$ . Taking into account the signs of the torques, we find that the sum of the torques about the left end of the rod is  $r_1(F_1 + F_2) - (r_1 + r_2)F_2 = r_1F_1 - r_2F_2$ . This is the same result we obtained for the torques about the pivot, and so the sum of the torques about the left end is zero.

Exercise 12.1 shows that the sum of the torques about the left end of the rod is zero, just like the sum of the torques about the pivot. You can repeat the calculation for the torques about the right end of the rod or any other point, and each time you will find that the sum of the torques is zero. The reason is that the rod is not rotating about any point, and so the sum of the torques must be zero about any point. In general we can say:

### For a stationary object, the sum of the torques is zero.

For a stationary object we can choose any reference point we like to calculate torques. It pays to choose a reference point that simplifies the calculation. As you have seen, we do not need to consider any force that is exerted at the reference point. So, by putting the reference point at the point of application of a force, we can eliminate that force from the calculation.

**12.2** In the situation depicted in Figure 12.2*a*, you must continue to exert a force on the seesaw to keep the child off the ground. The force you exert causes a torque on the seesaw, and yet the seesaw's rotational acceleration is zero. How can this be if torques cause objects to accelerate rotationally?

### Example 12.2 Torques on lever

Three forces are exerted on the lever of **Figure 12.7**. Forces  $\vec{F}_1$  and  $\vec{F}_3$  are equal in magnitude, and the magnitude of  $\vec{F}_2$  is half as great. Force  $\vec{F}_1$  is horizontal,  $\vec{F}_2$  and  $\vec{F}_3$  are vertical, and the lever makes an angle of 45° with the horizontal. Do these forces cause the lever to rotate about the pivot? If so, in which direction?

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Group 1's comments -

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Multiply magnitude of  $\vec{F}$  by  $r_{\perp}$ line of action of  $\vec{F}$ lever arm: perpendicular distance from line of action of force to rotation axis (pivot)

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Enter your comment or question and press Enter

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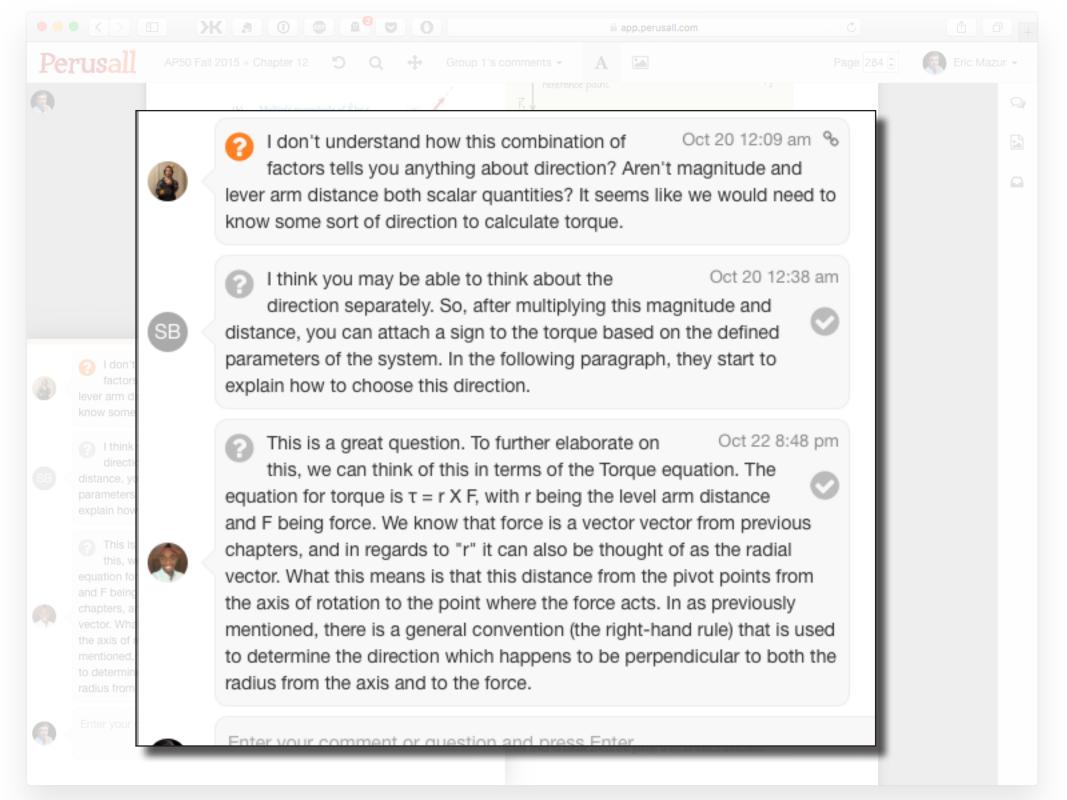
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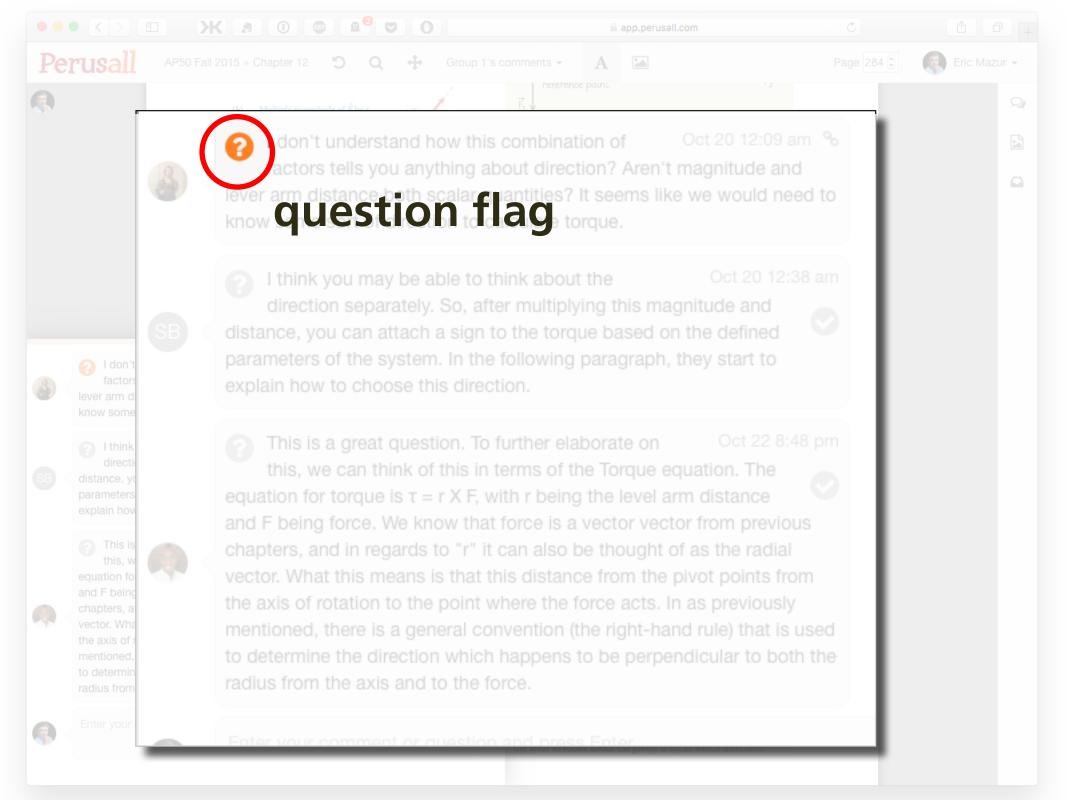
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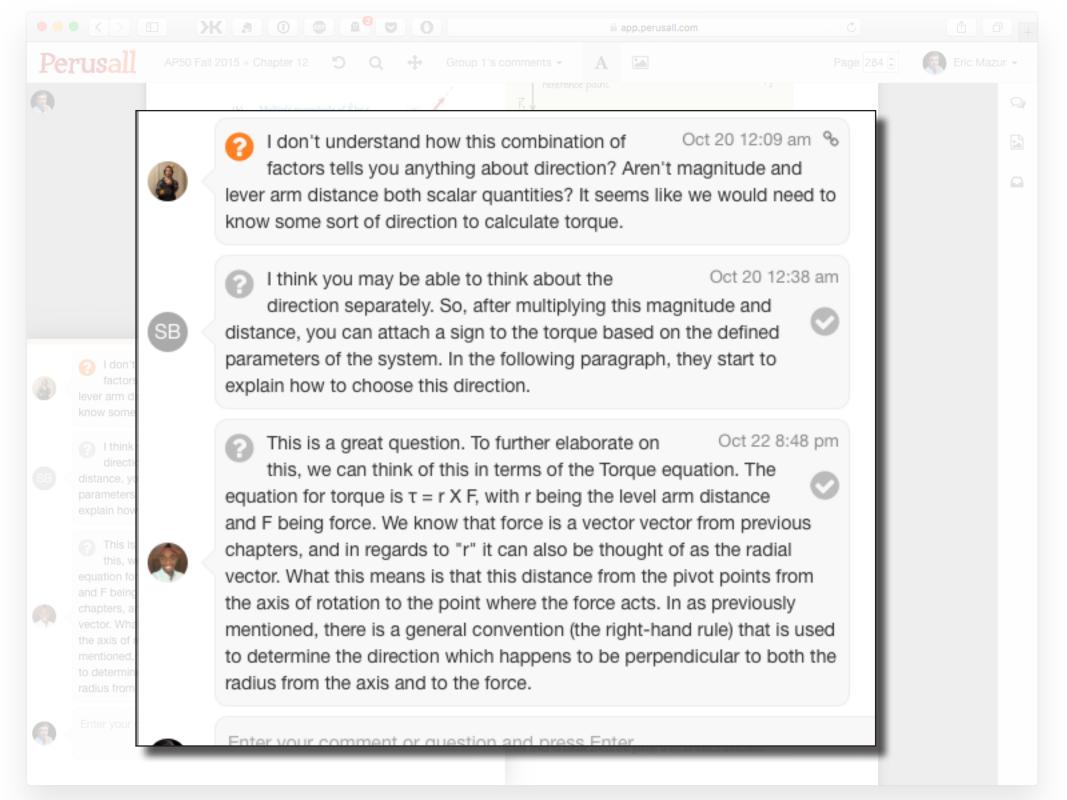
### Example 12.2 Torques on lever

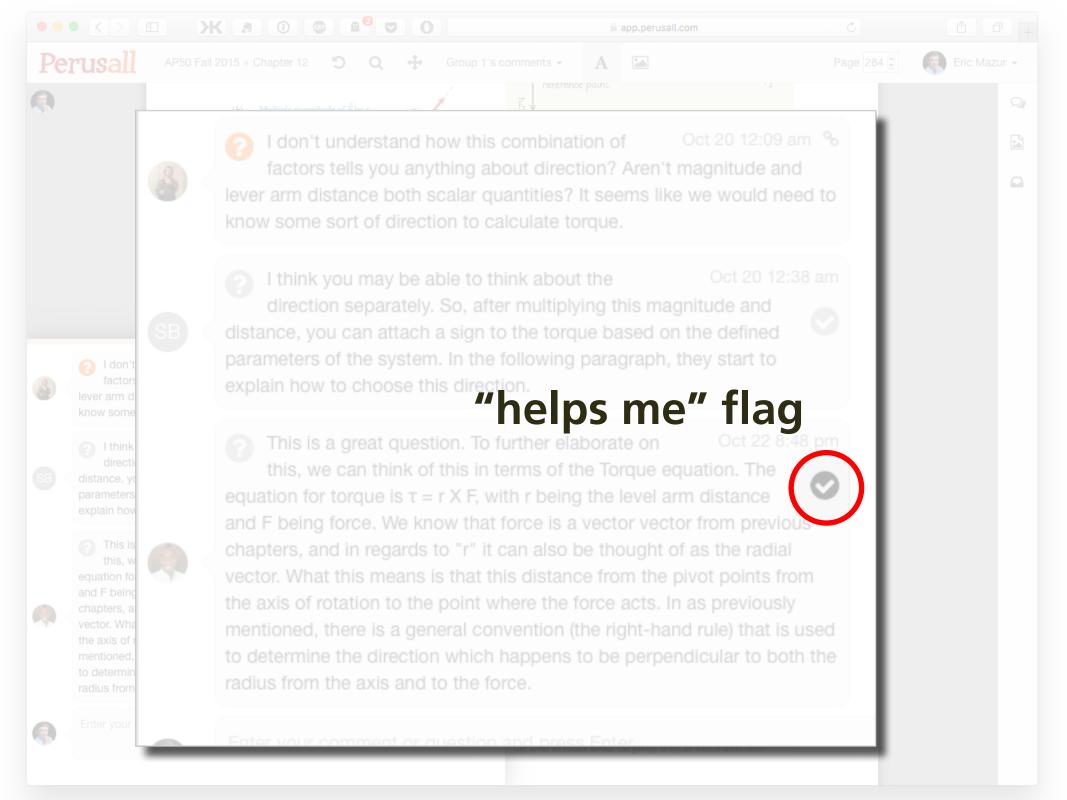
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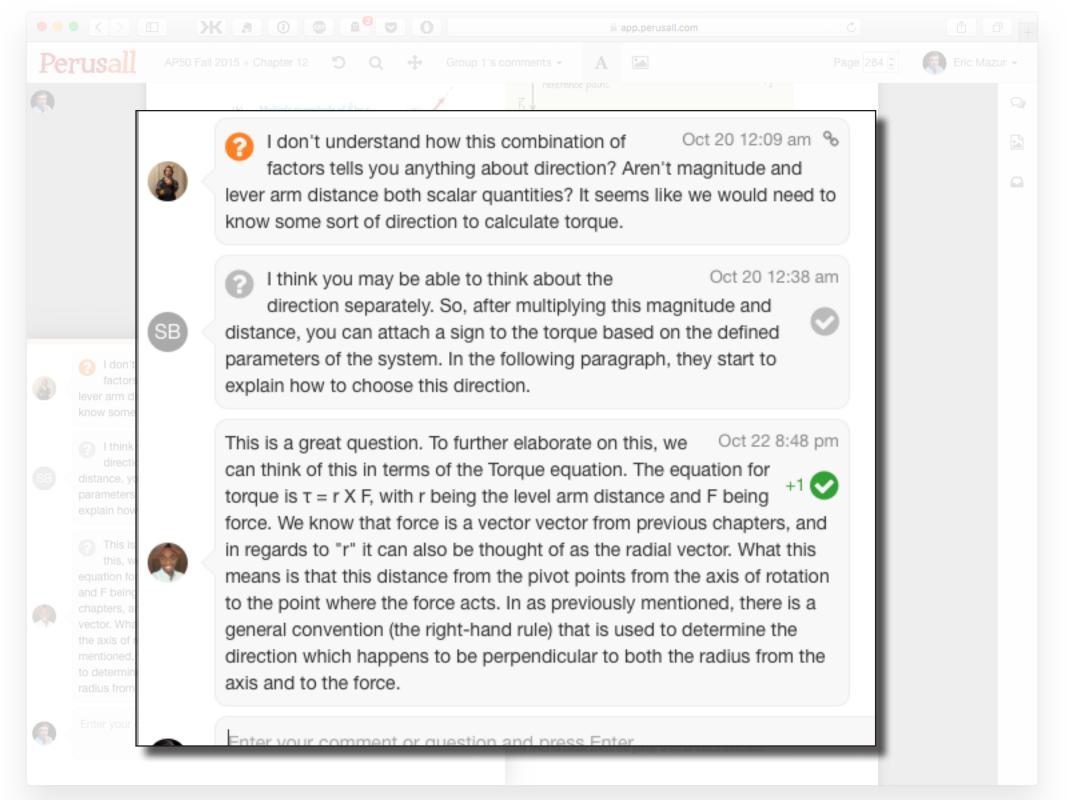












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Group 1's comments -

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Multiply magnitude of  $\vec{F}$  by  $r_{\perp}$ line of action of  $\vec{F}$ lever arm: perpendicular distance from line of action of force to rotation axis (pivot)

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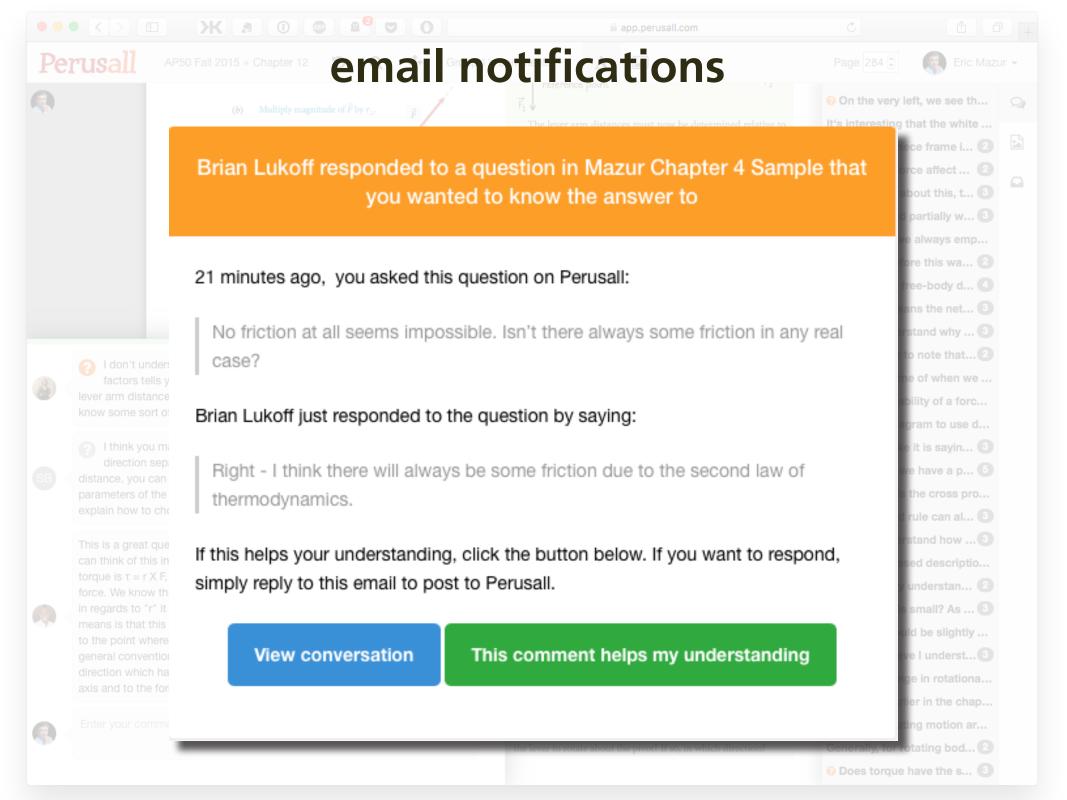
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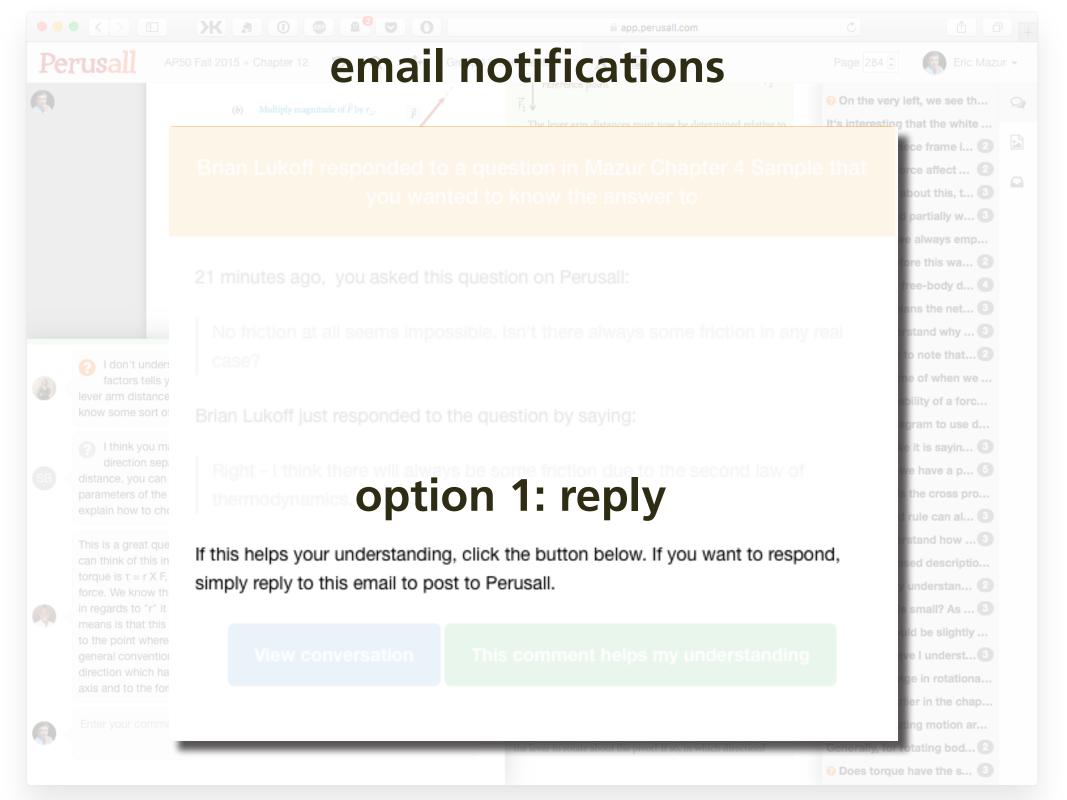
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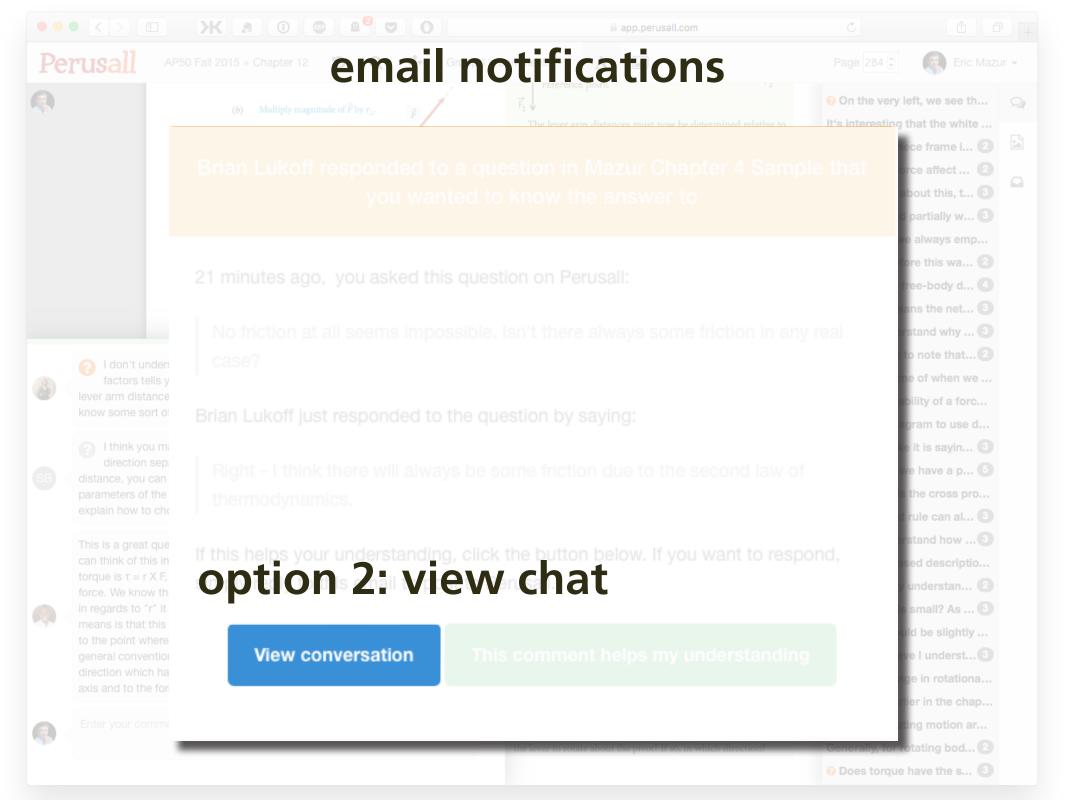
### Example 12.2 Torques on lever

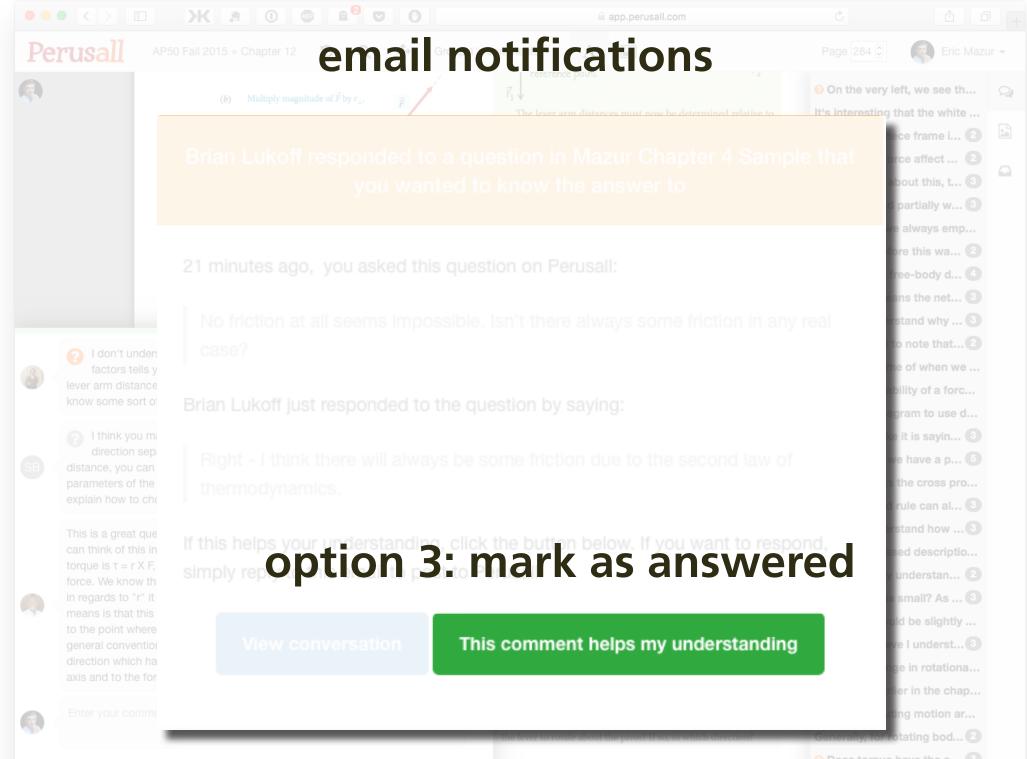
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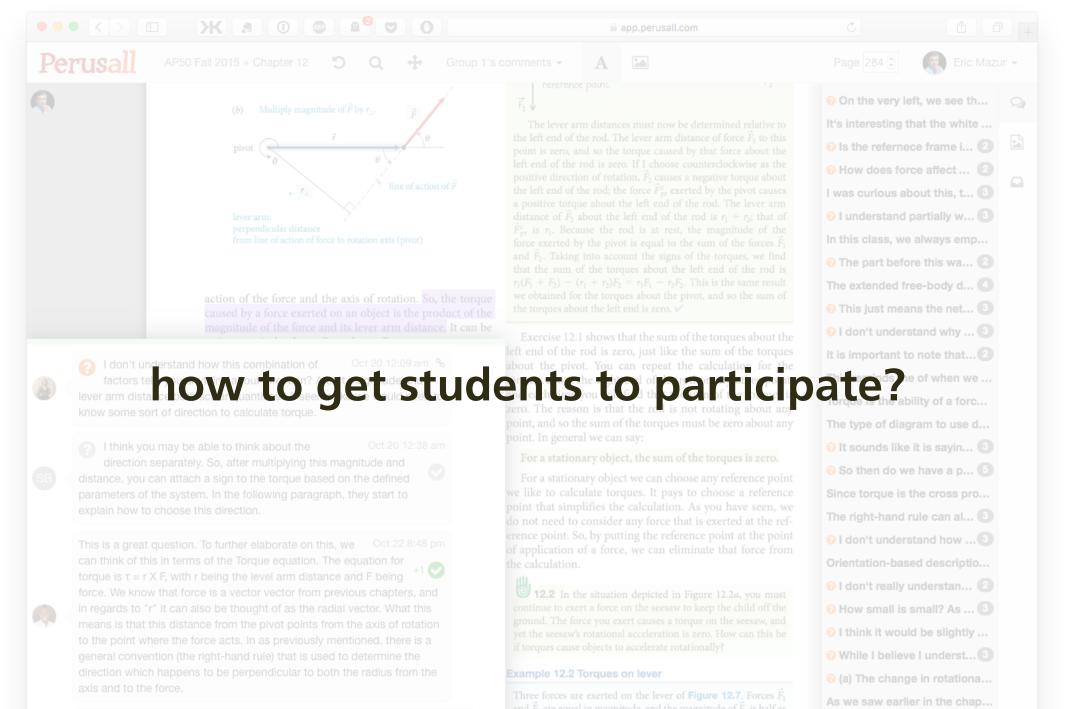








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Eric Mazur 🗸

(b) Multiply magnitude of  $\vec{F}$  by  $r_{\perp}$ .  $\vec{F}$ pivot  $\vec{r}$   $\theta$   $\theta$   $\theta$ line of action of  $\vec{F}$ lever arm: perpendicular distance from line of action of force to rotation axis (pivot)

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## rubric-based assessment

## (b) Multiply magnitude of $\vec{F}$ by $r_{\perp}$ .

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## Perusal

## rubric-based assessment

## (b) Multiply magnitude of $\vec{F}$ by $r_{\perp}$ .

L line of action of F

lever arm: perpendicular distance from line of action of force to rotation axis (pive

## quality (thoughtful reading & interpretation)

action of the force and the axis of rotation. So, the torqu caused by a force exerted on an object is the product of th magnitude of the force and its lever arm distance. It can b

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 $r_1(F_1 + F_2) - (r_1 + r_2)r_2 = r_1F_1 - r_2F_2$ . This is the same result we obtained for the torques about the pivot, and so the sum of the torques about the left end is zero.  $\checkmark$ 

Exercise 12.1 shows that the sum of the torques about the left to the rod is zero, just like the sum of the torques about the right end of the rod or any other point, and each time you will find that the sum of the torques is zero. The reason is that the rod is not rotating about any point, and so the sum of the torques must be zero about any point. In general we can say:

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**12.2** In the situation depicted in Figure 12.2*a*, you must continue to exert a force on the seesaw to keep the child off the ground. The force you exert causes a torque on the seesaw, and yet the seesaw's rotational acceleration is zero. How can this be if torques cause objects to accelerate rotationally?

### Example 12.2 Torques on level

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## rubric-based assessment

## quality (thoughtful

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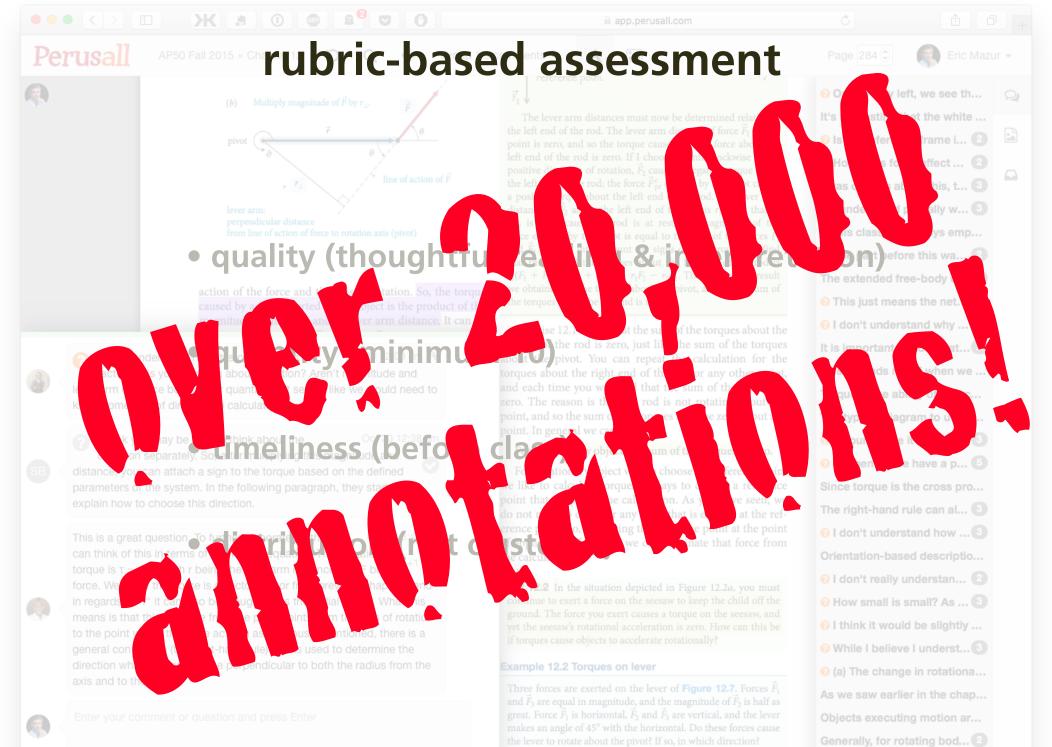
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## quality (thoughtfu

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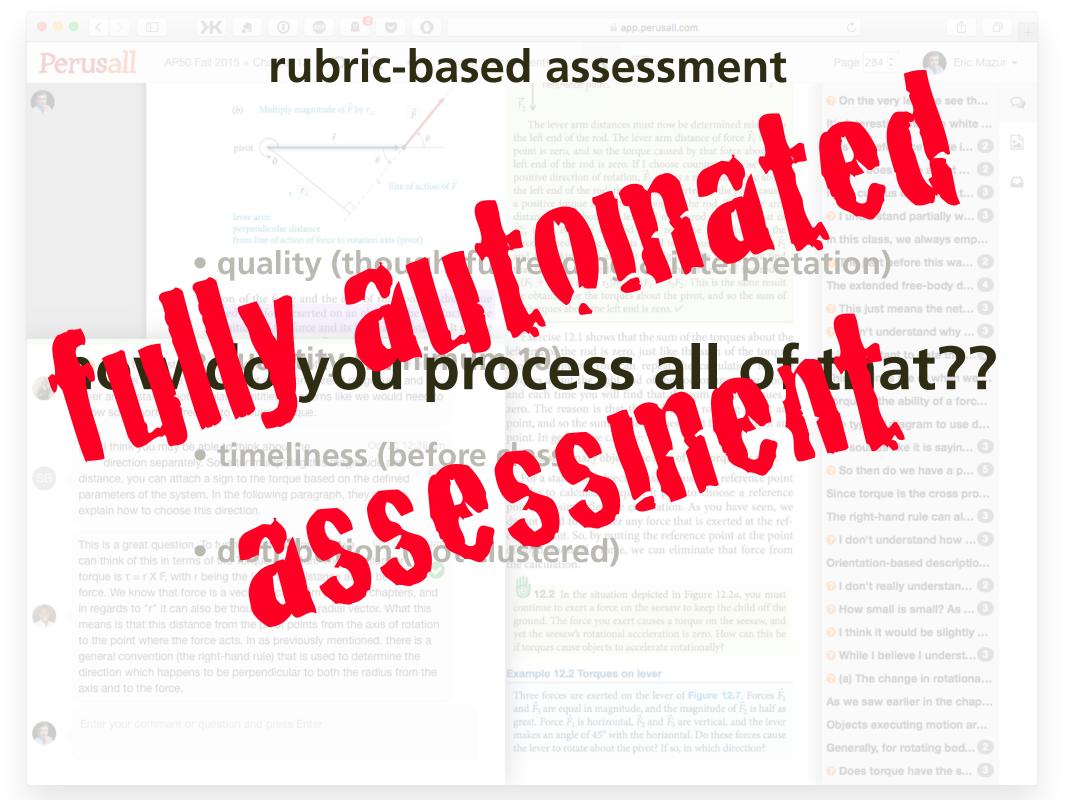
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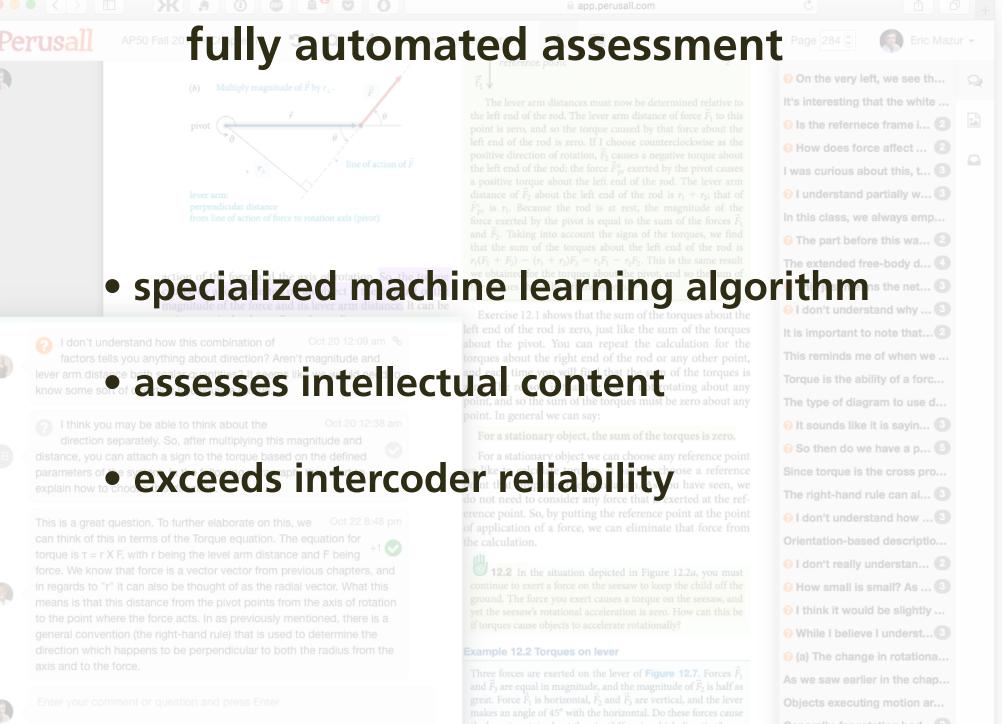
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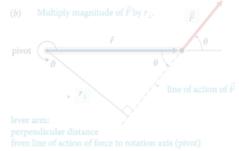




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# Perusall AP50 Fall 2015 » Chapter 12 Q Group 1's comments ~ A



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connect pre-class and in-class activities

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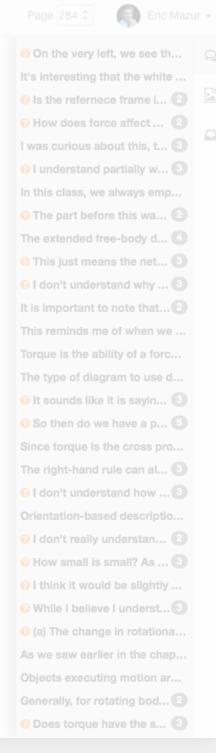
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		right h	and rule (11 questions)		does forc	e affect ( out this, t (		
		JB	Can someone in simpler terms explain the right- hand rule?	16		artially w (		
	•	WJ	Is there another way, besides the right hand rule, to find the direction of the magnetic field with a current?	ß		always emp. e this wa ( e-body d (		
		SB	Using the right hand rule, I believe the answer is D. Is that correct? Show more		just mean	s the net ( and why (		
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3	factors tells you anyt lever arm distance both so know some sort of directle	СР	Why is it that the magnet field points away from the north pole and towards the south pole? When on the previous page it stated that the direction of the magnetic field is the direction that the north pole of a compass needle points.	2	is the abil	of when we ity of a forc. am to use d		
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	direction separately: distance, you can attach a parameters of the system explain how to choose thi	КН	So whichever way the north pole faces is the direction of the magnetic field but that doesn't always mean its pointing true north? Show more	1	orque is th ht-hand ru	have a p ( ne cross pro ile can al (	3	
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	means is that this distanc to the point where the ford general convention (the rig direction which happens t axis and to the force.	AK	Can someone explain why this type of bacteria knows what direction the earth's magnetic fields are facing?	ß		be slightly . I underst(		
		J	Does the circular loop of current have any similarities with the look of the earths magnetic field? They kind of look similar to me.	ß		in rotationa r in the chap		
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## motivating factors

## Intrinsic:

• social interaction at the sum of the torques about the left end of the rod is



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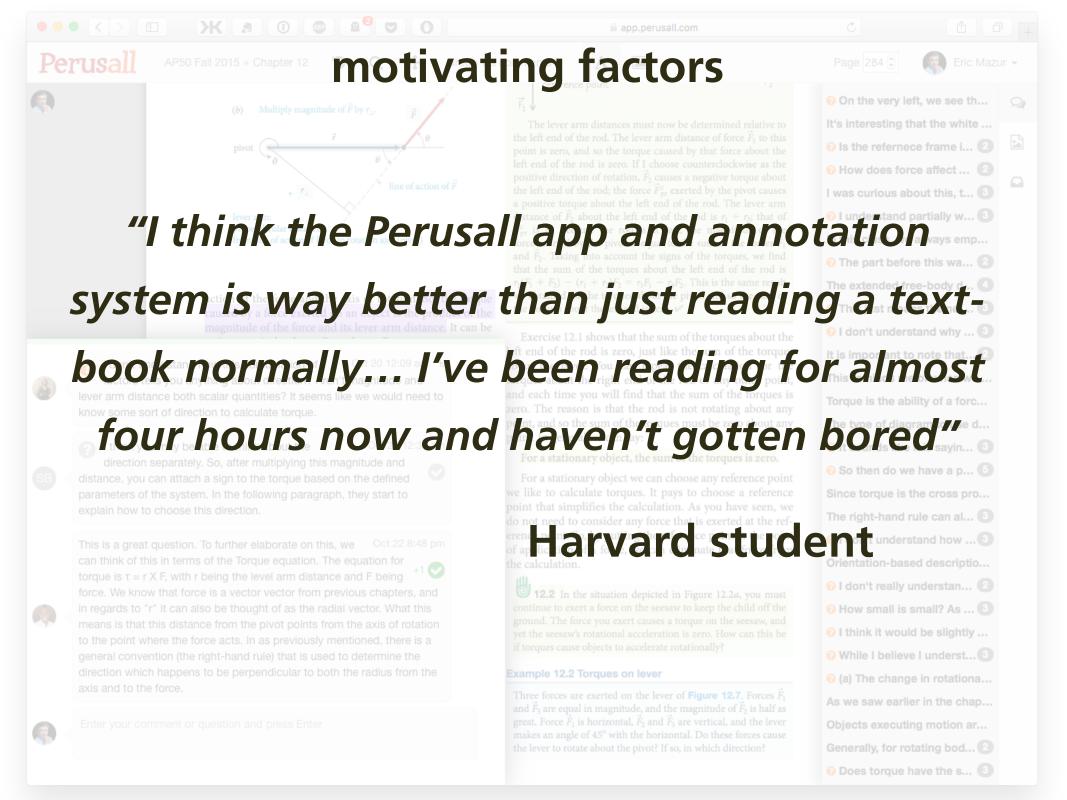
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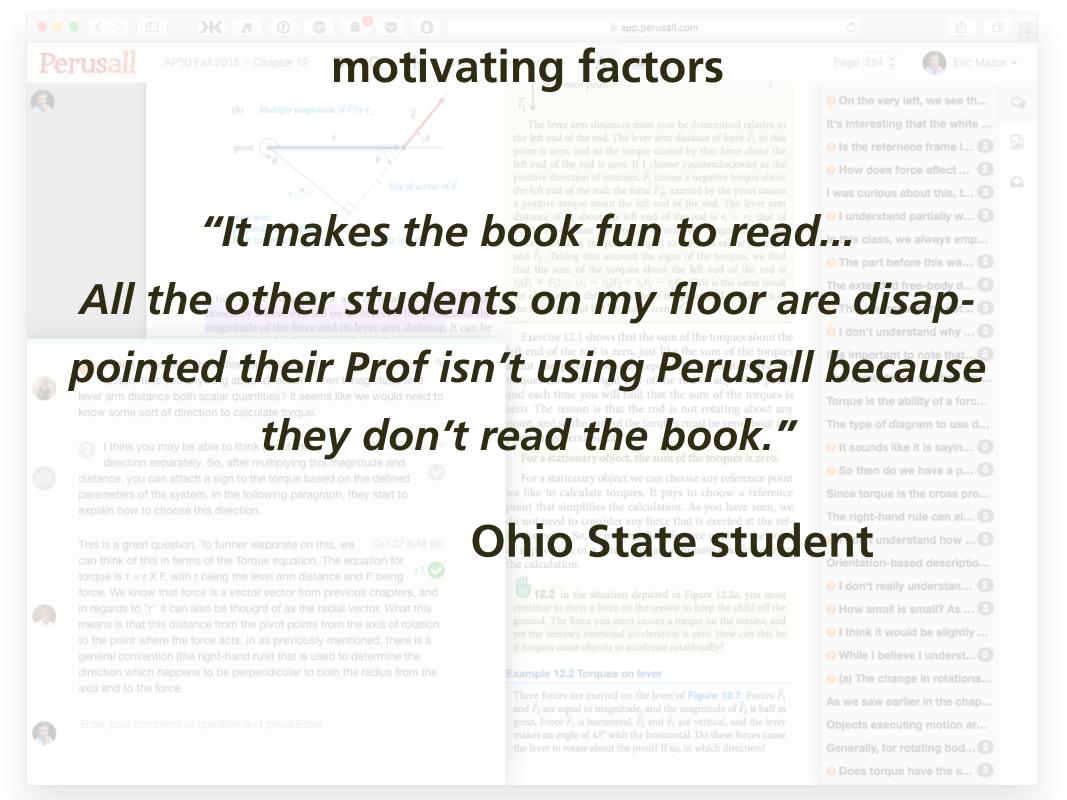
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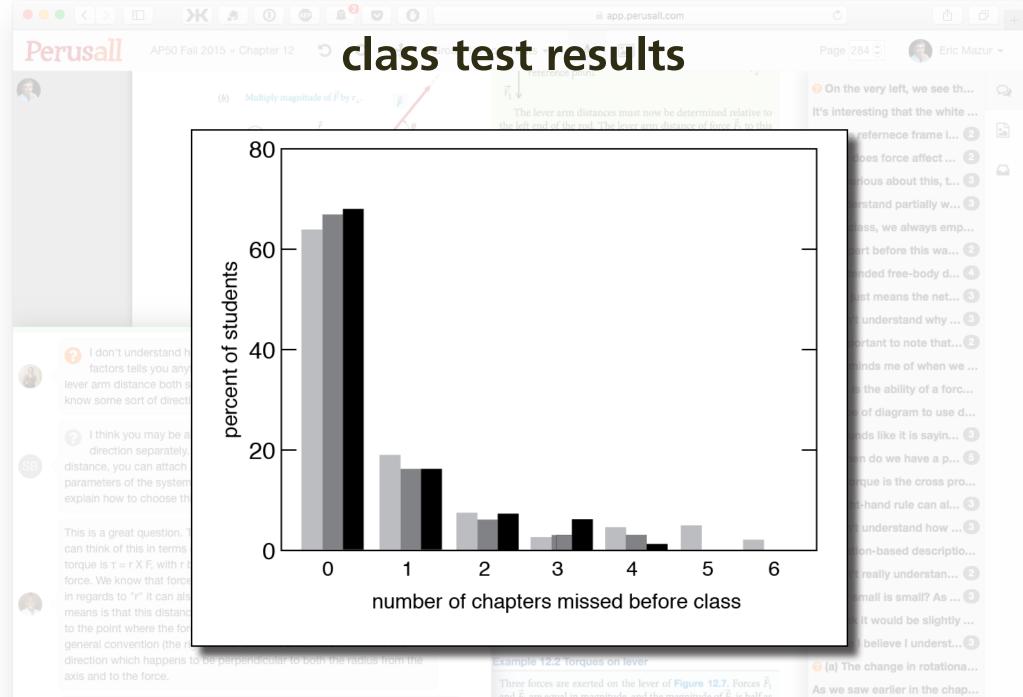
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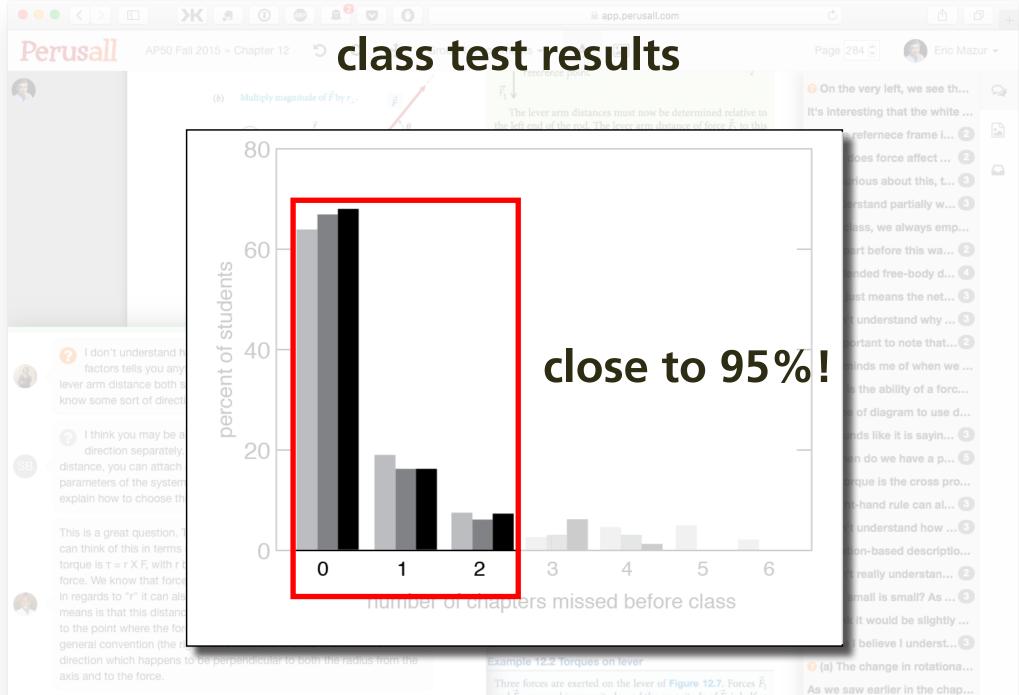




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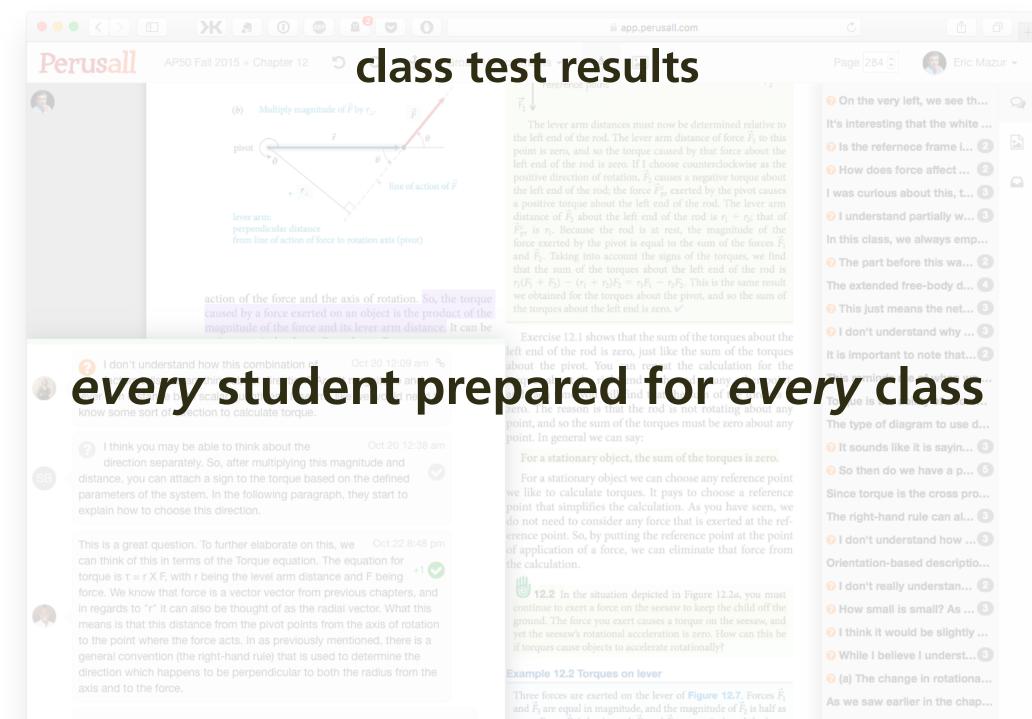
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## additional research data



perpendicular distance

## • Engagement:

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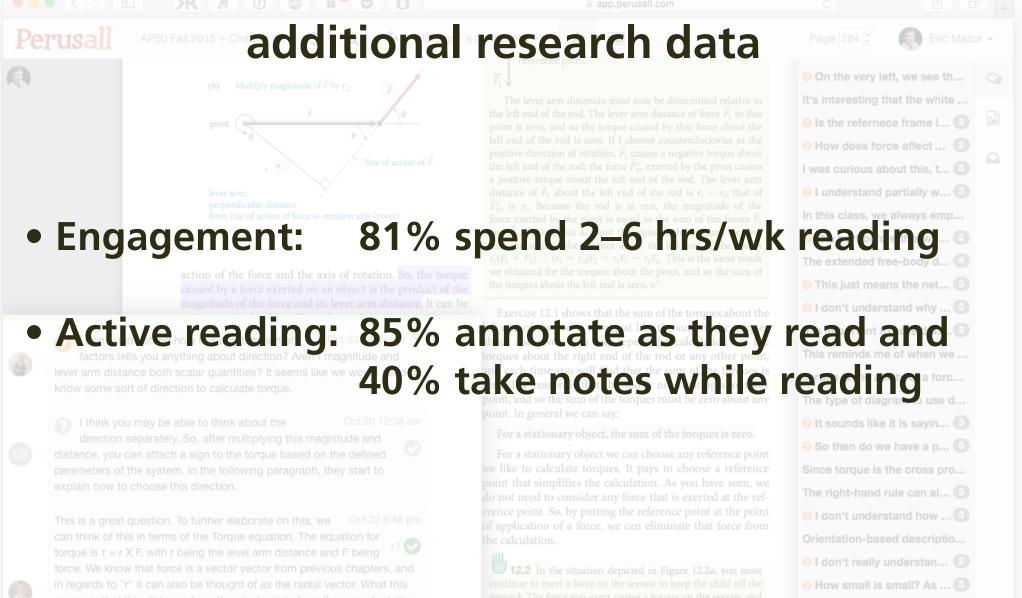
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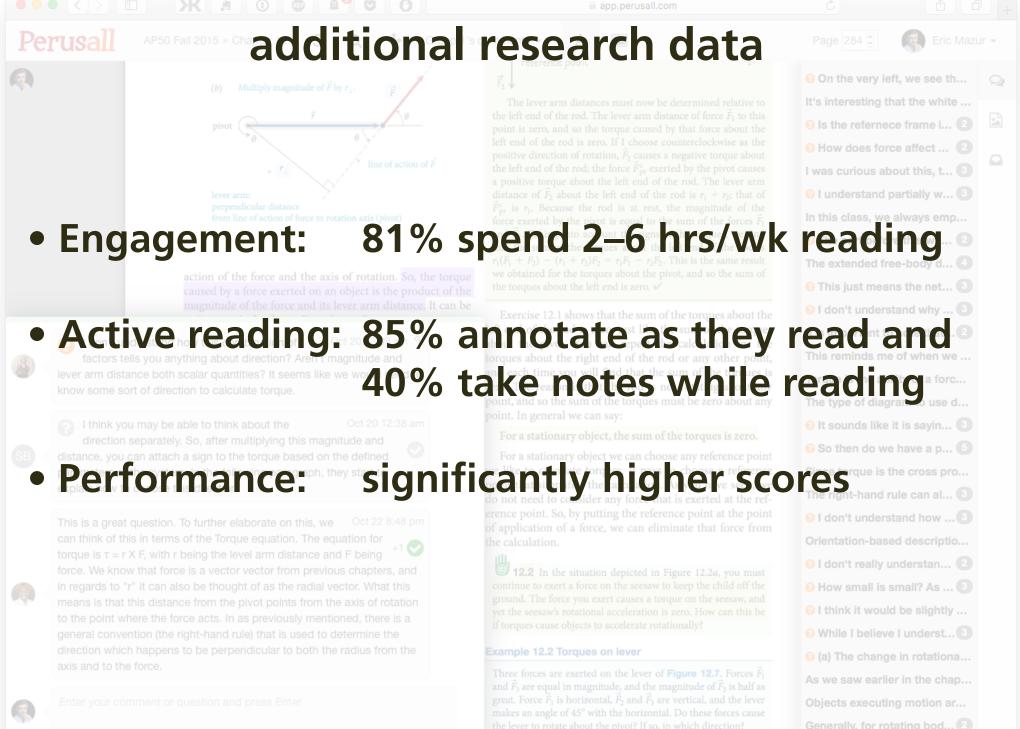
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## **Benefits**

## virtually 100% completion of assignments

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## all at no cost & without additional instructor effort!

**Education is not just about:** 

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