

# Less is more: Extreme optics with zero refractive index



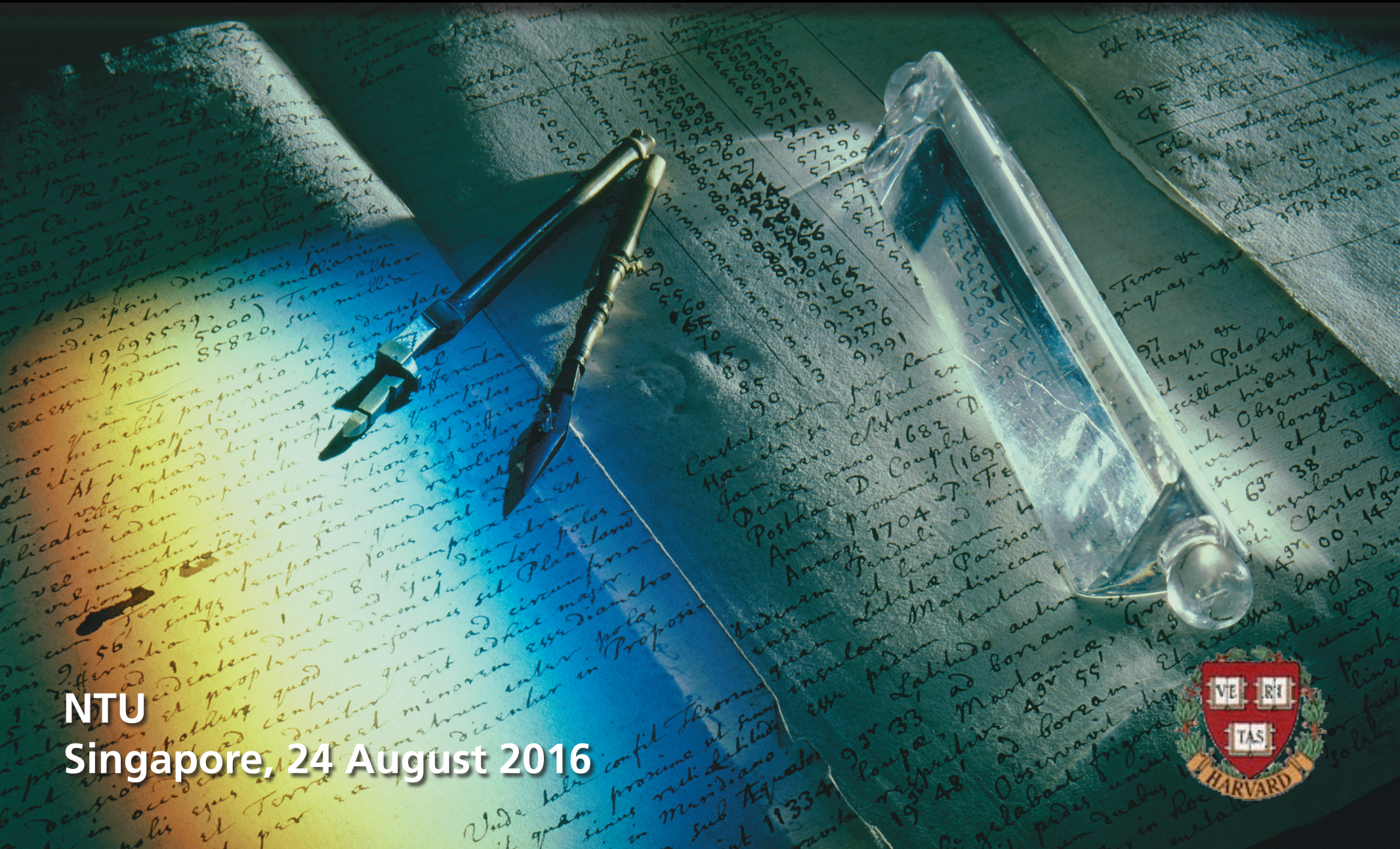
@eric\_mazur

NTU  
Singapore, 24 August 2016





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Singapore, 24 August 2016



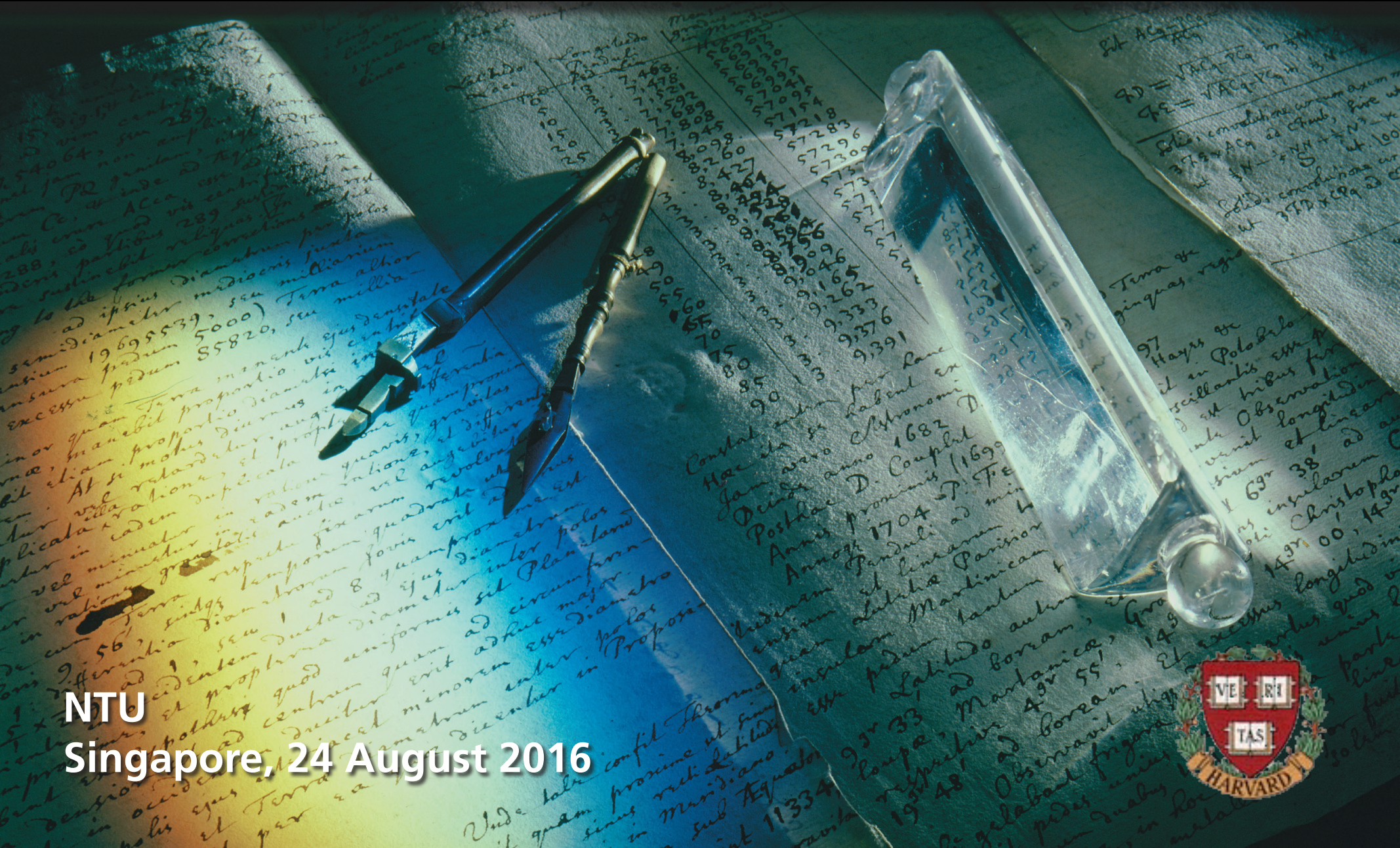


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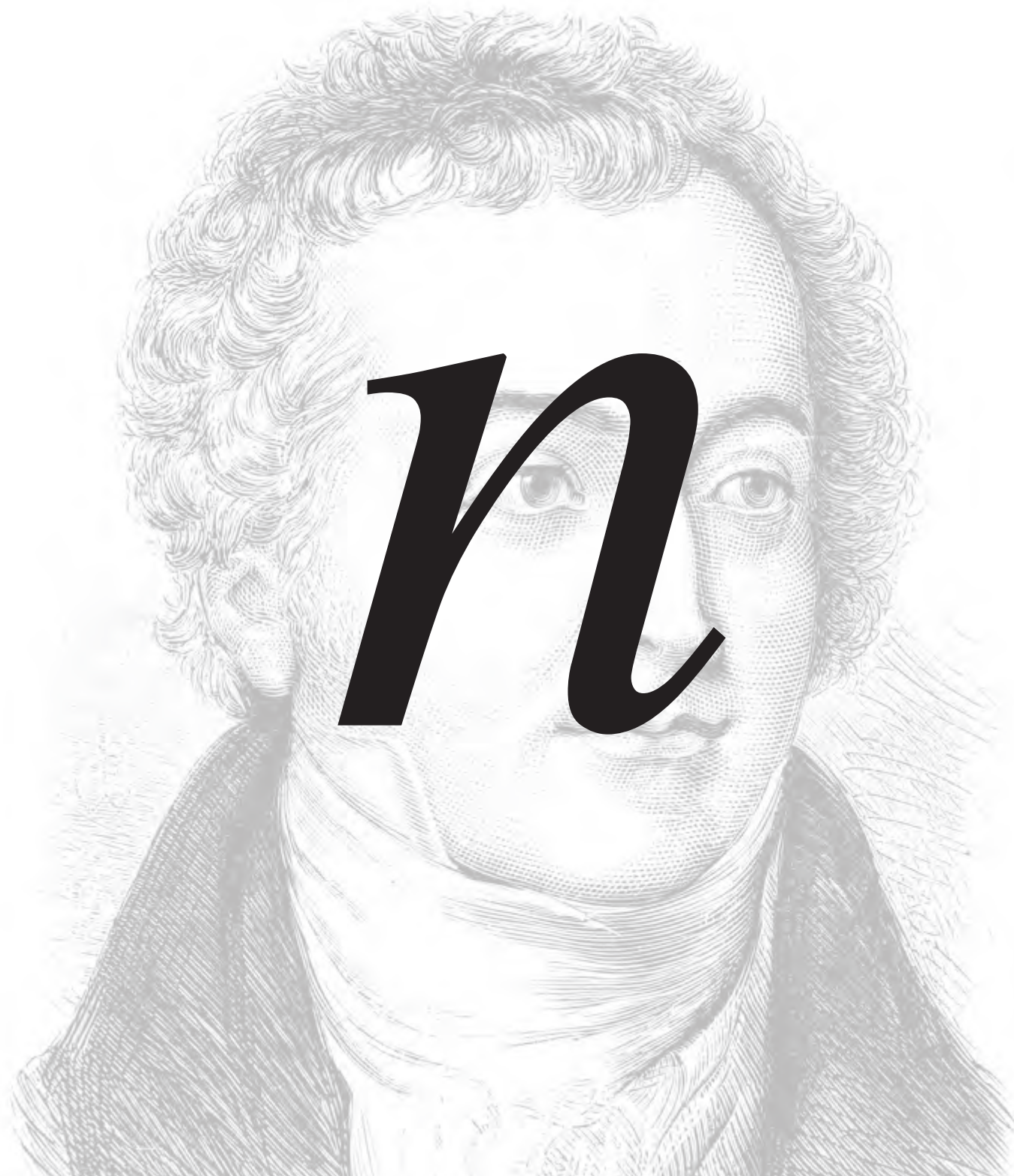
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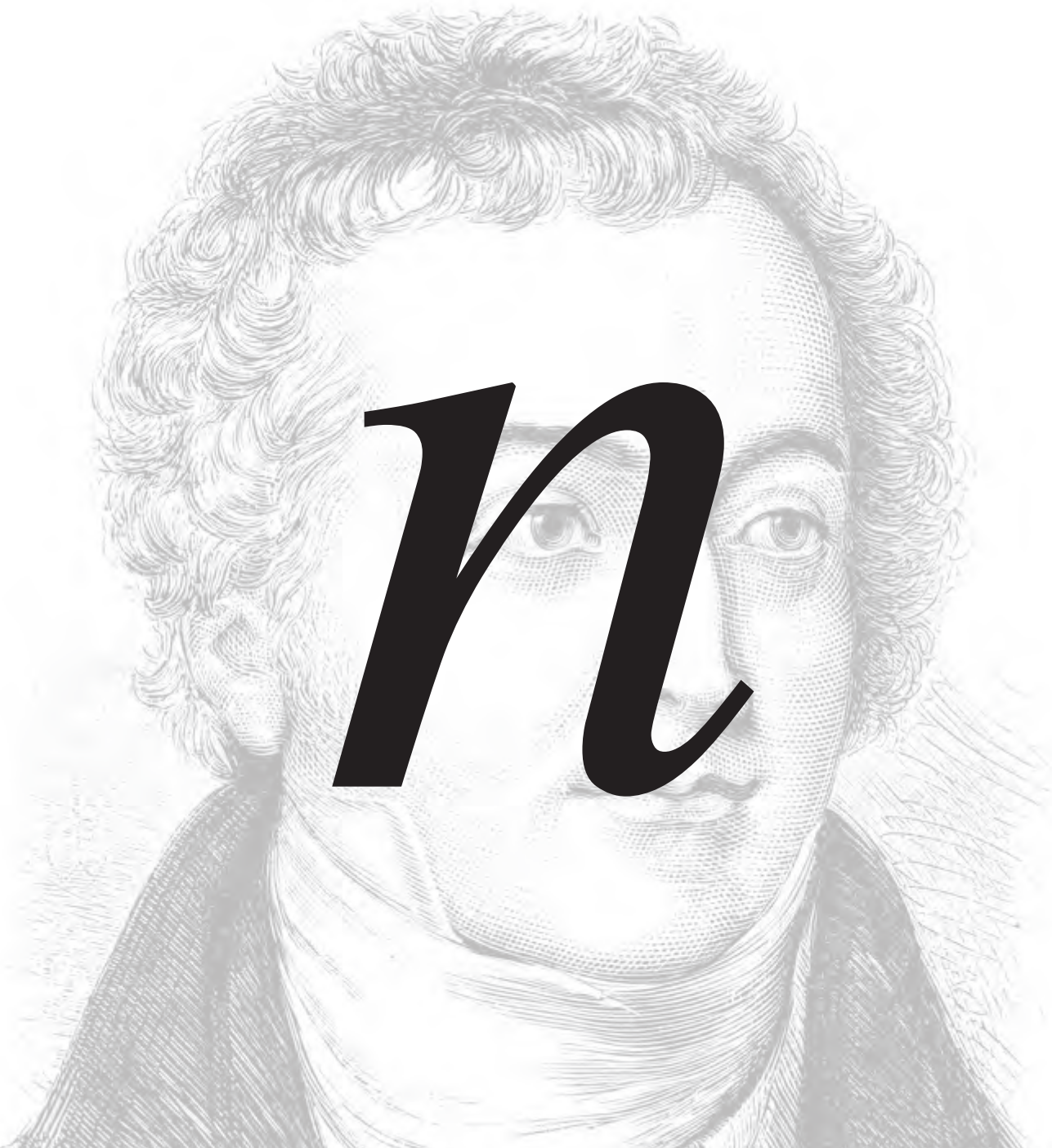




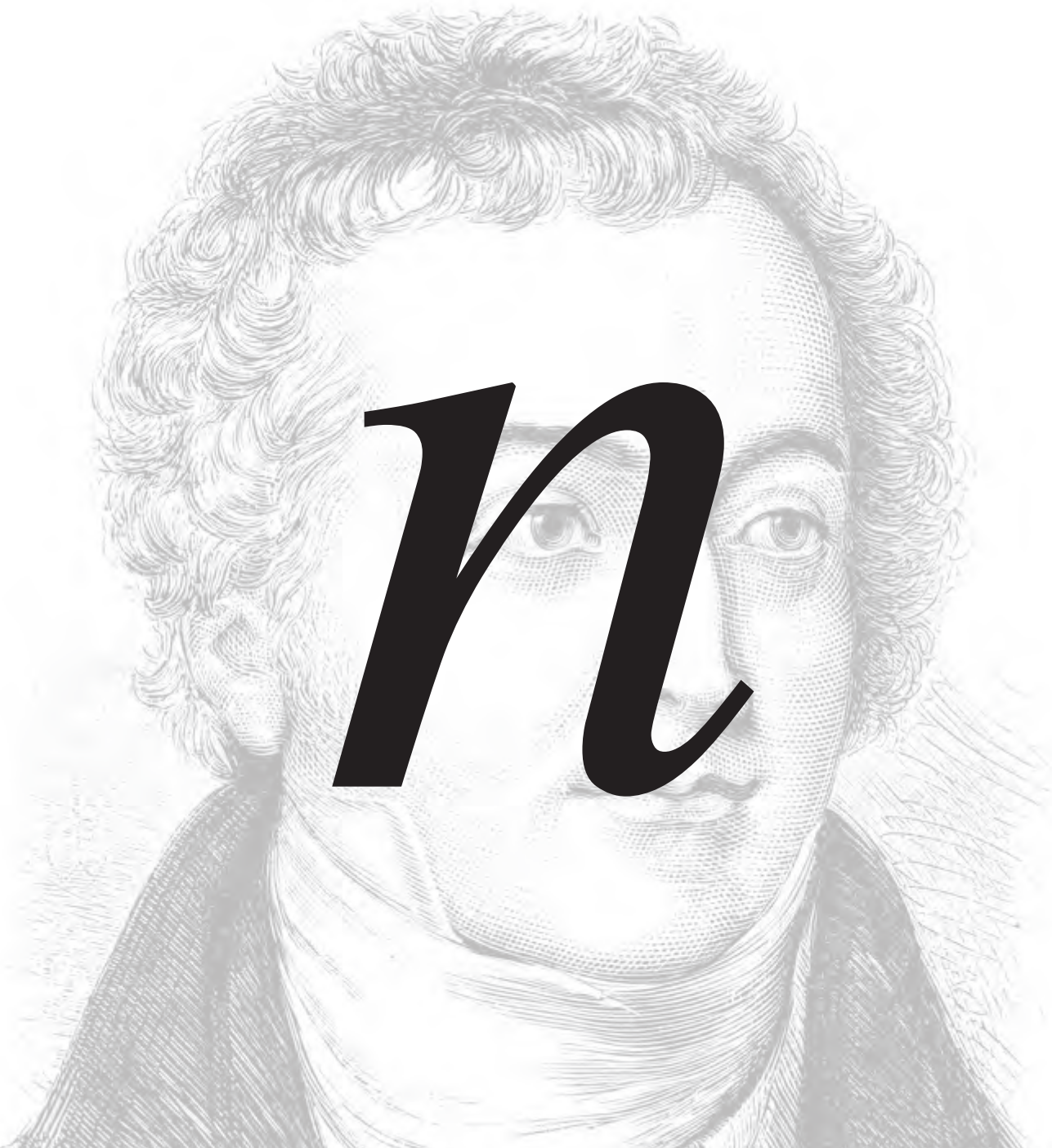








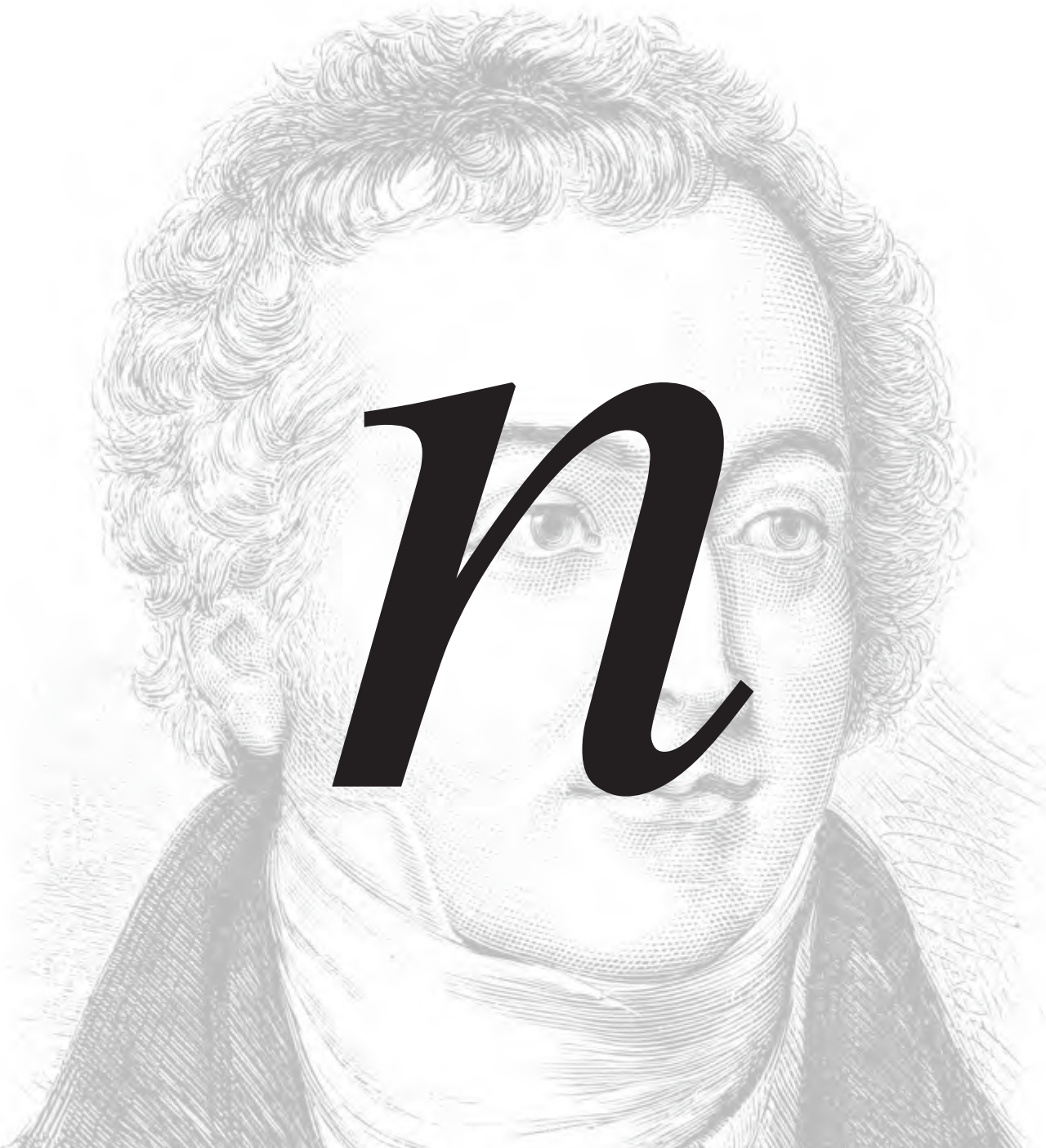




1 index

2 zero index





1 index

2 zero index

3 experiments



# Propagation of EM wave



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governed by wave equation

$$\nabla^2 \vec{E} - \frac{\mu\epsilon}{c^2} \frac{\partial^2 \vec{E}}{\partial t^2} = 0$$



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In dispersive media  $n = n(\omega)$  .

# Index of refraction

$$n = \sqrt{\epsilon\mu}$$



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**So  $n(\omega)$  determined by response of material to external fields**

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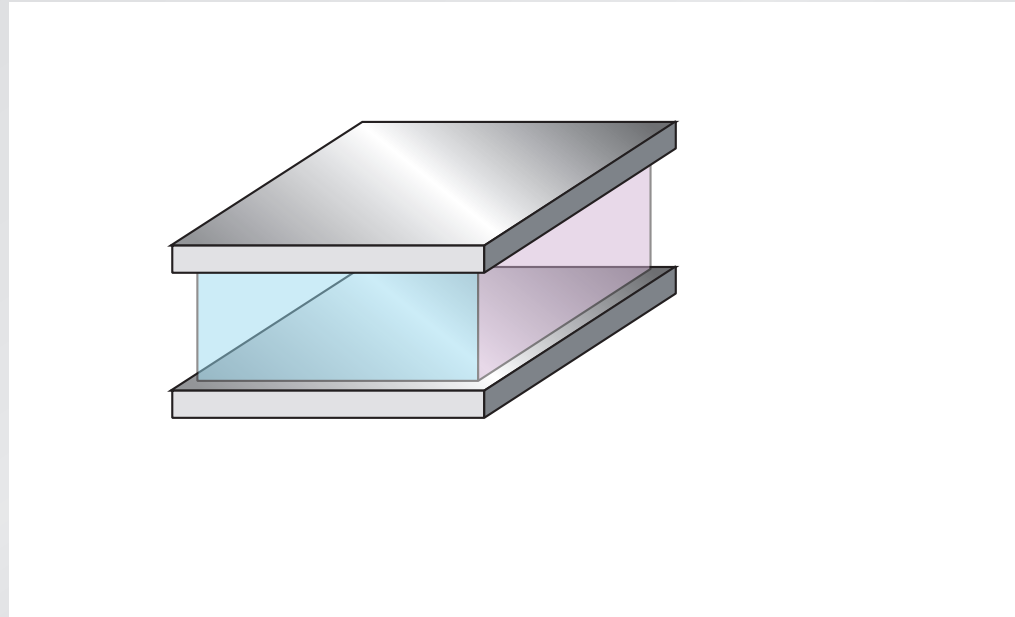
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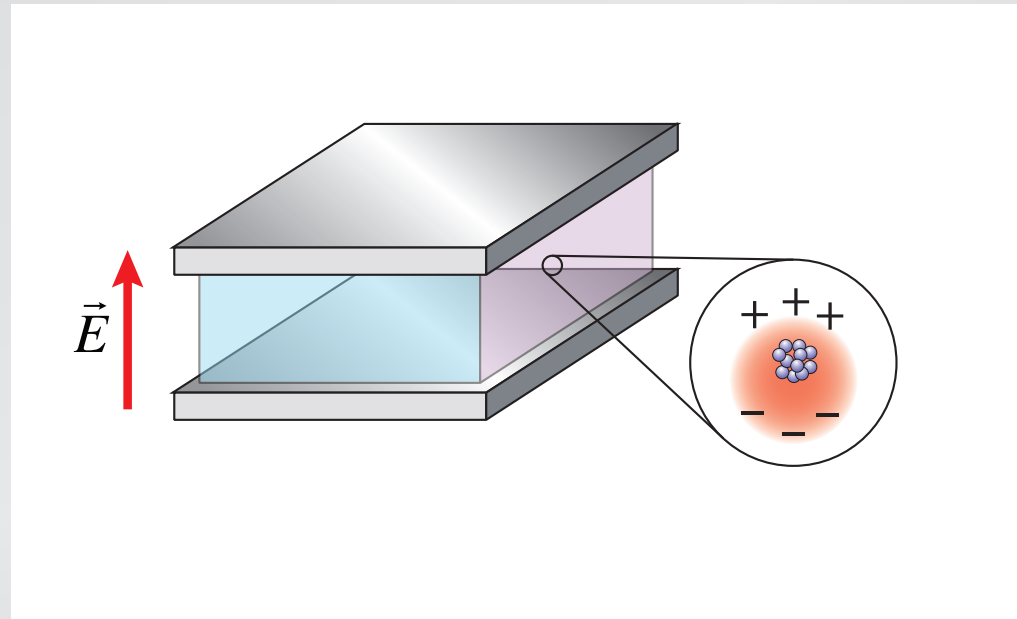
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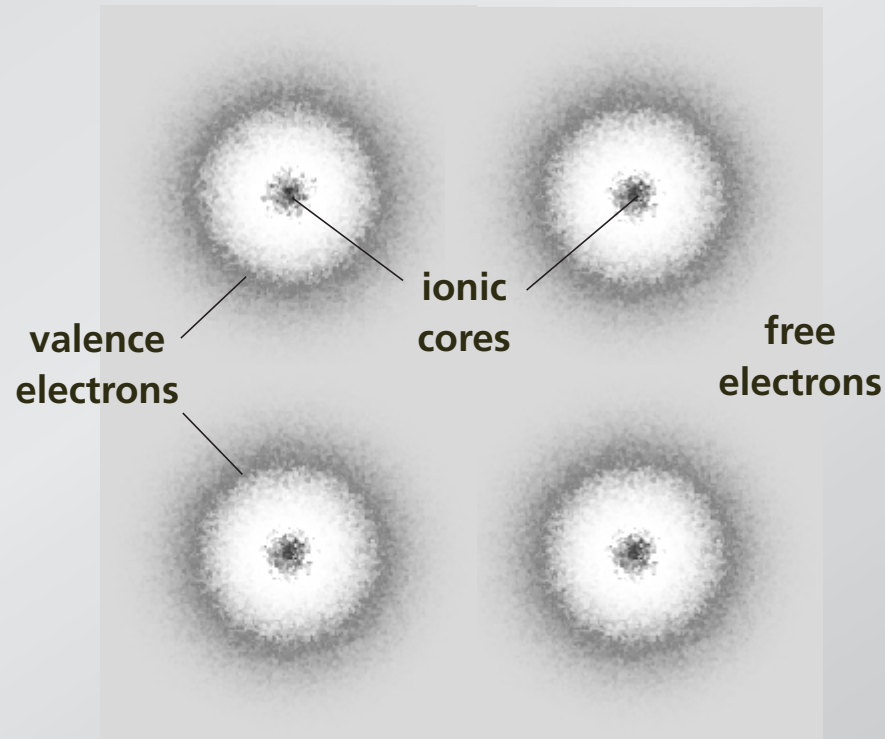
$\epsilon(\omega)$  measure of attenuation of electric field



# Index of refraction

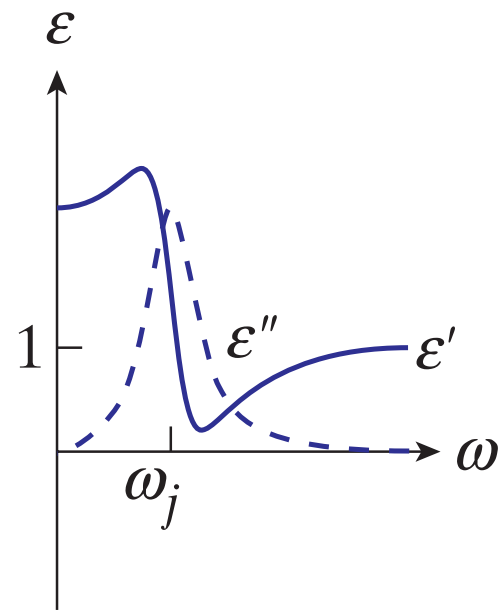
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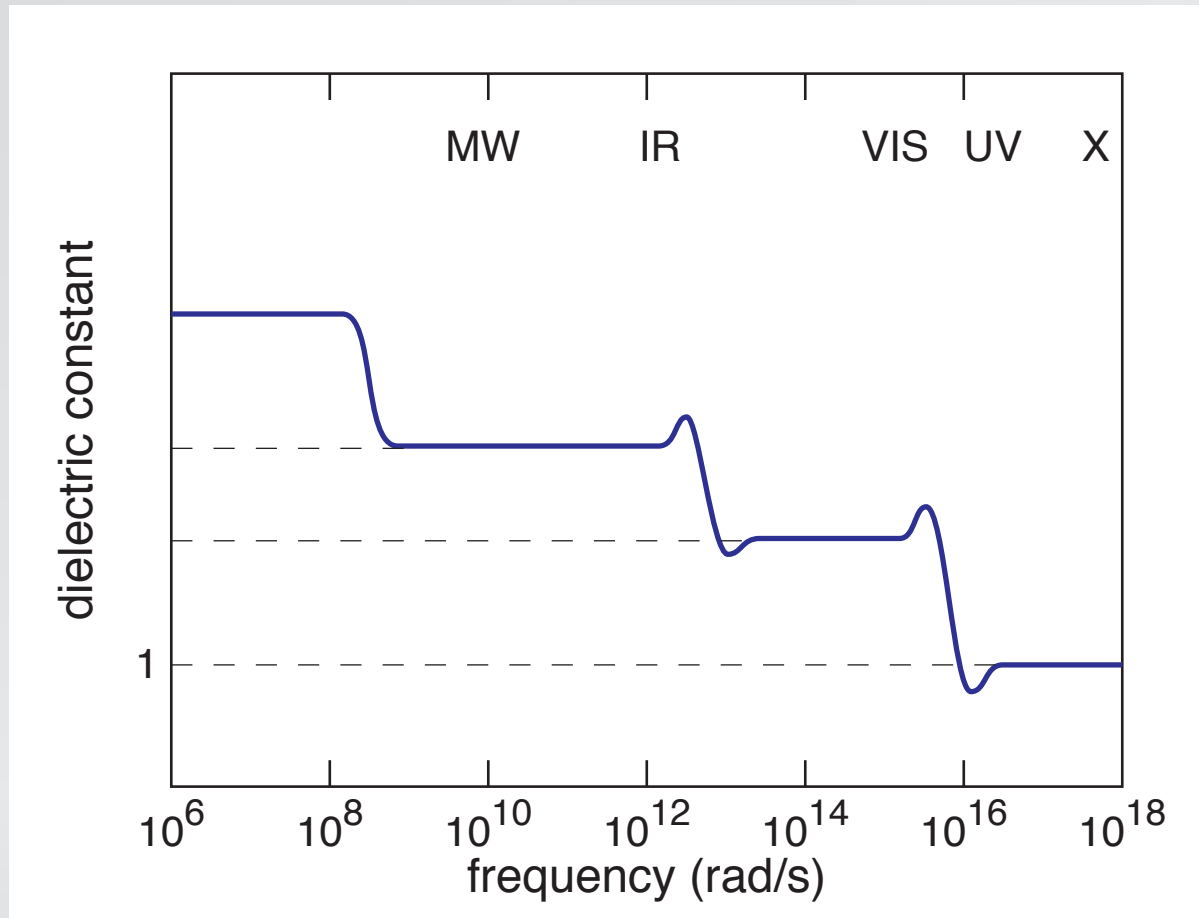
# Dielectric constant

## Lorentz oscillator

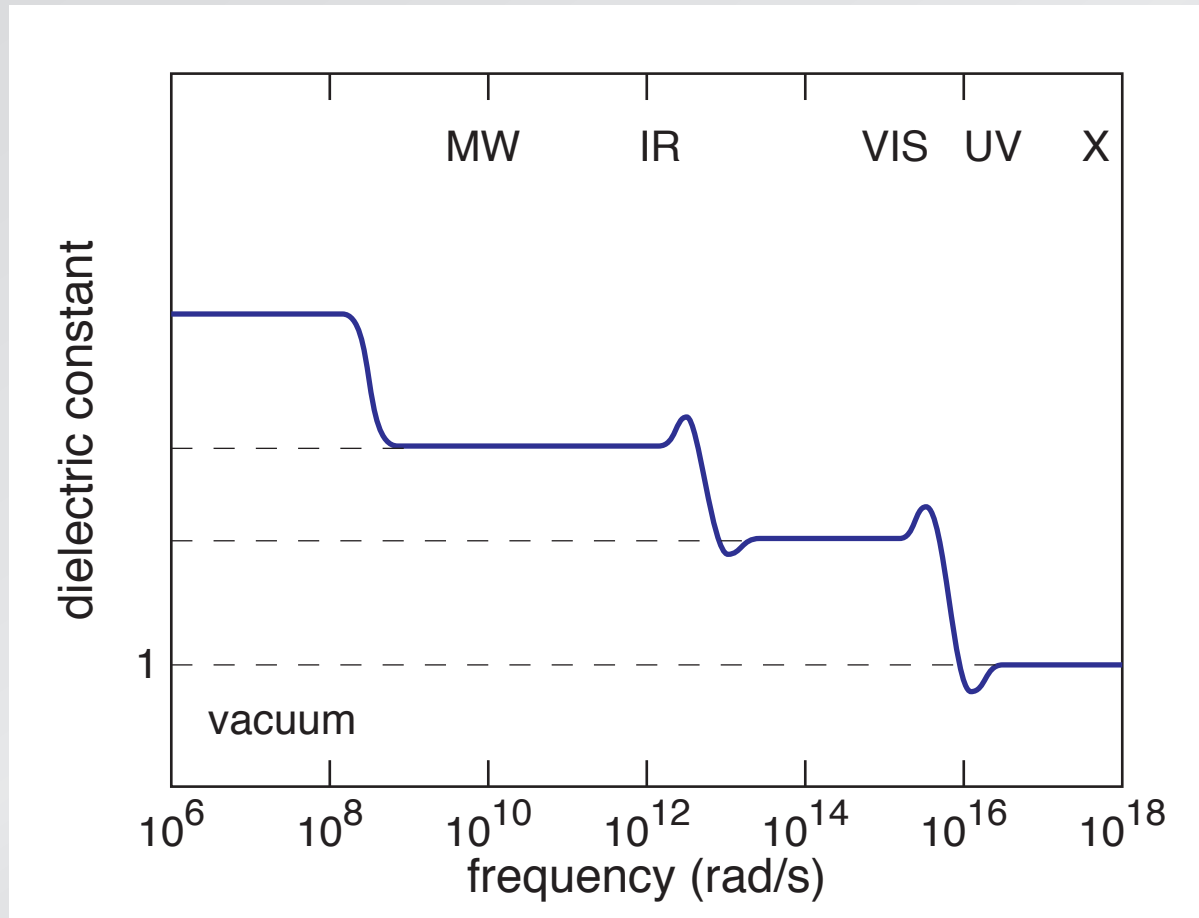




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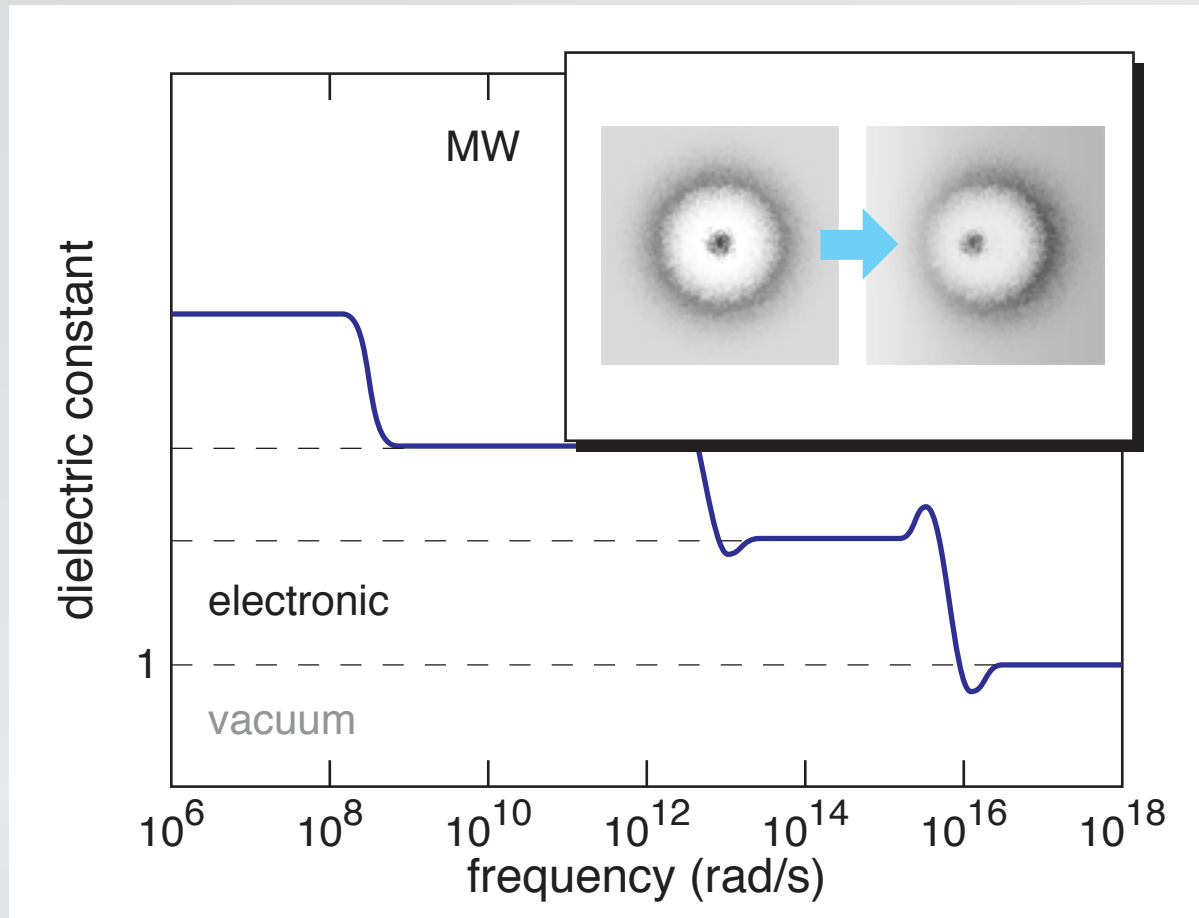


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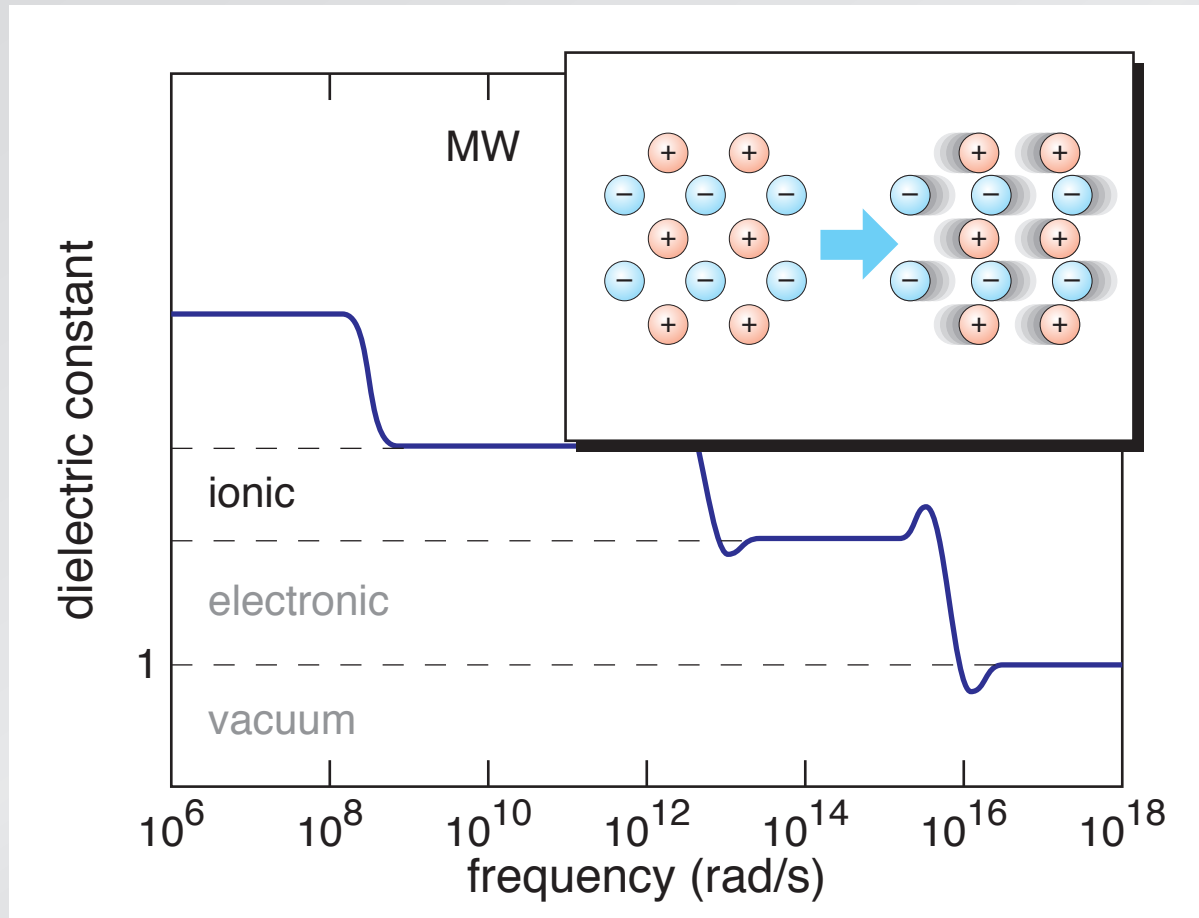




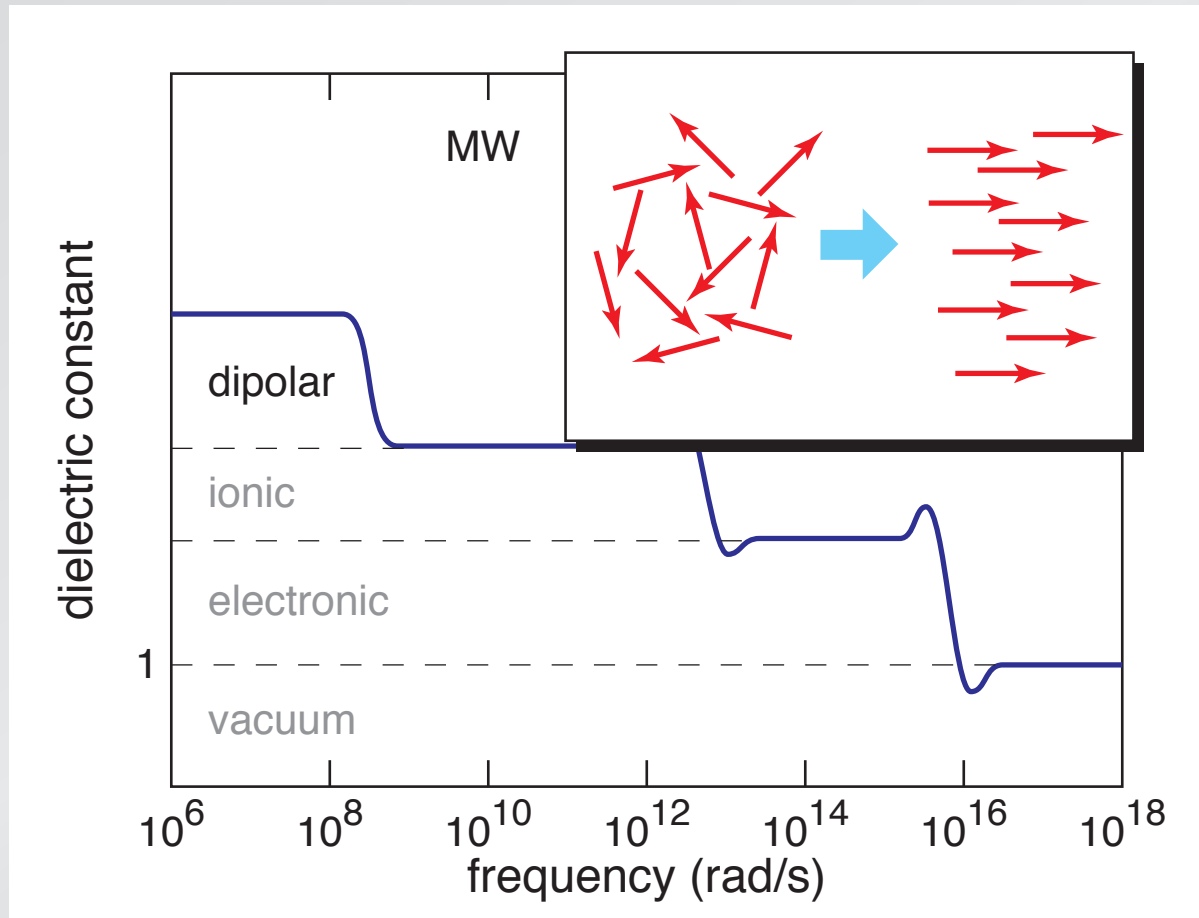
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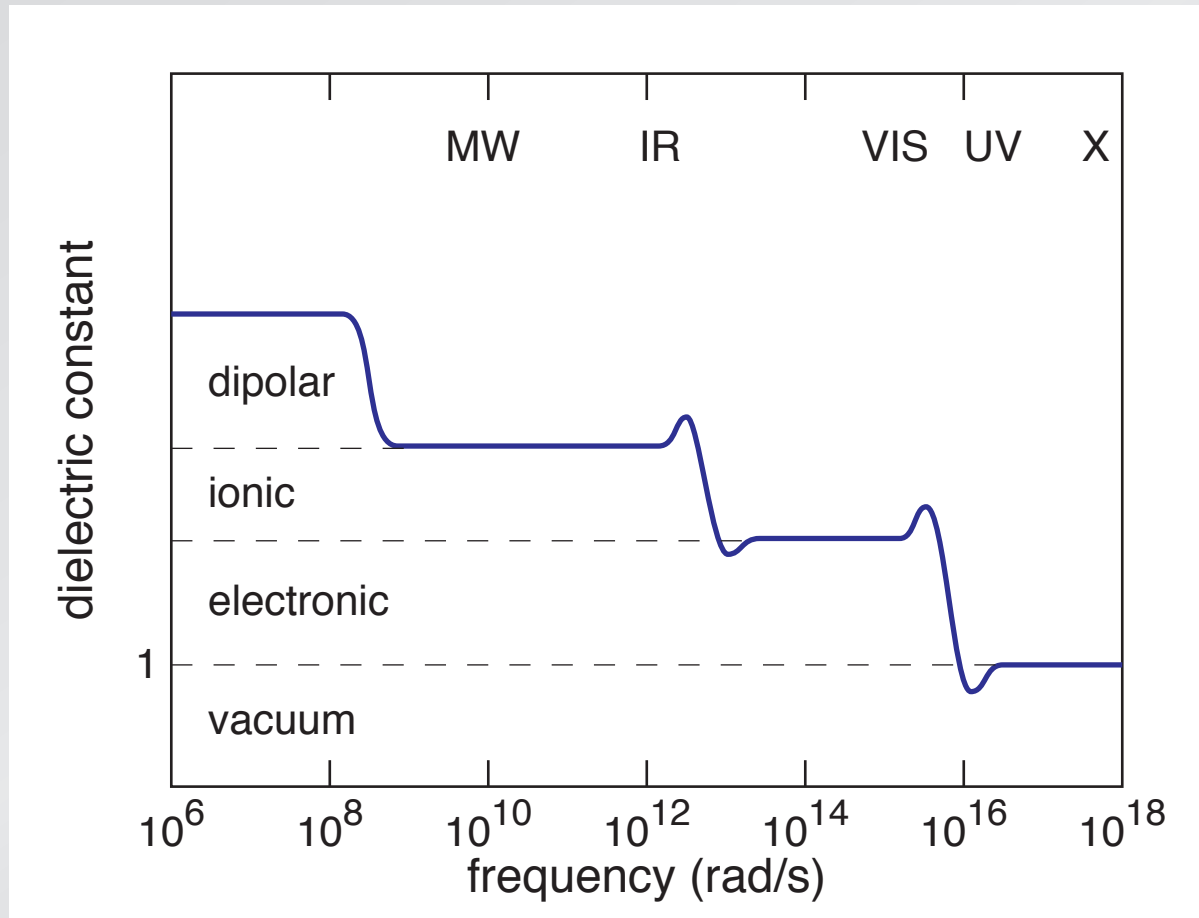


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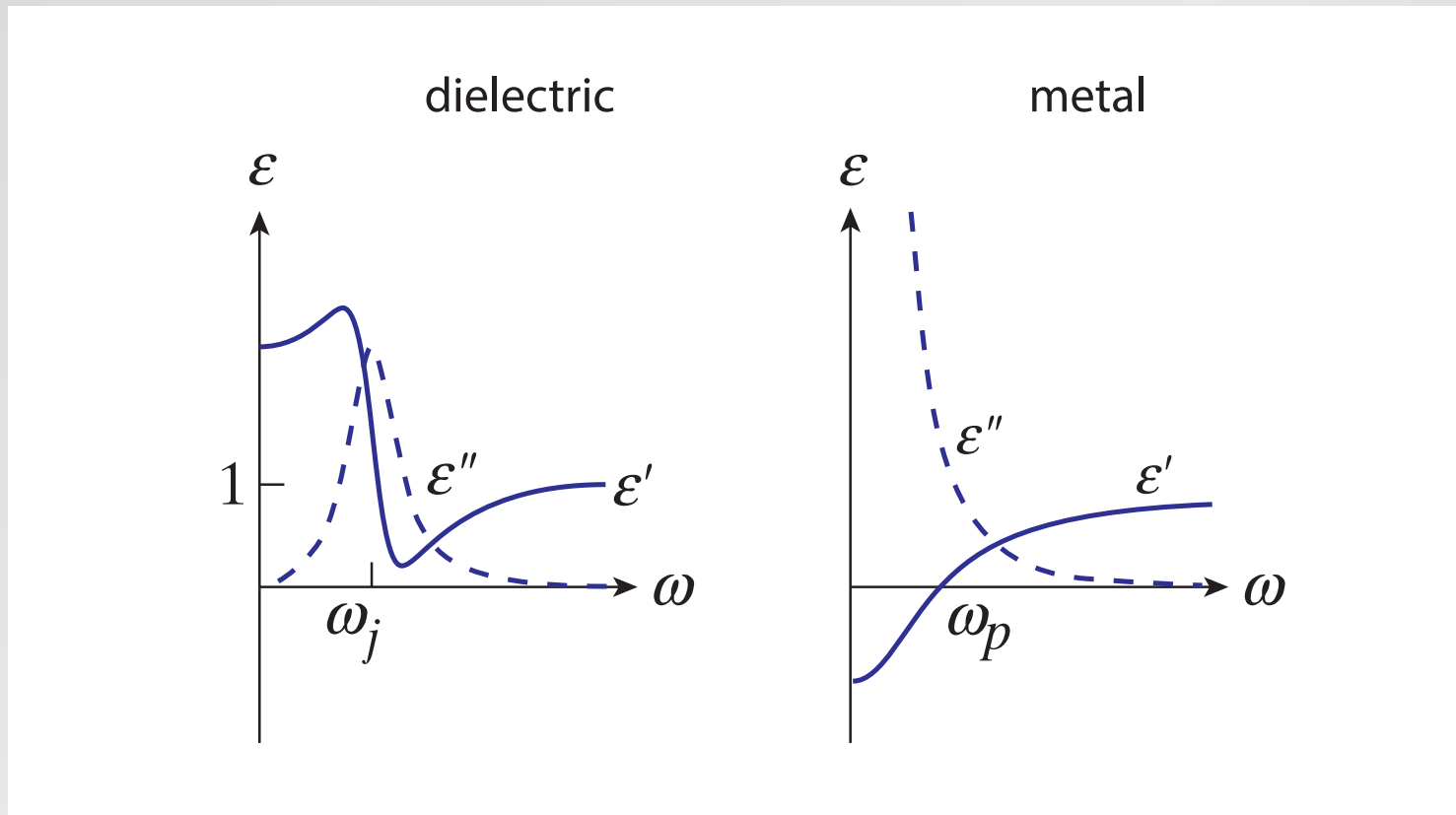




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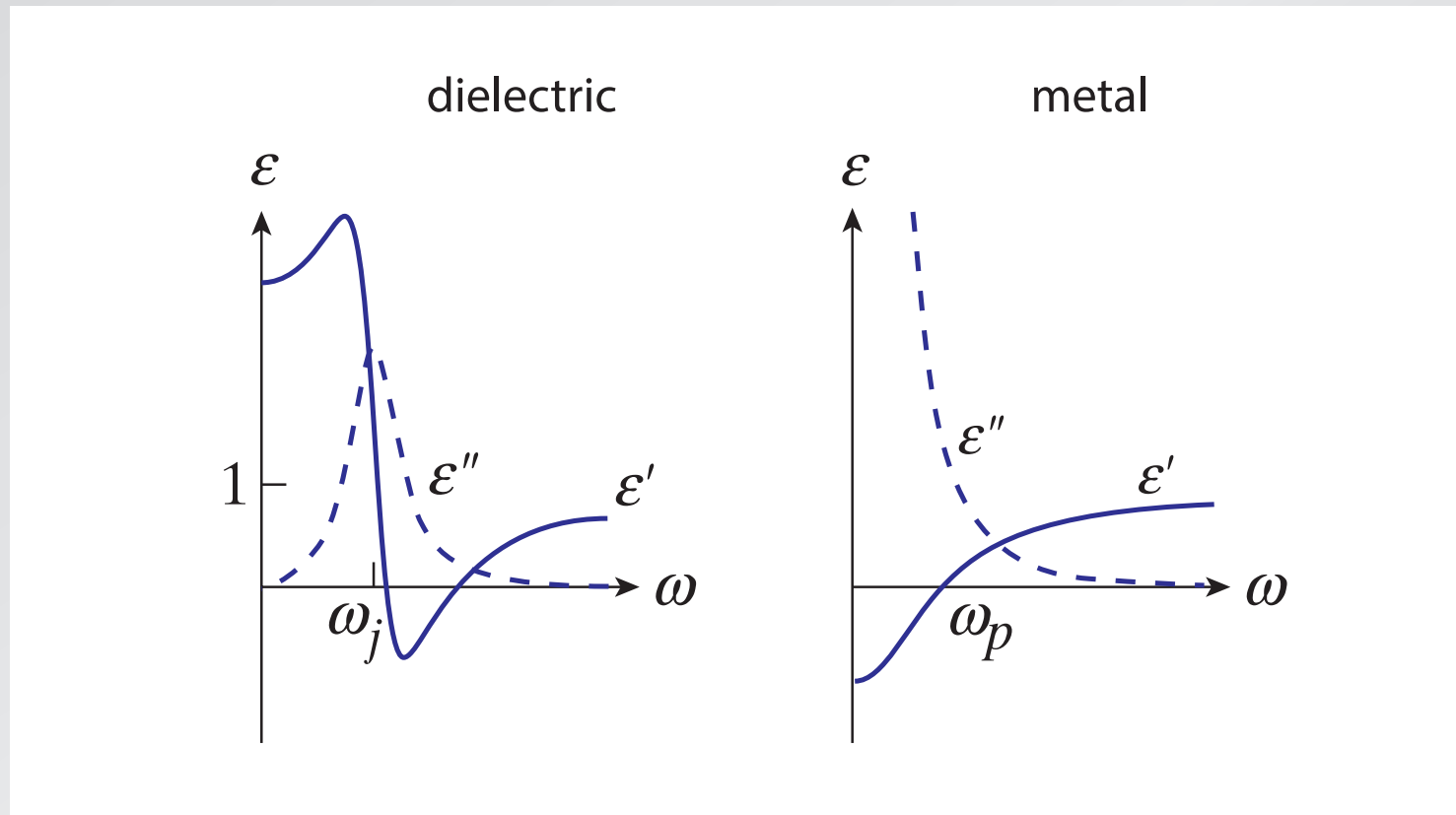


# Lorentz and Drude models



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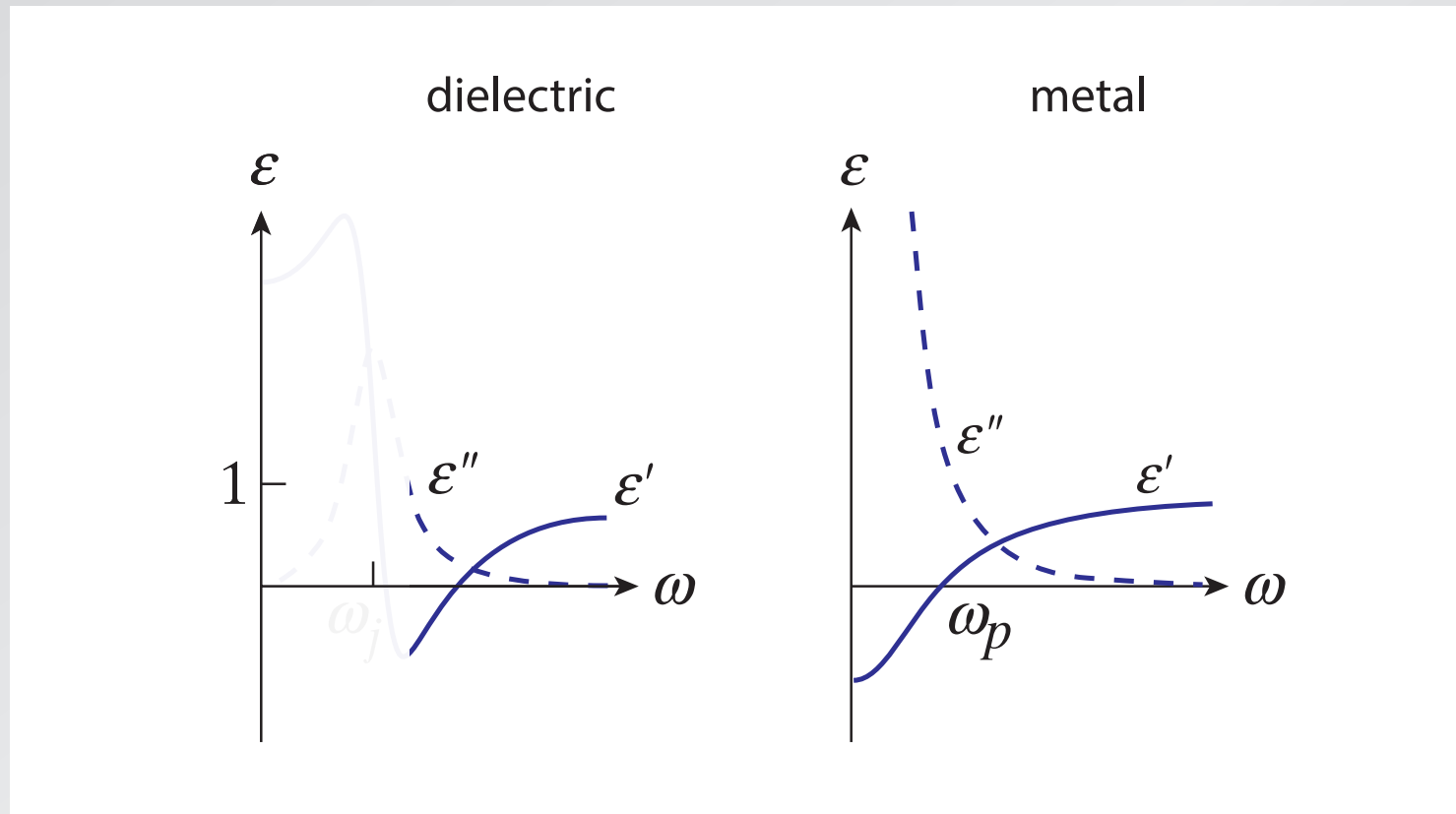
for a strong (dielectric) resonance  $\epsilon$  can become negative





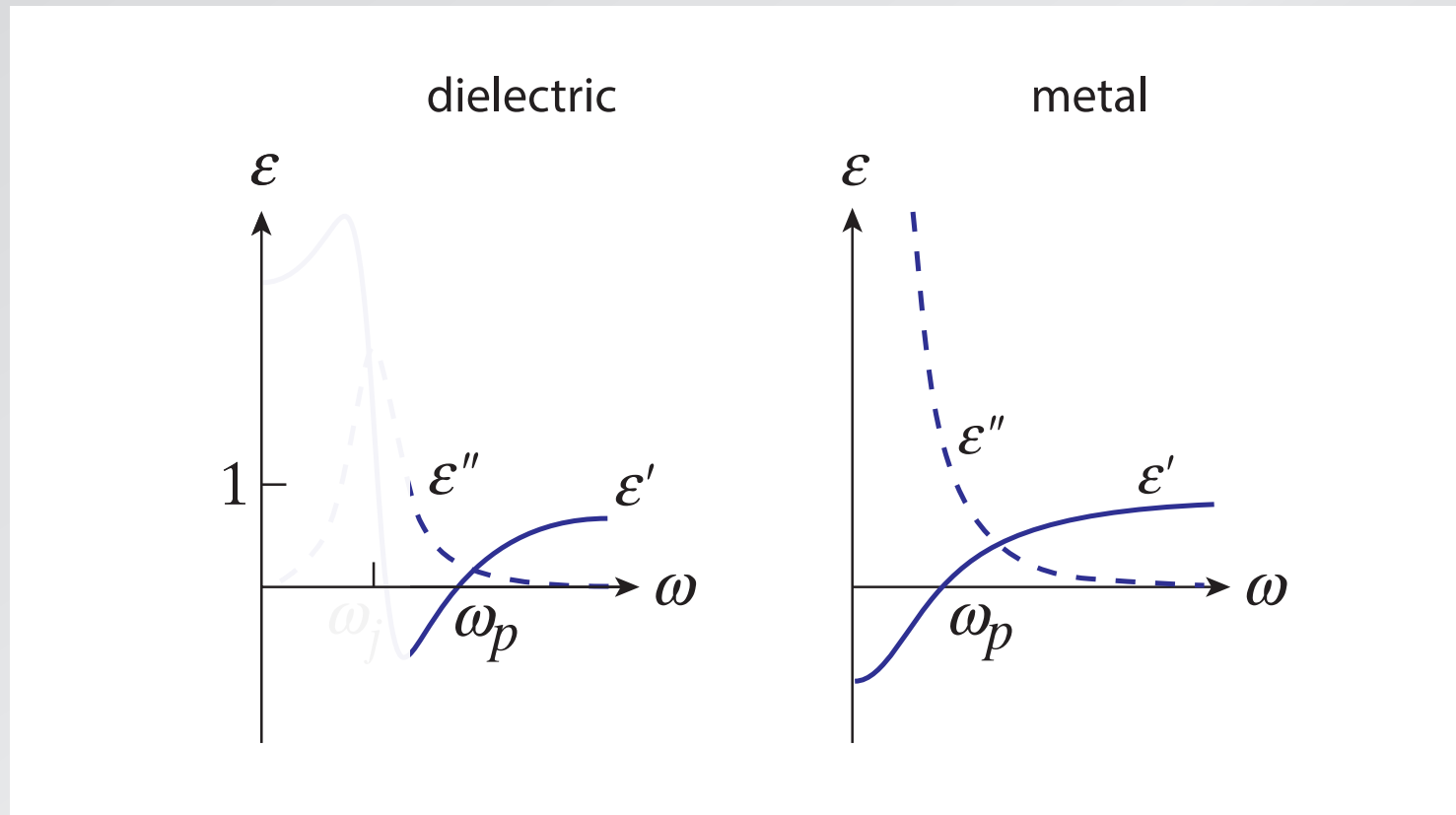
# Lorentz and Drude models

valence electrons in dielectric then behave like a plasma



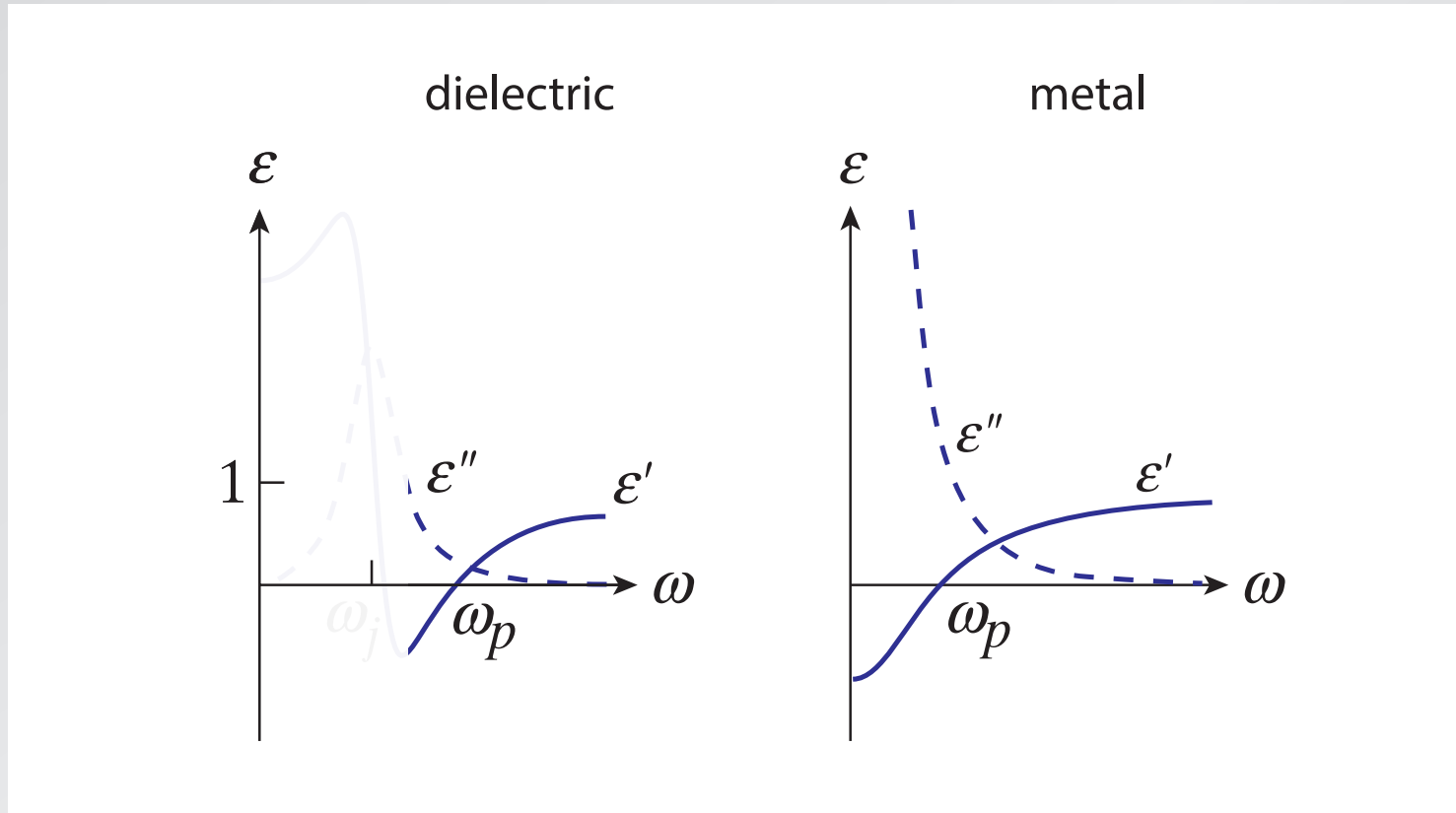
# Lorentz and Drude models

with plasma frequency above the resonance



# Lorentz and Drude models

(and far below the UV region)





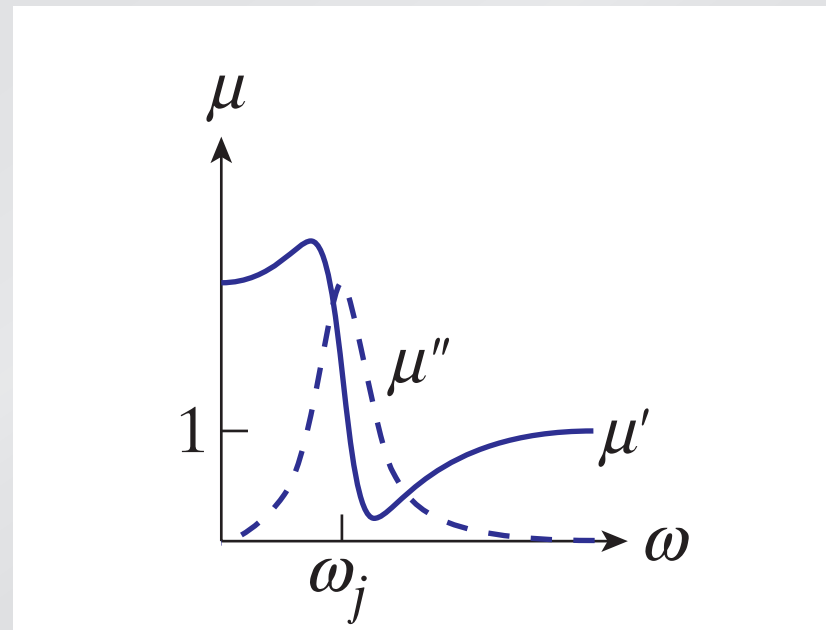
Index also determined by magnetic response

$$n = \sqrt{\epsilon \mu}$$

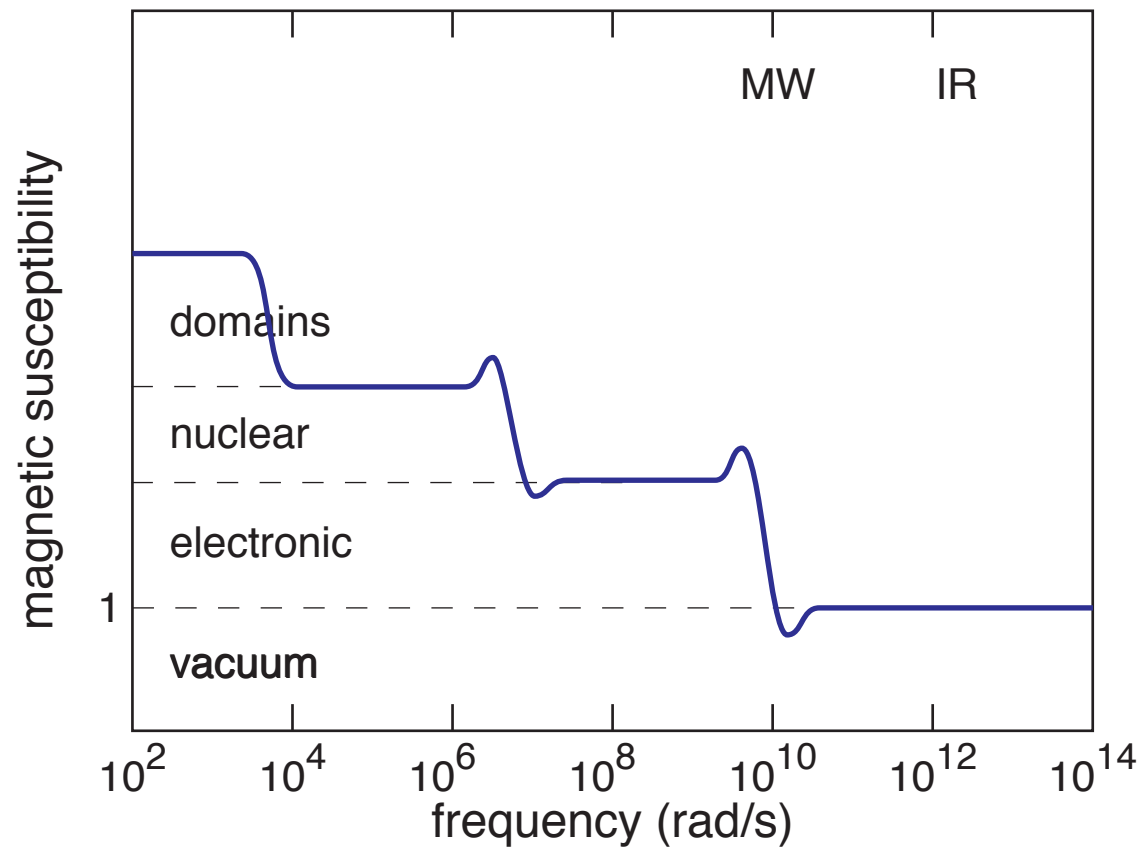
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and magnetic response shows similar resonances

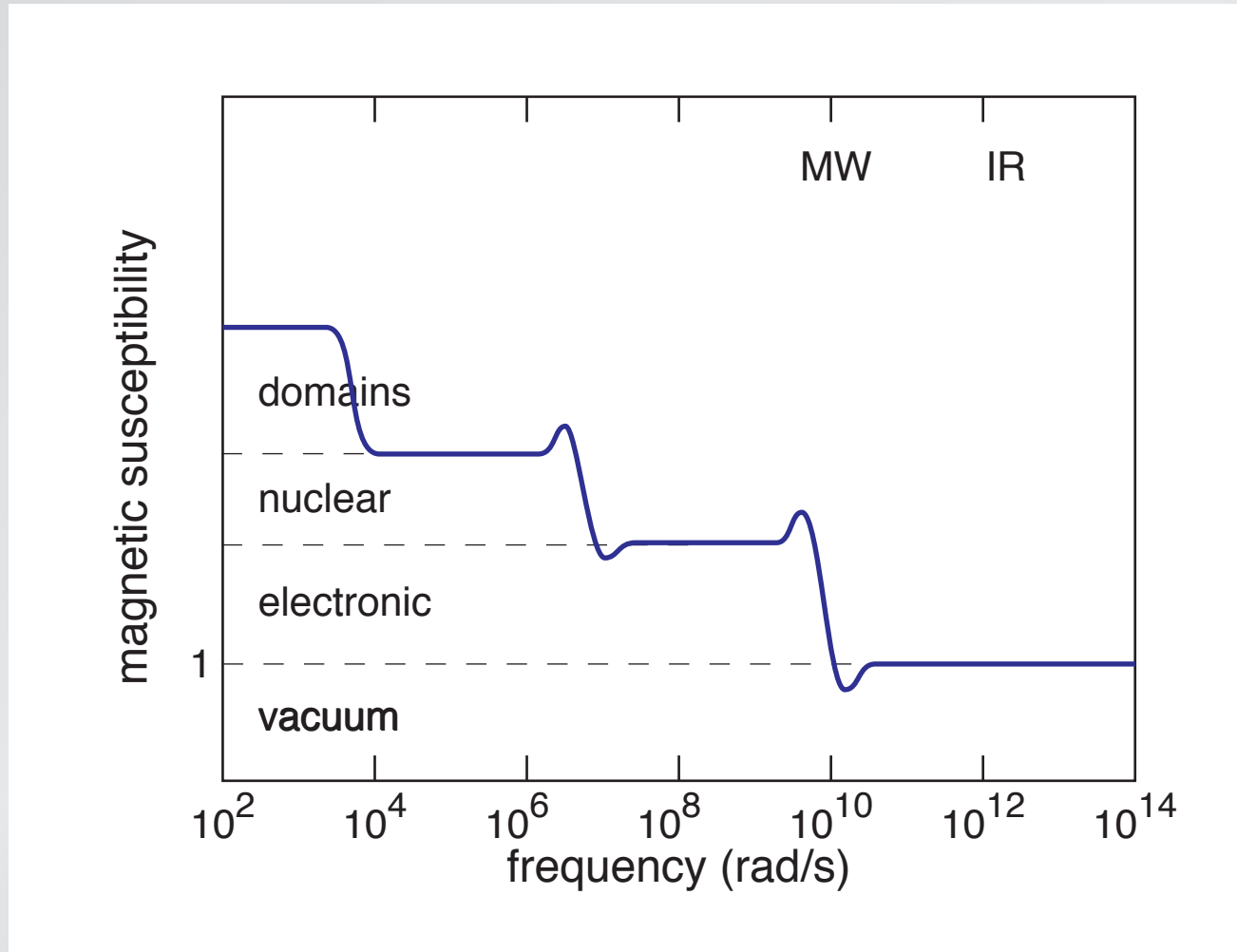


# Magnetic response



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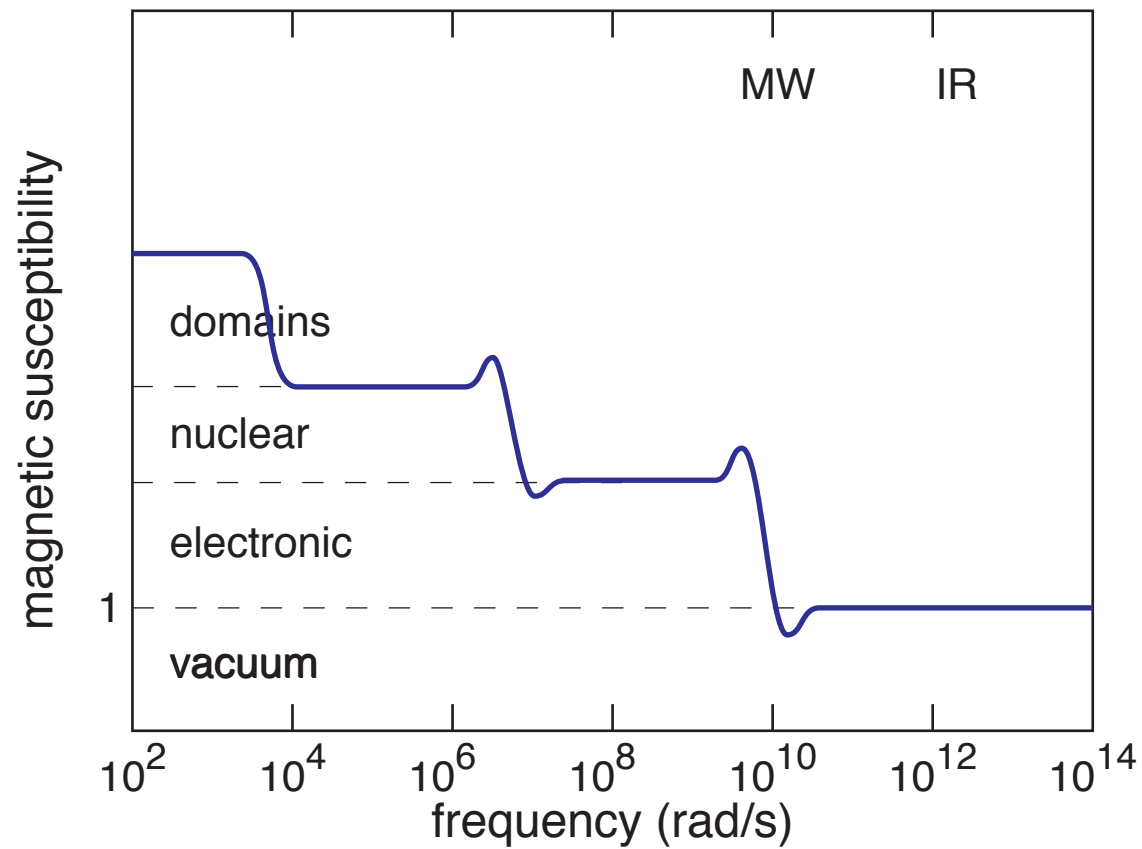
but magnetic resonances occur below optical frequencies





# Magnetic response

so, in optical regime,  $\mu \approx 1$



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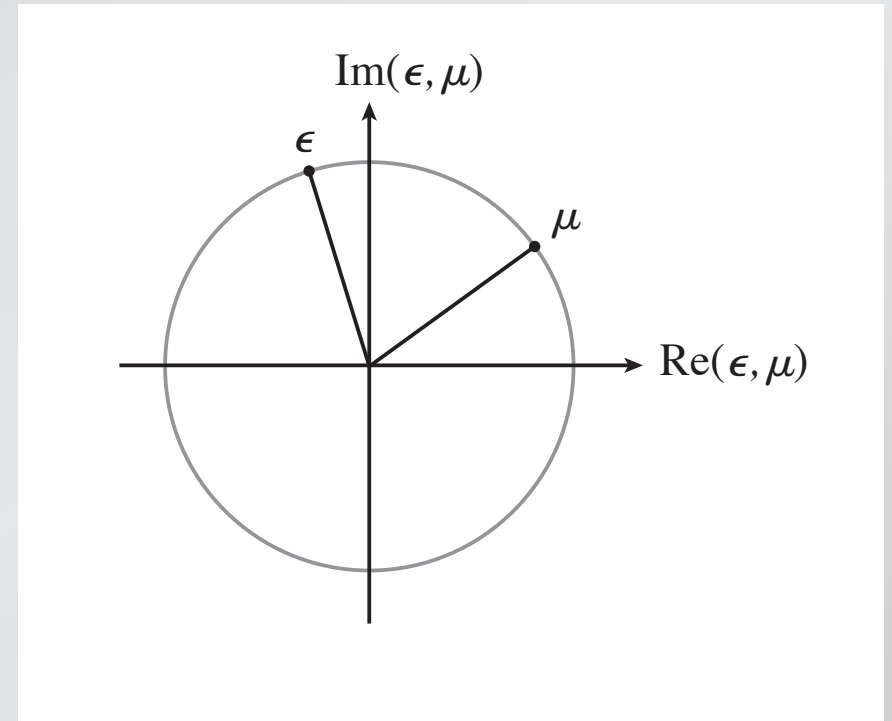
What happens when  $\text{Re}\epsilon$  and/or  $\text{Re}\mu$  is negative?

Write complex quantities as

$$\varepsilon = |\varepsilon| e^{i\theta} \quad \mu = |\mu| e^{i\phi}$$

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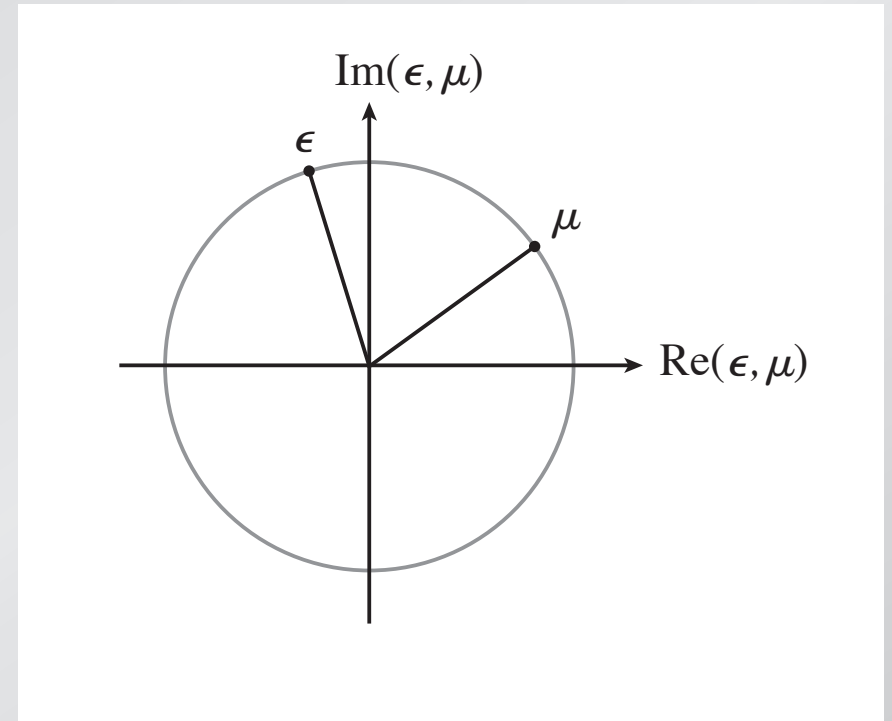


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$$n = \sqrt{|\varepsilon||\mu|} e^{i\frac{\theta+\phi}{2}}$$

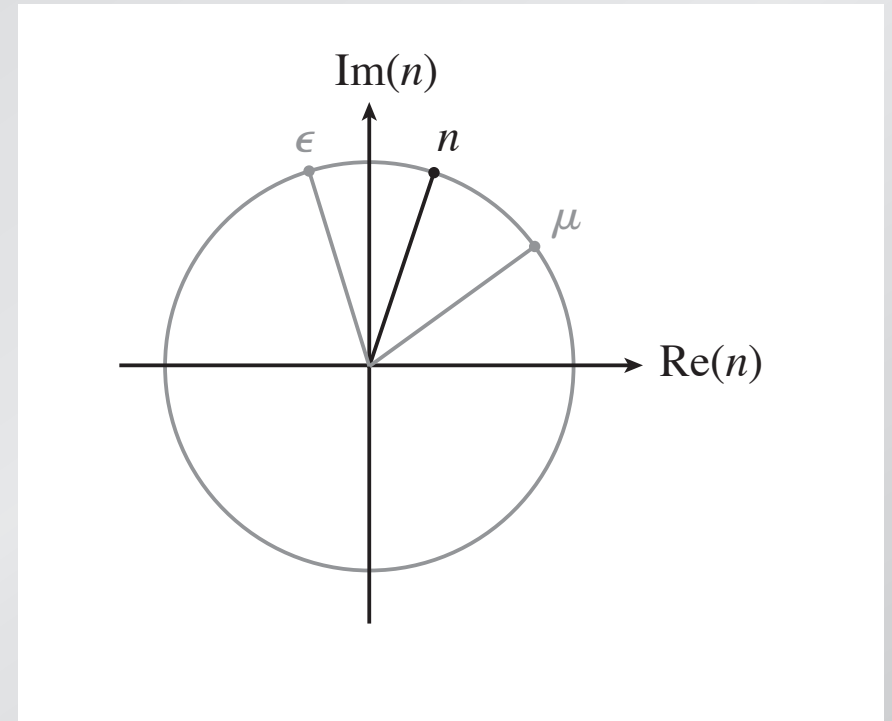


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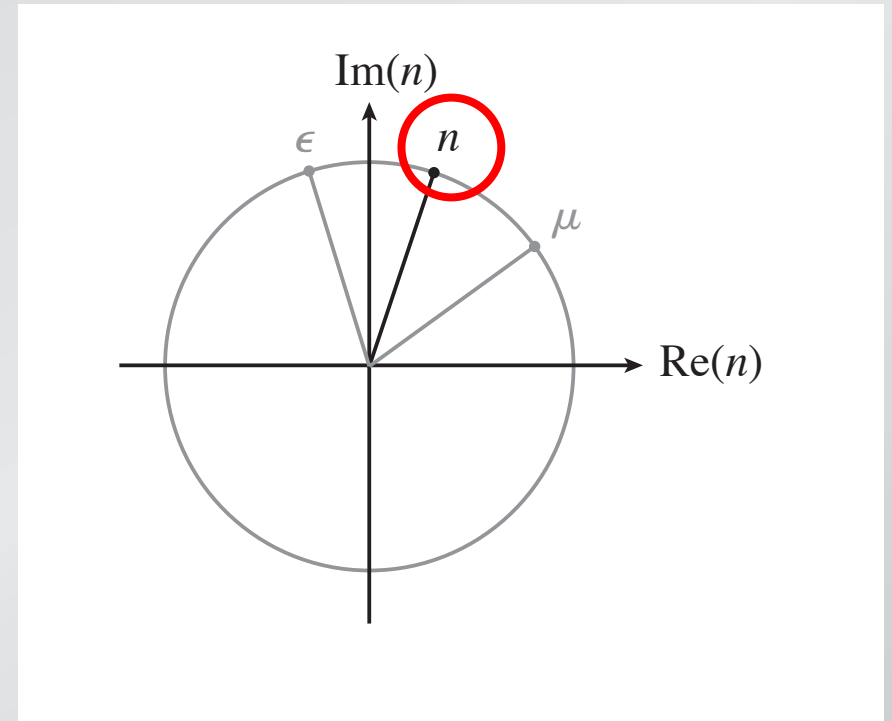
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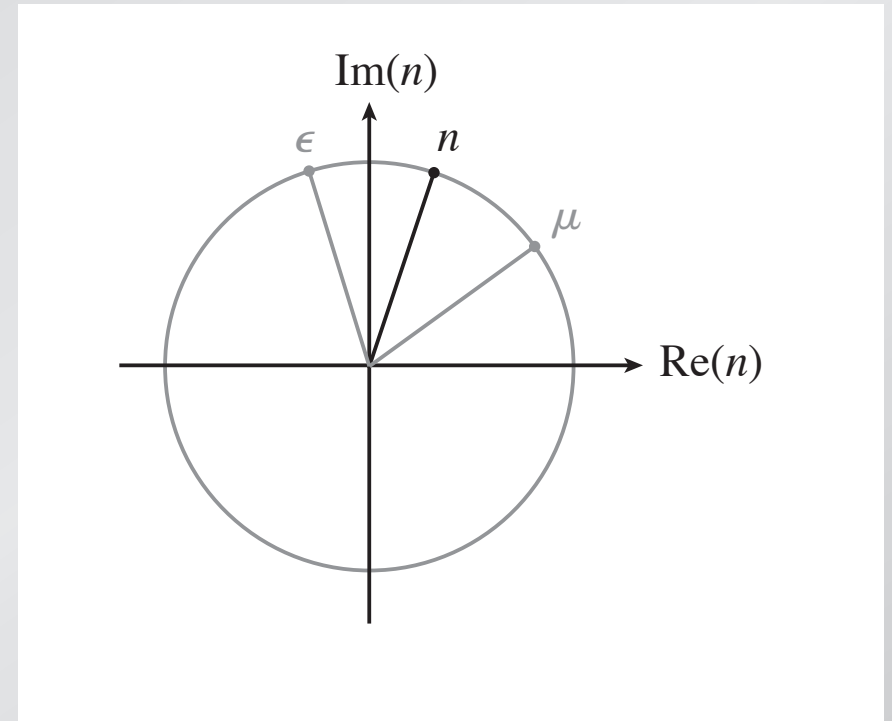
$$n = \sqrt{|\varepsilon||\mu|} e^{i\frac{\theta+\phi}{2}}$$

Q: Is this only possible value?

1. yes
2. no, there's one more
3. there are many more
4. it depends



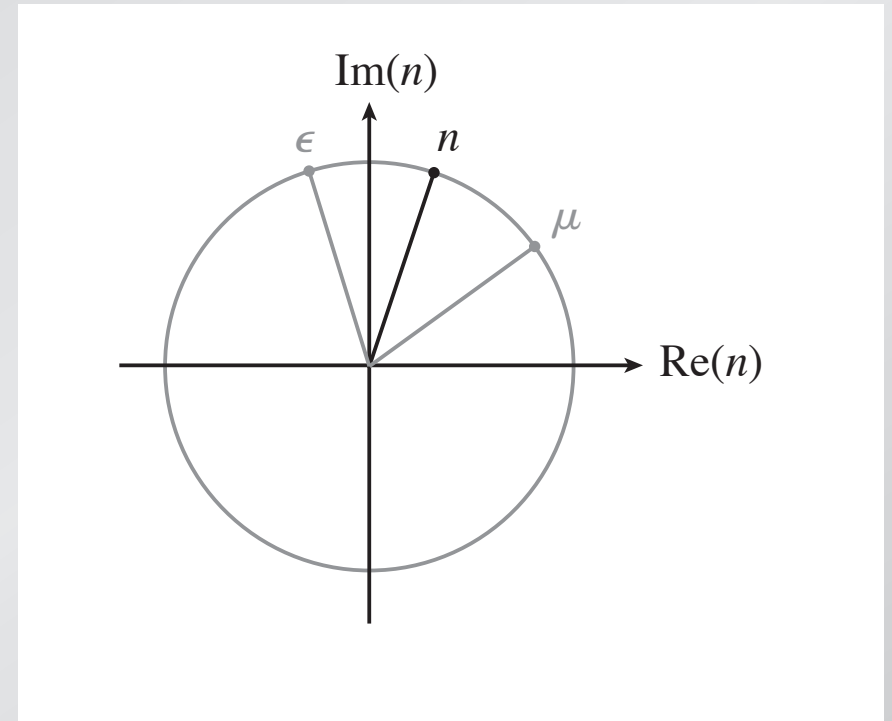
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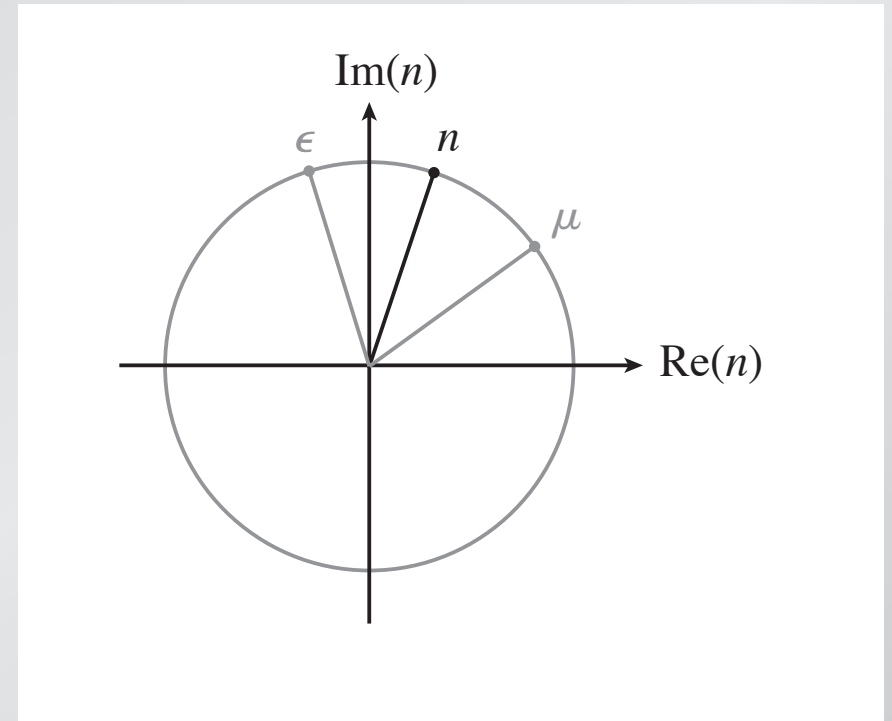
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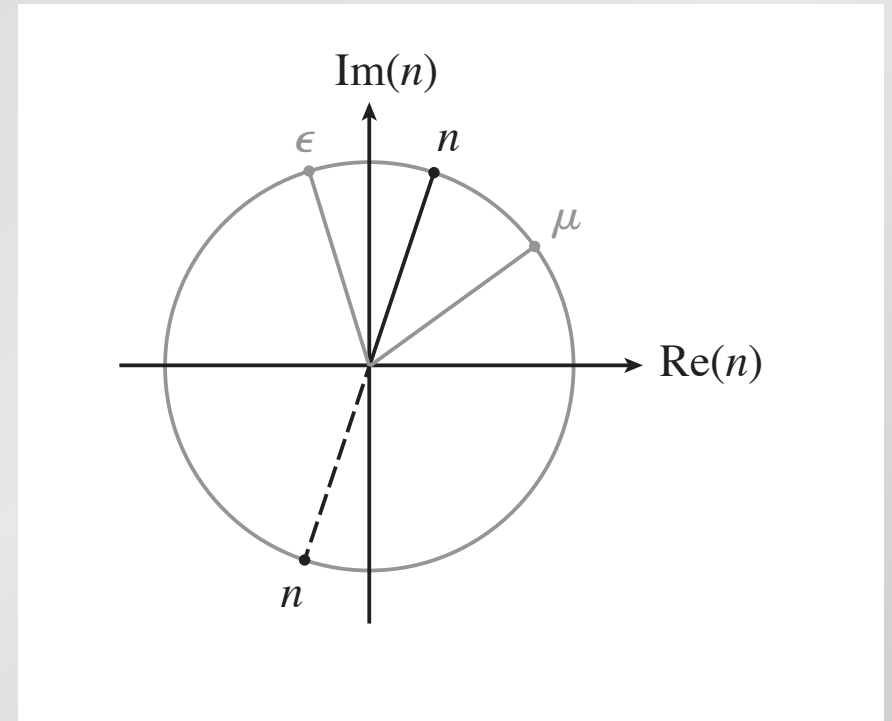
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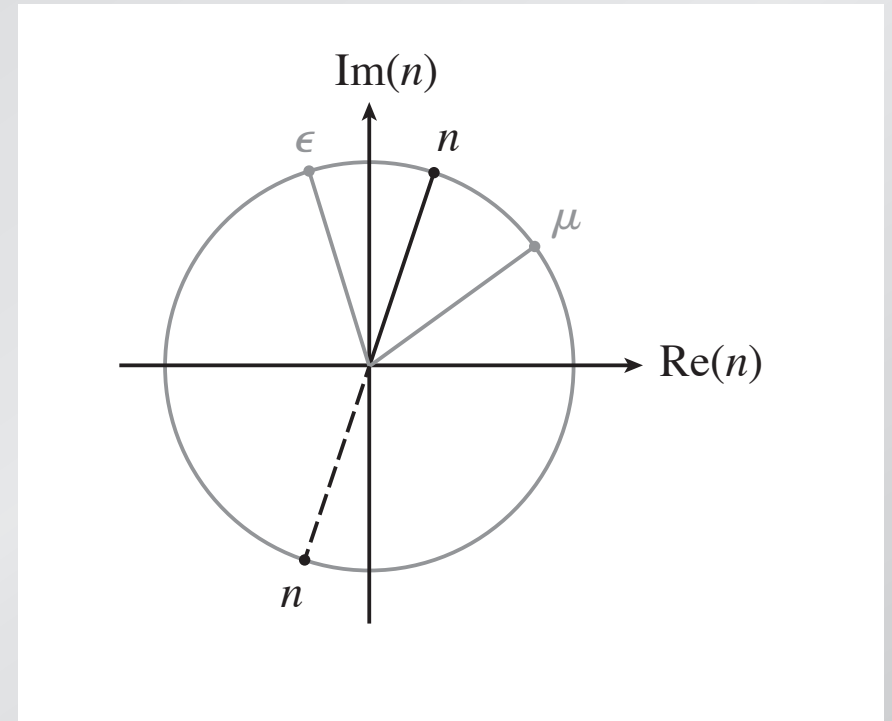
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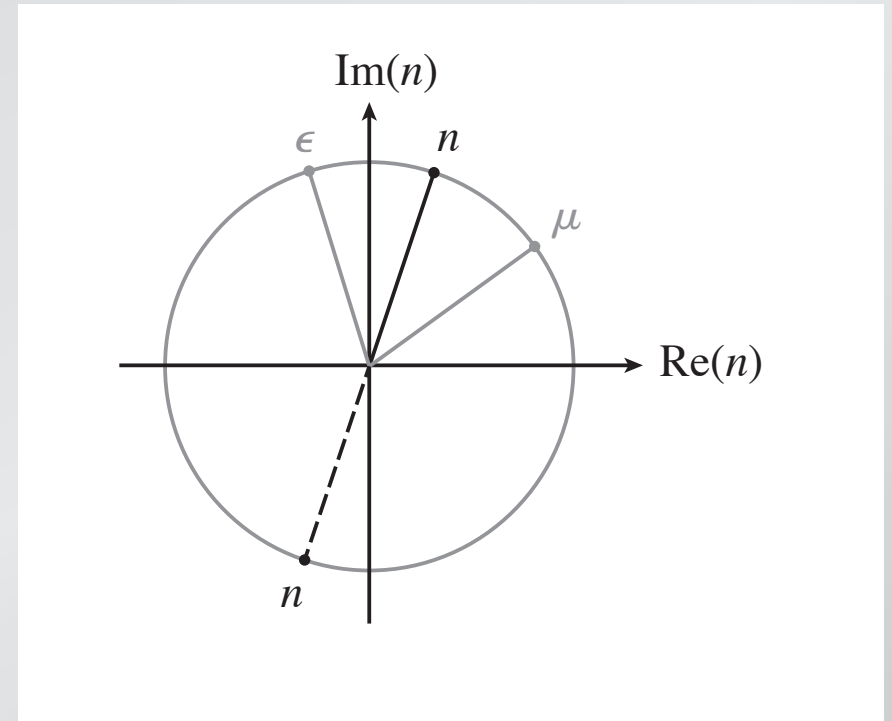
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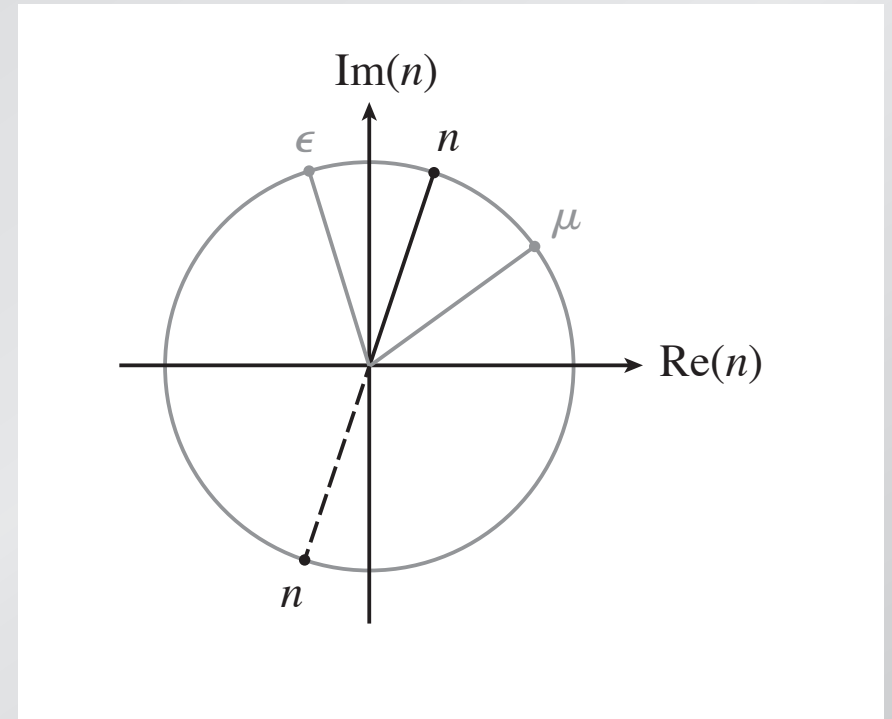
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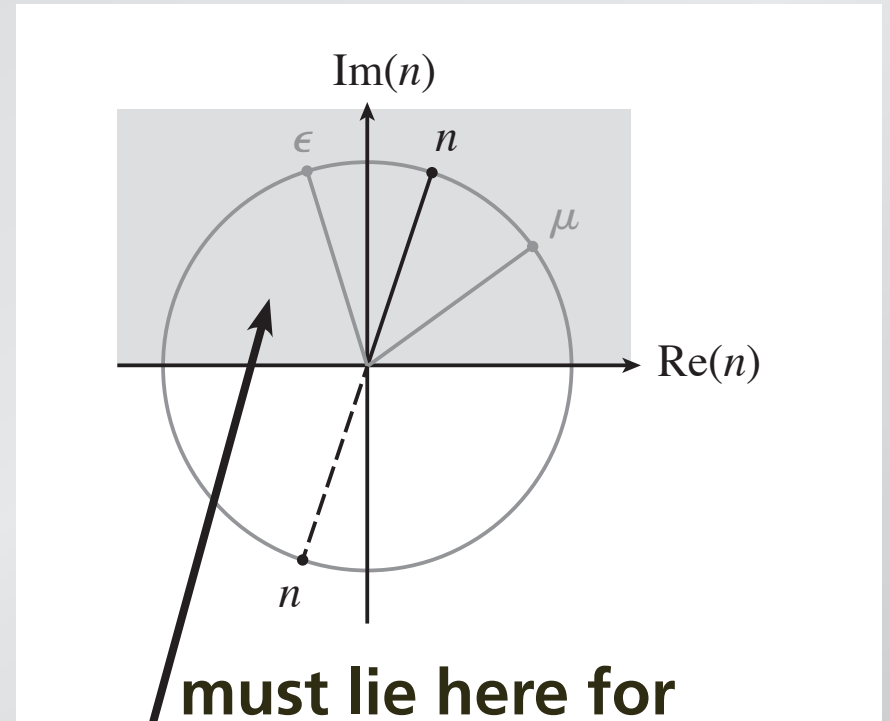
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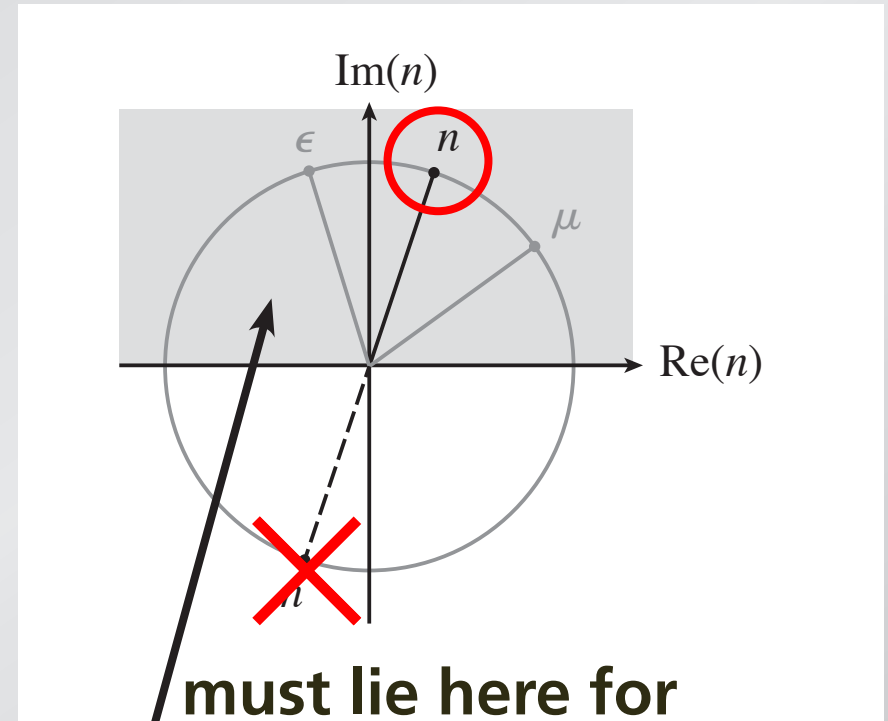
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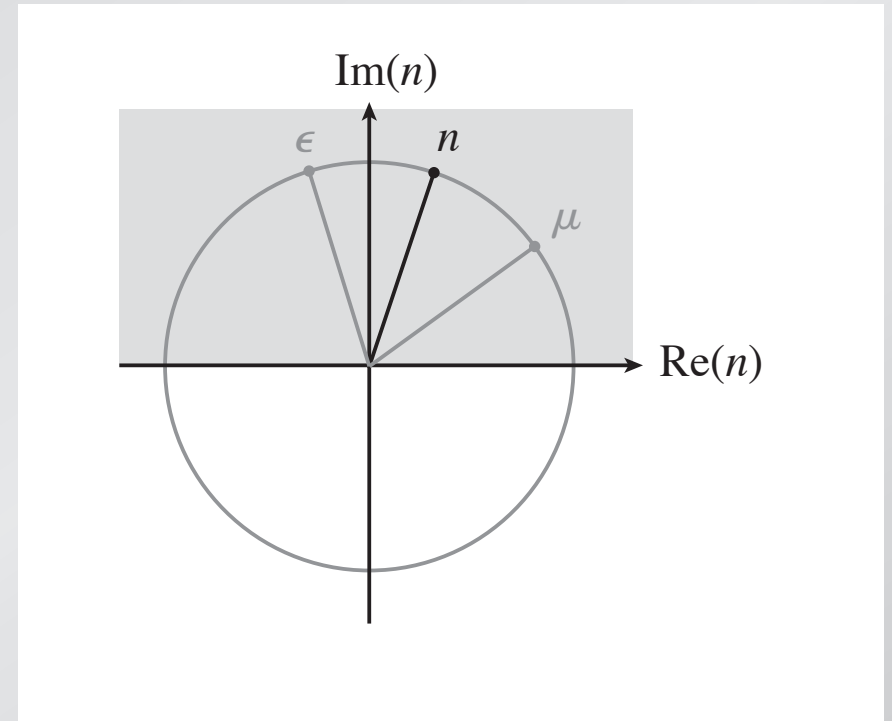
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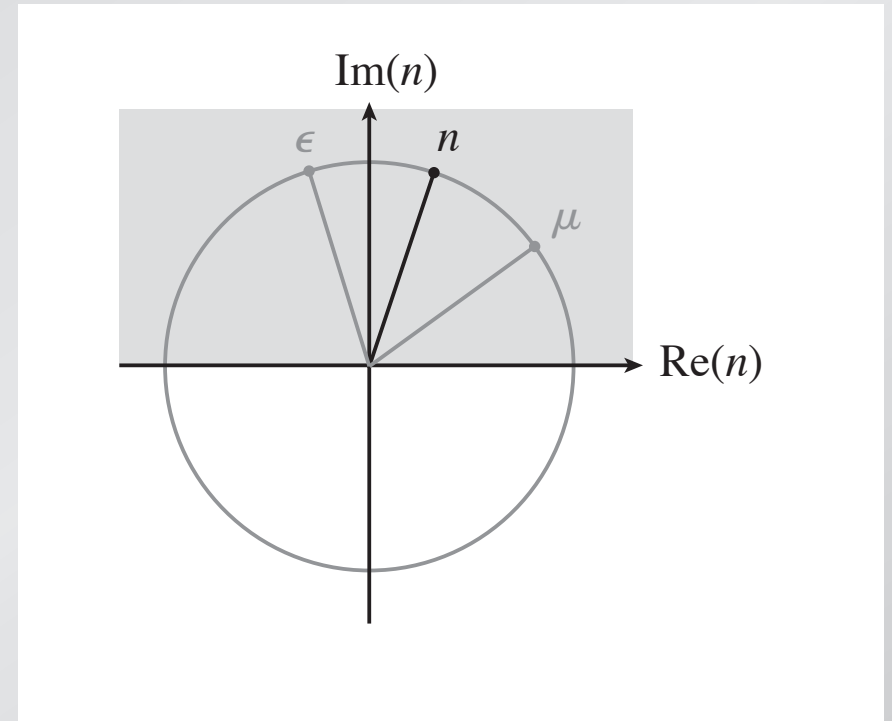
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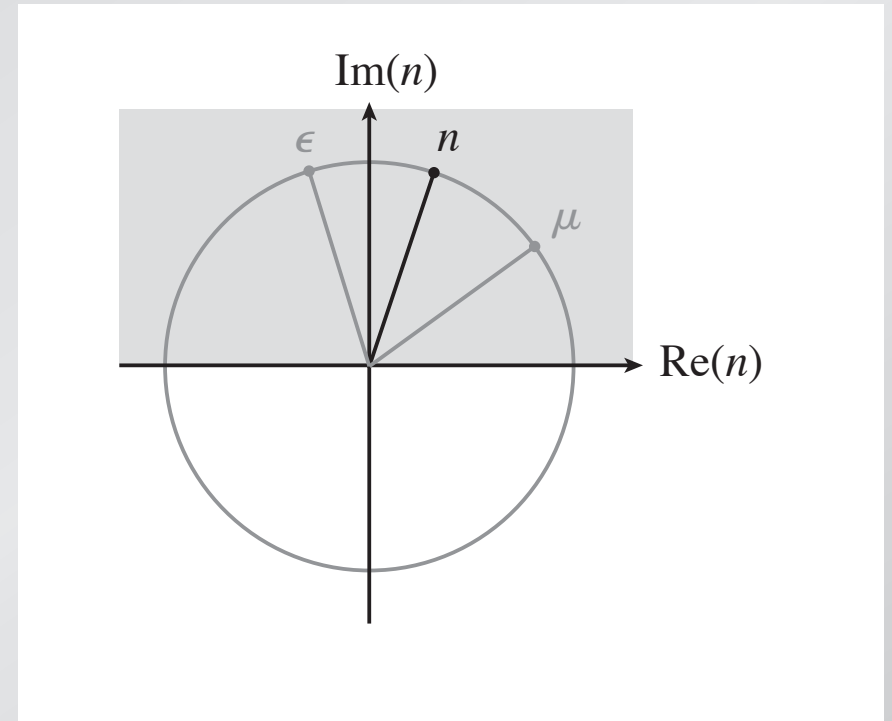
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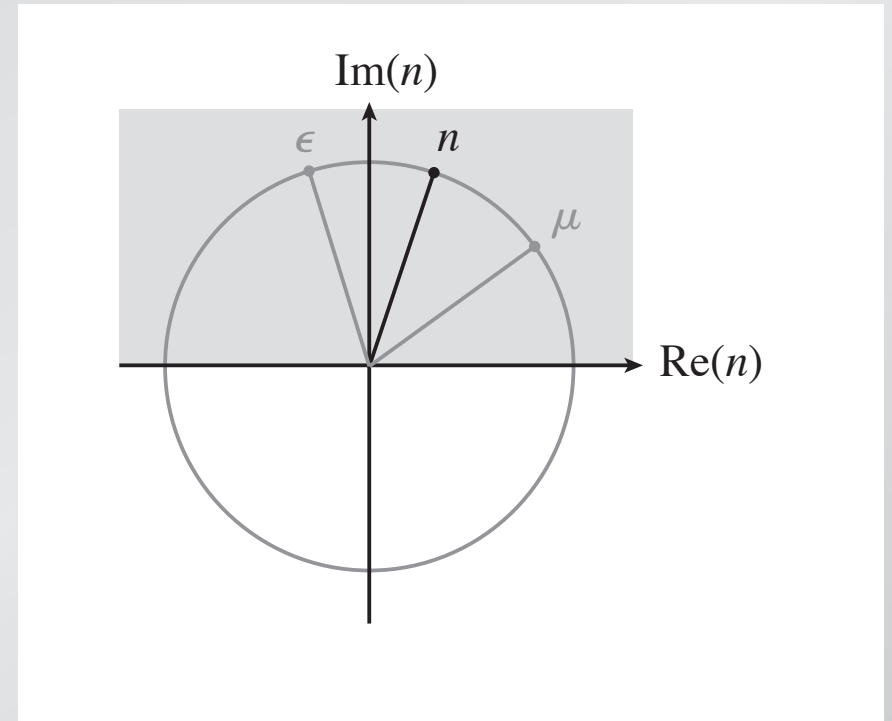
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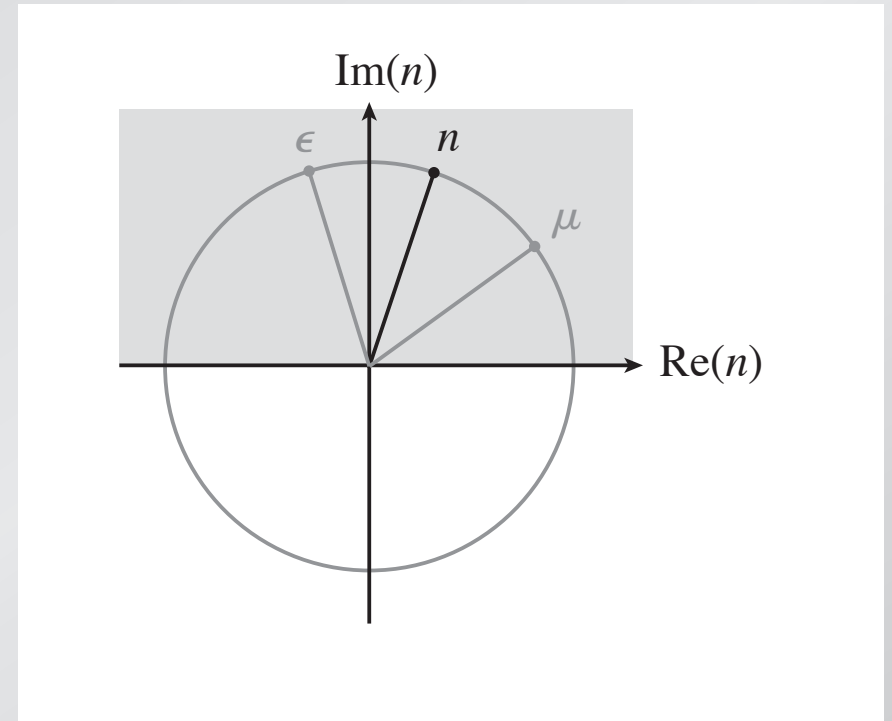
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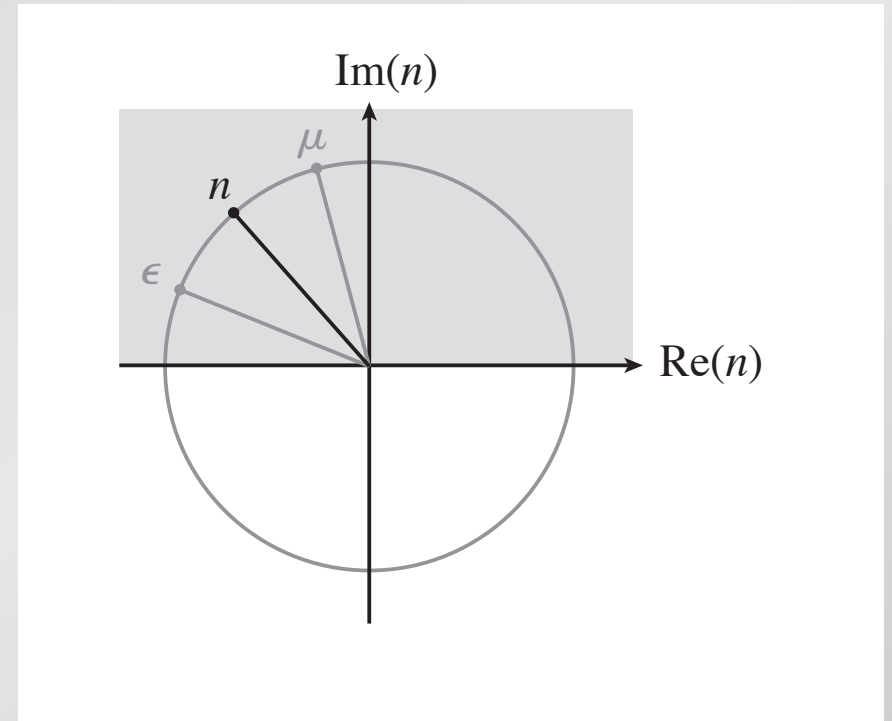
To find  $n$  (passive materials):

1. Draw line that bisects  $\epsilon$  and  $\mu$
2. Choose upper branch



**What happens when  $\text{Re}\epsilon$  and/or  $\text{Re}\mu$  is negative?**

For certain values of  $\epsilon$  and  $\mu$   
we can get a *negative*  $\text{Re}(n)$ !



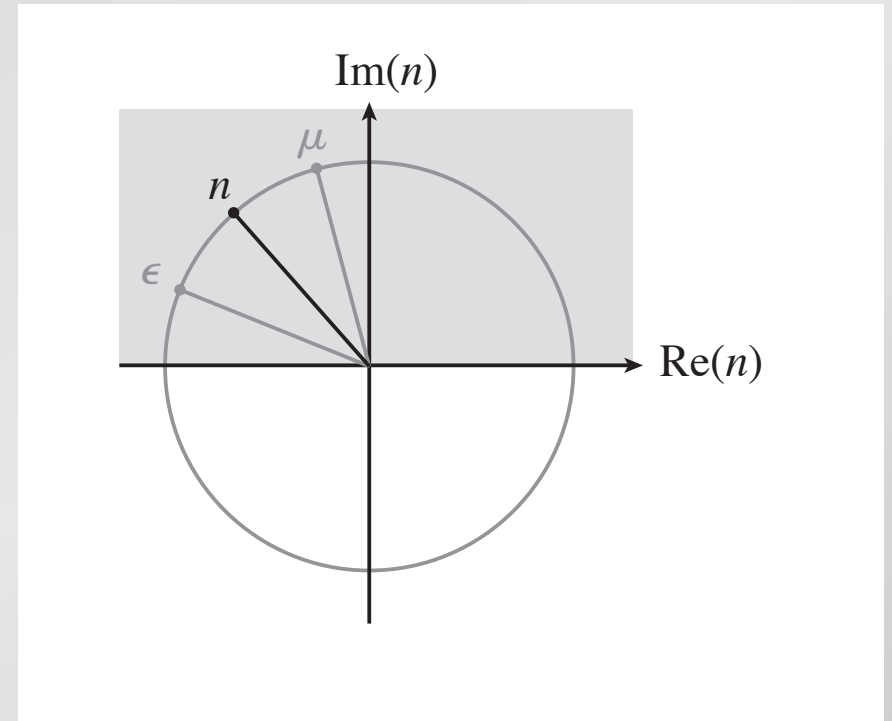


**Q: Must both  $\text{Re}\epsilon < 0$  and  $\text{Re}\mu < 0$**

**to get a negative  $\text{Re}(n)$ ?**

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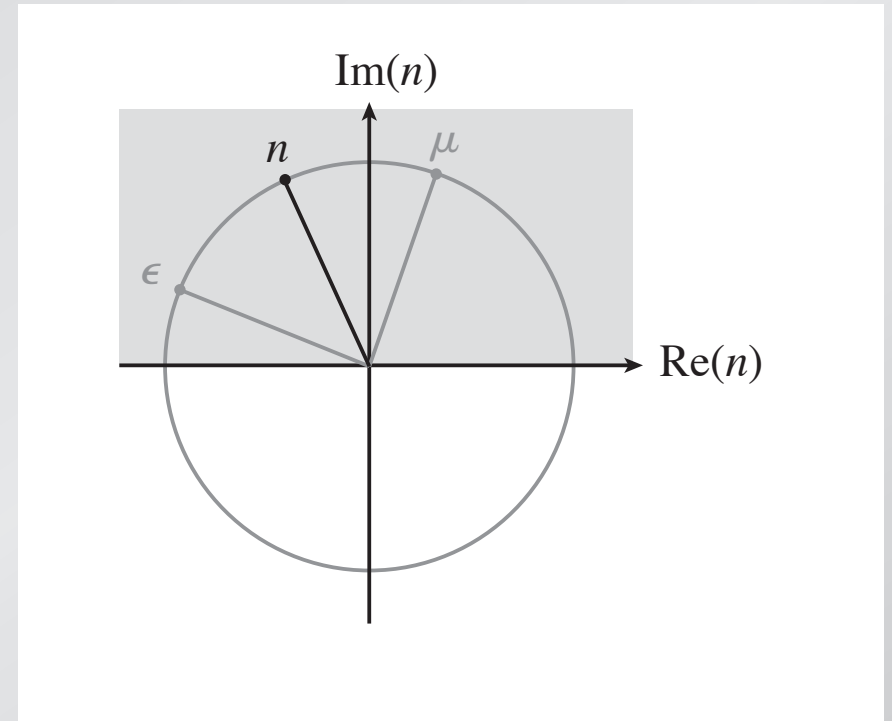


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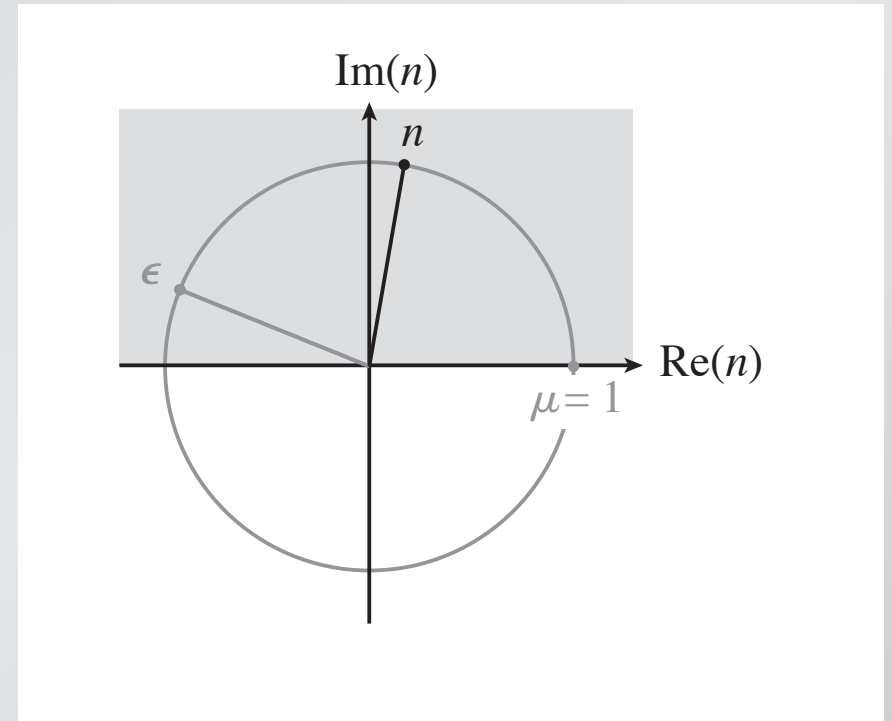
**to get a negative  $\text{Re}(n)$ ?**

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2. no ✓



However, need magnetic response  
to achieve  $\text{Re}(n) \leq 0$ !



What happens when  $\operatorname{Re}(n) < 0$ ?

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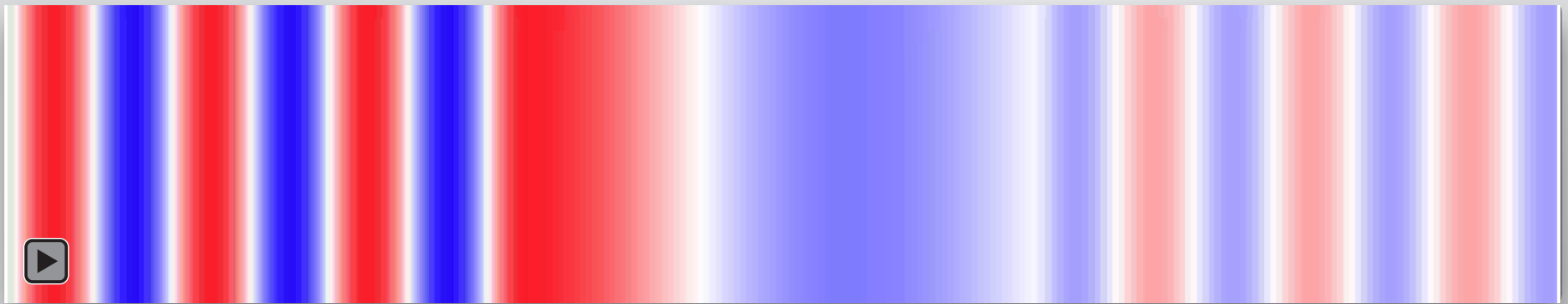
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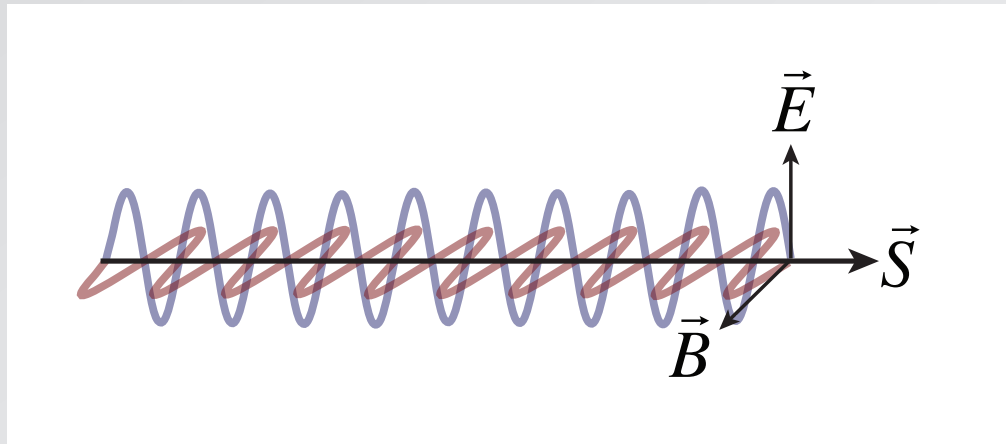
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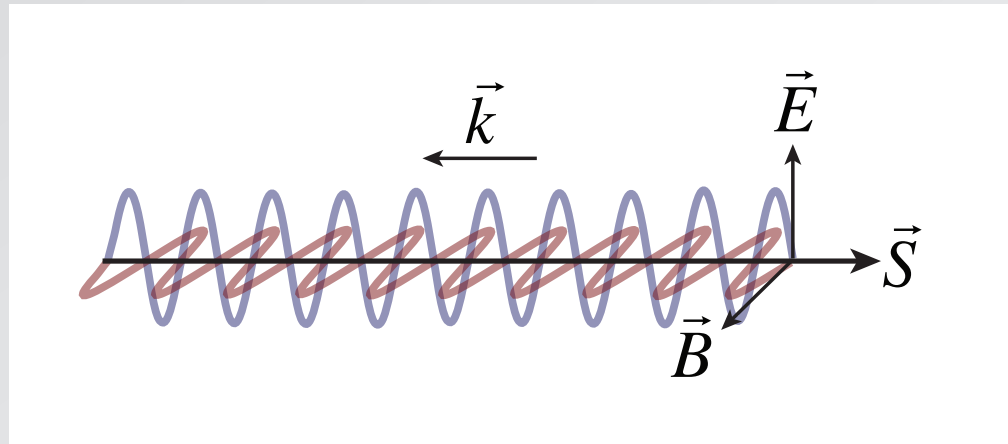


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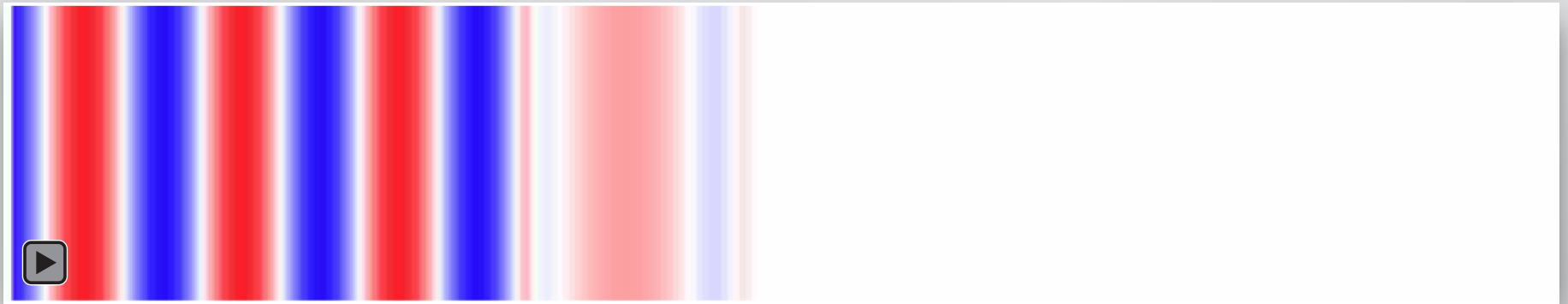


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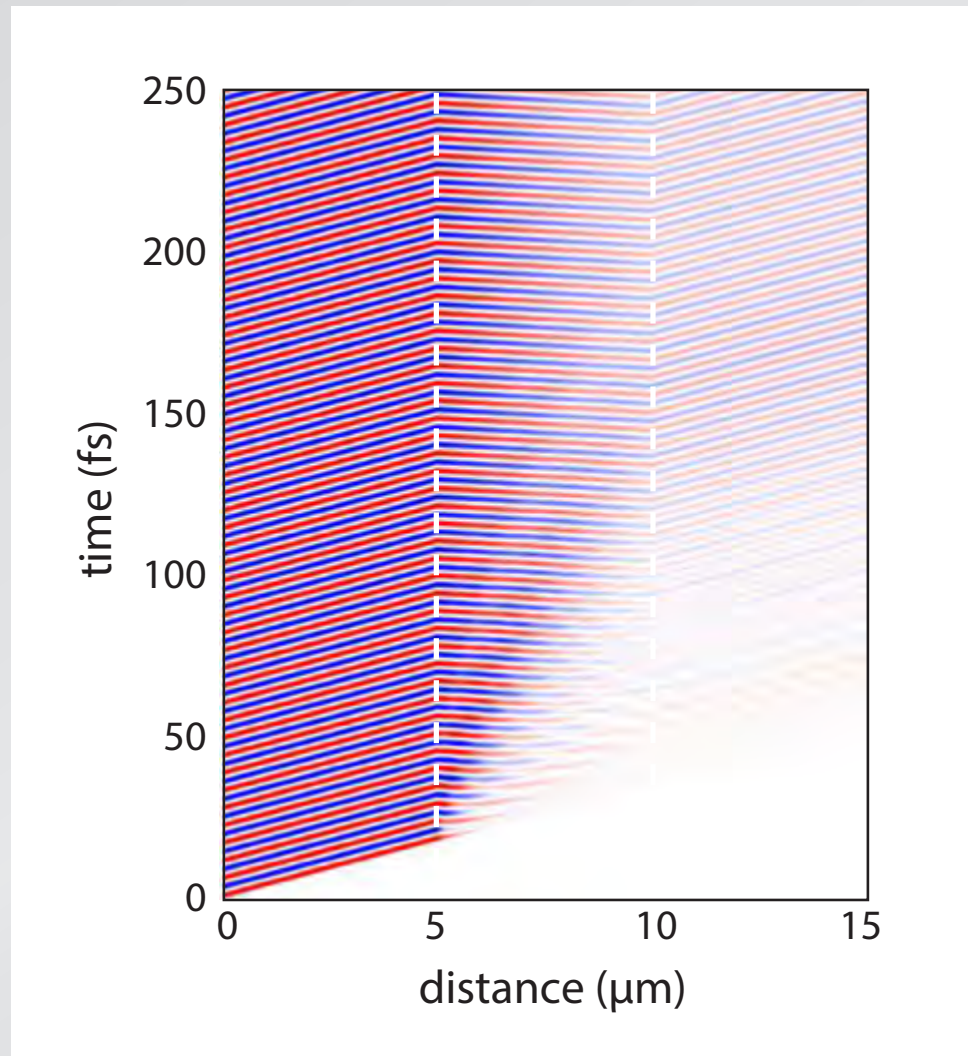
# What about causality?



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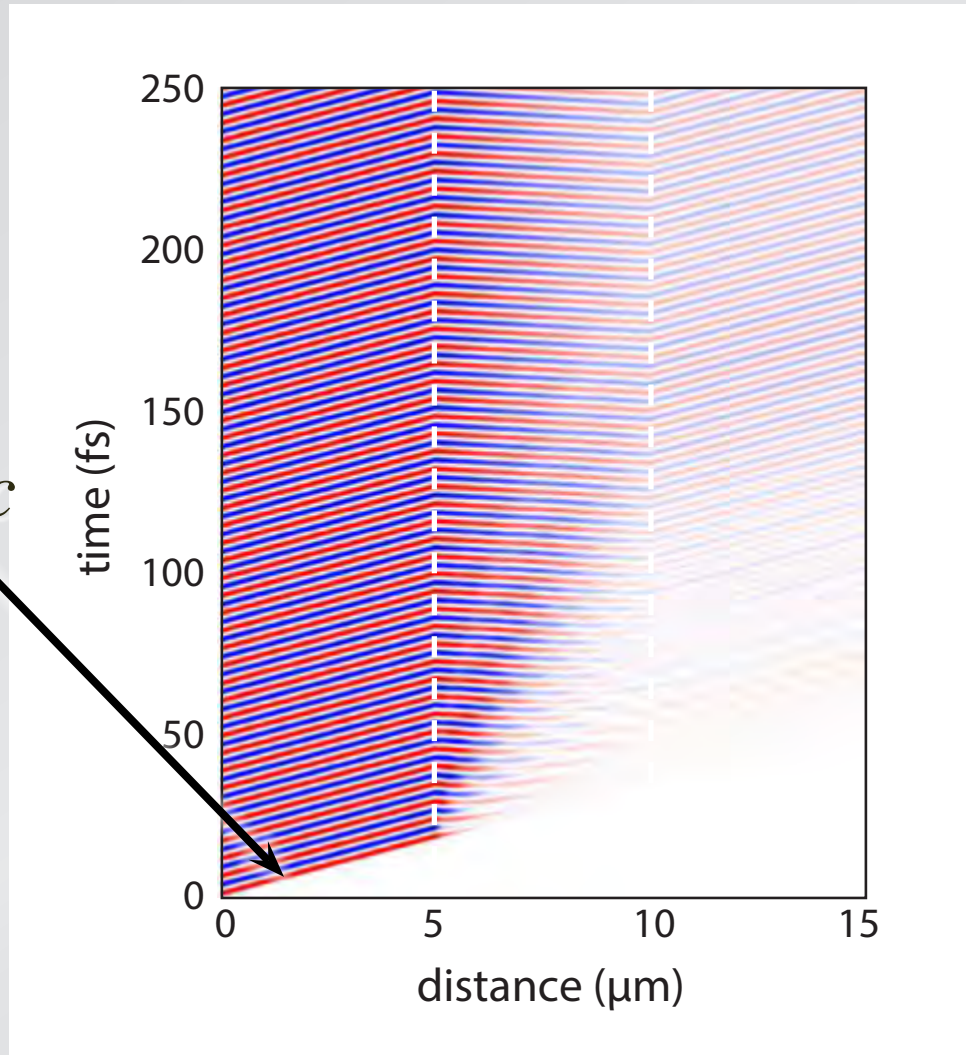
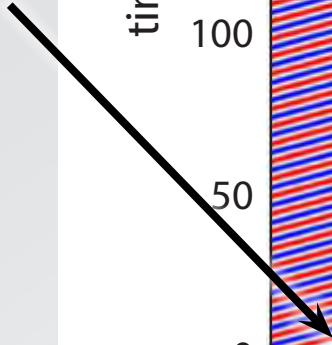


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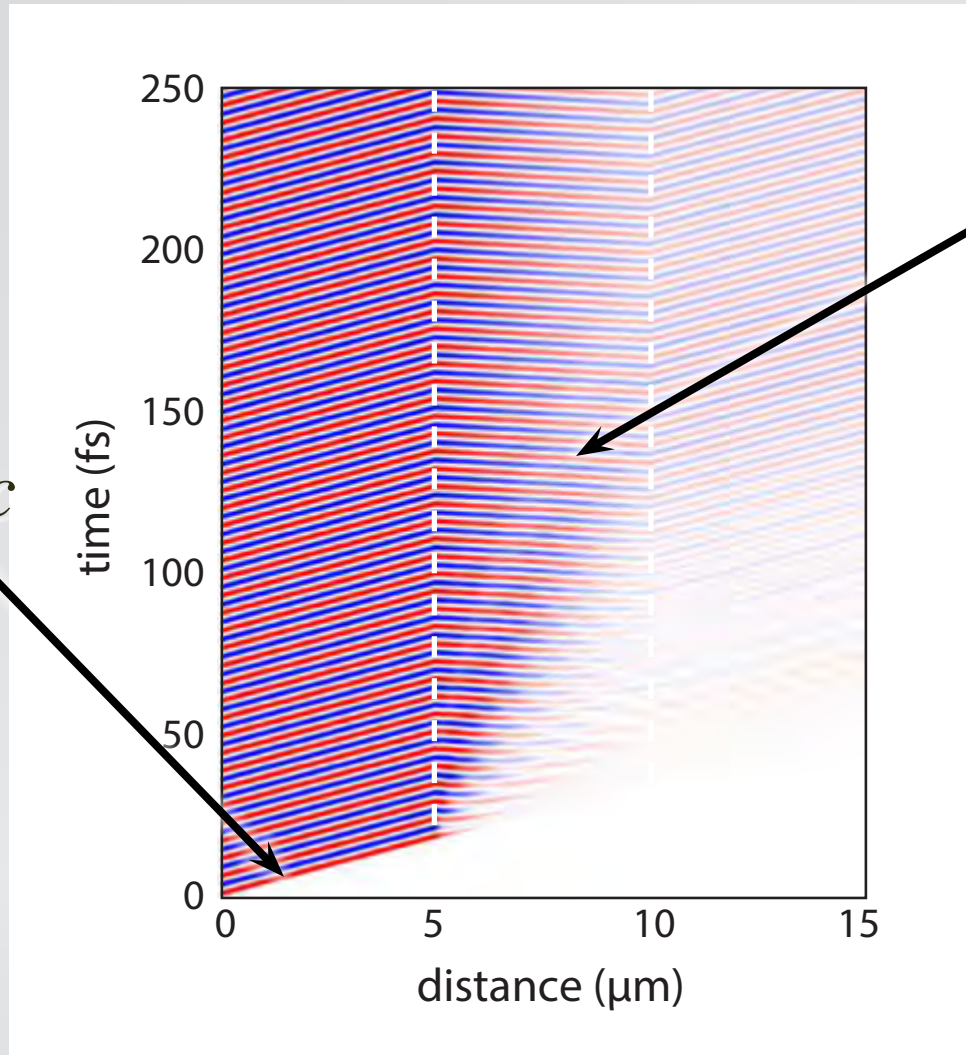
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speed of light  $c$



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reverse phase propagation

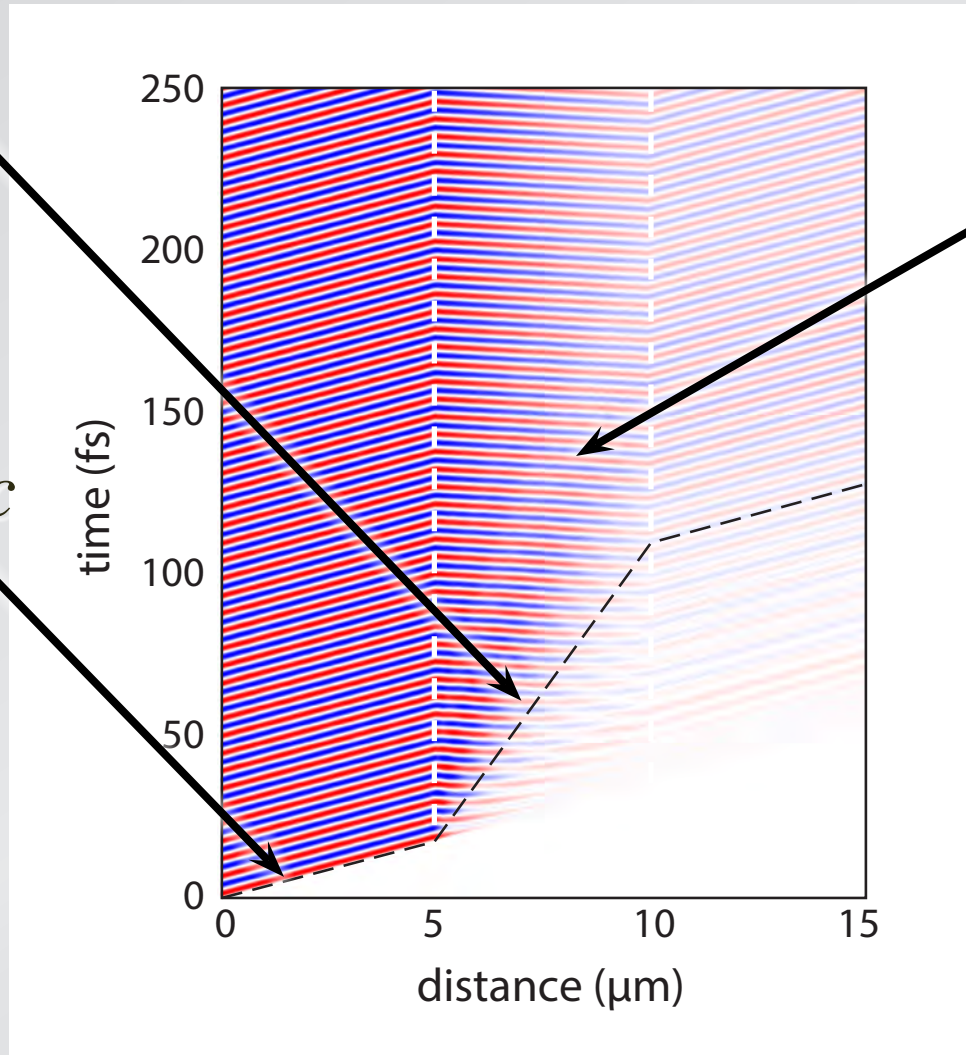


# What about causality?

group velocity

$$v_g < c$$

speed of light  $c$



reverse phase propagation

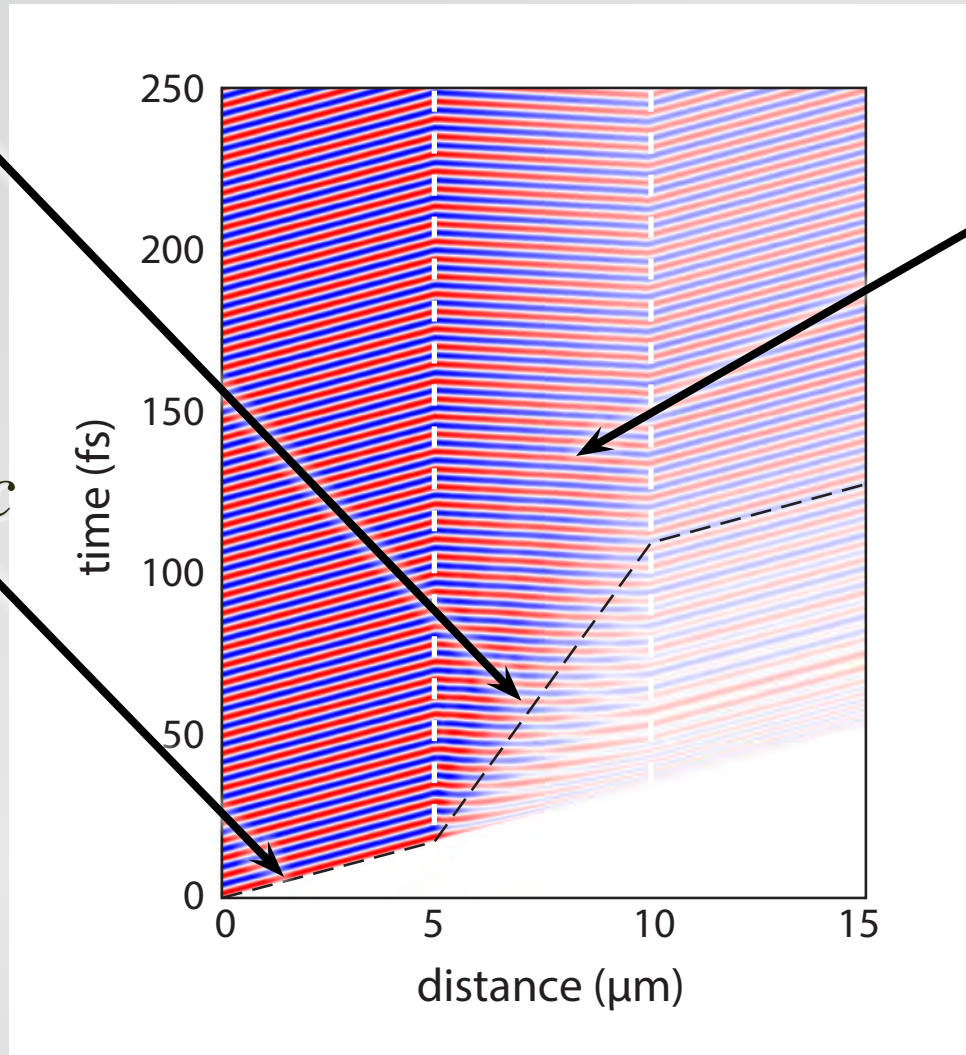


# What about causality?

group velocity

$$v_g < c$$

speed of light  $c$



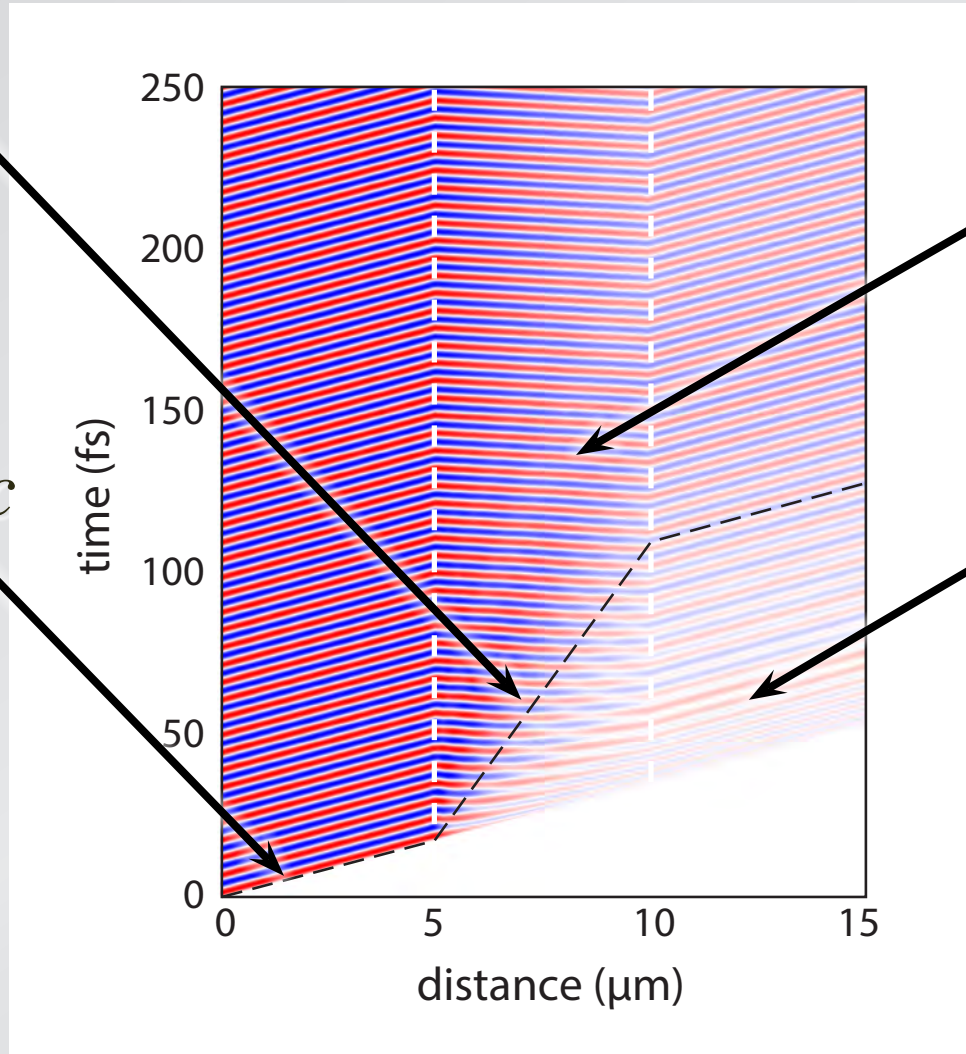
reverse phase propagation

# What about causality?

group velocity

$$v_g < c$$

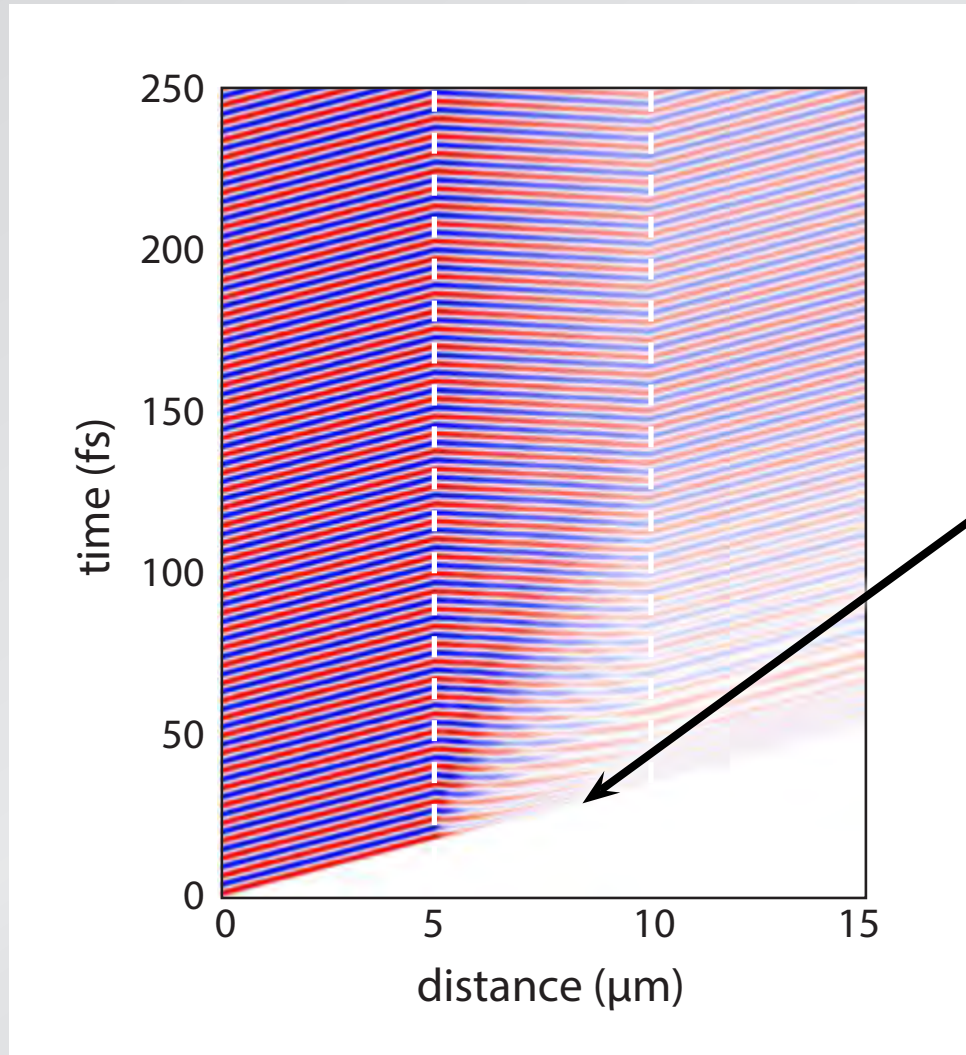
speed of light  $c$



reverse phase propagation

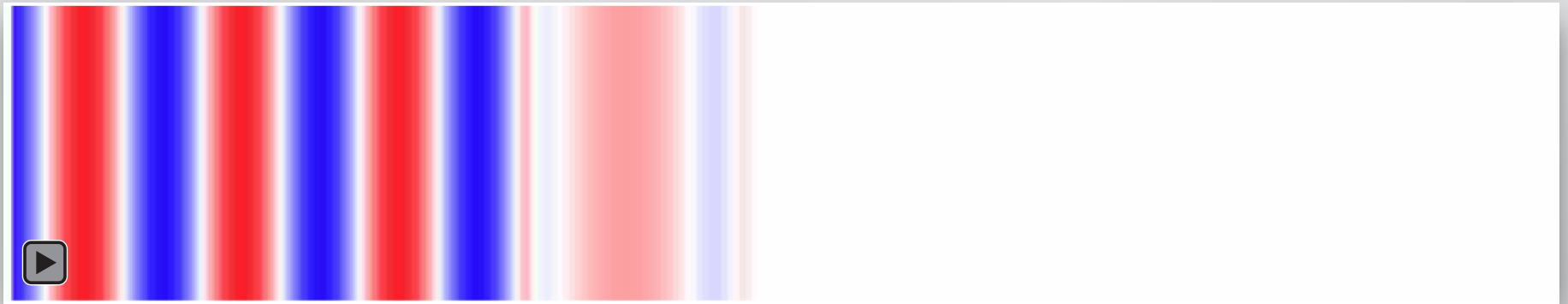
high-frequency precursors

# What about causality?

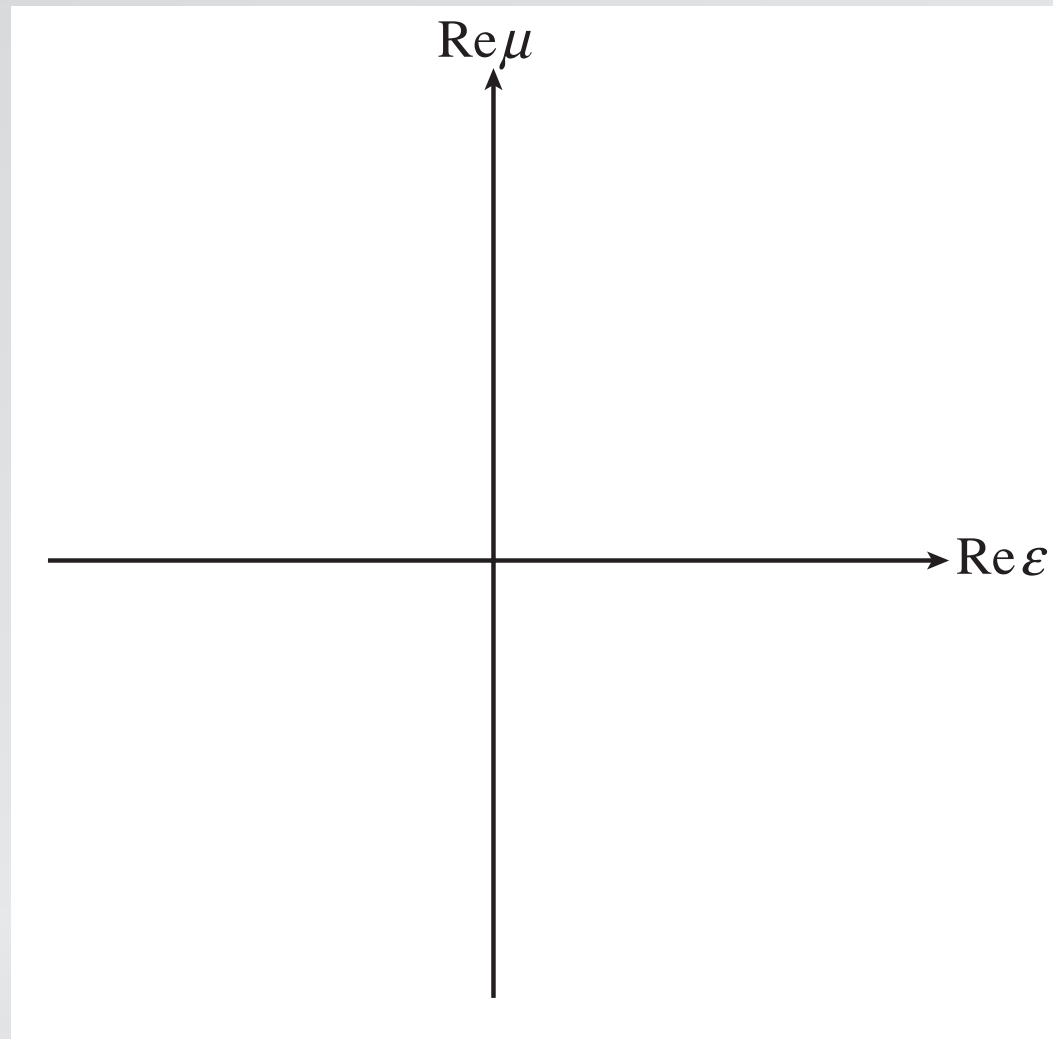


signal *always*  
travels at speed  $c$ !

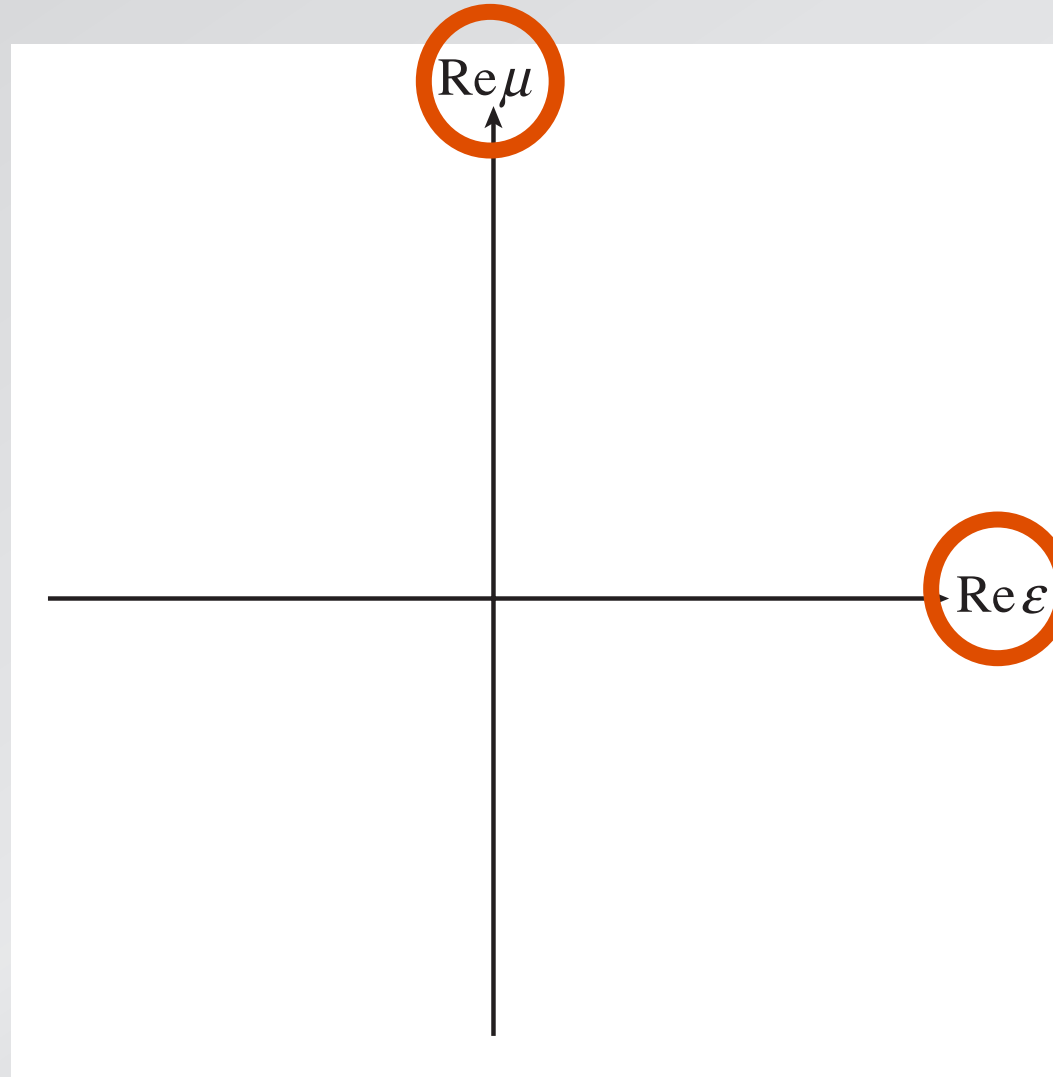
# What about causality?



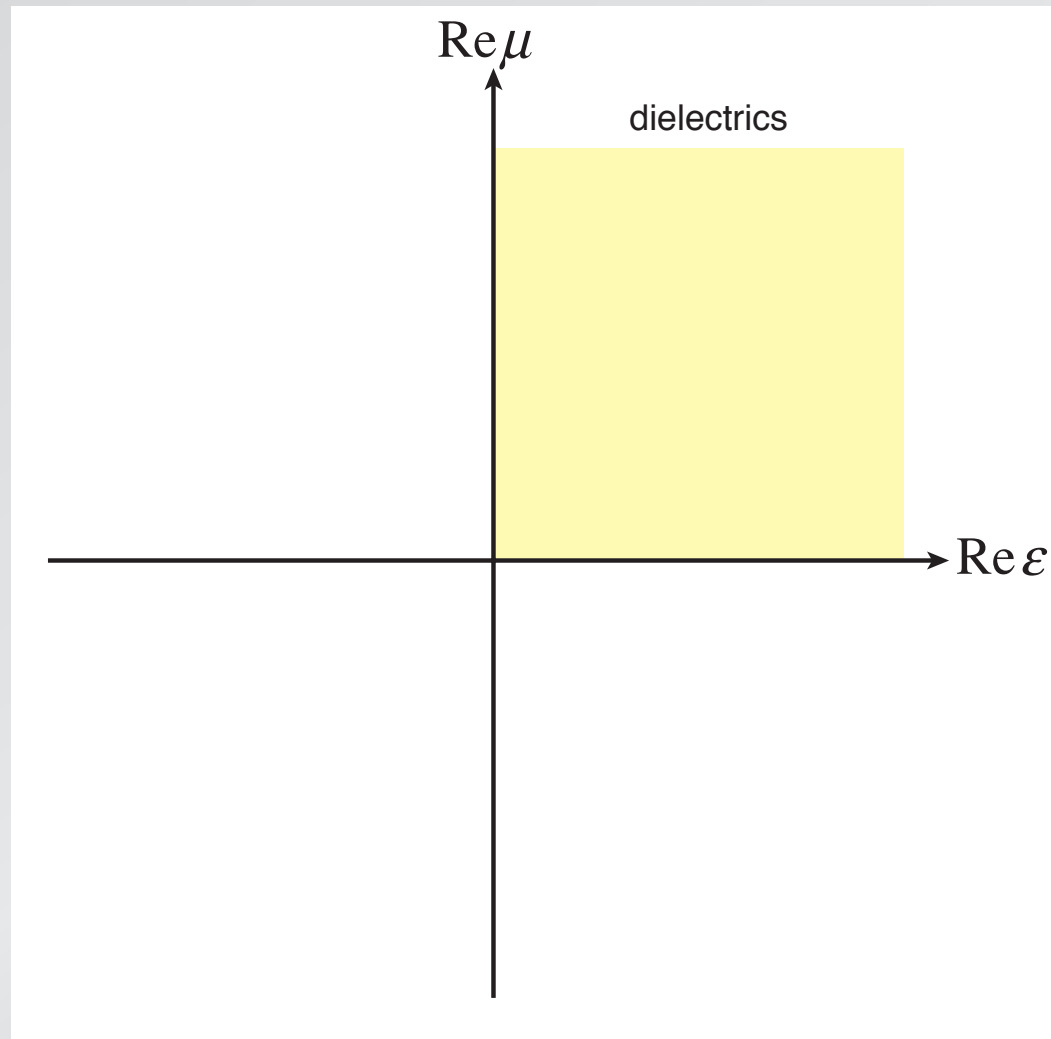
## classification of (non-lossy) materials



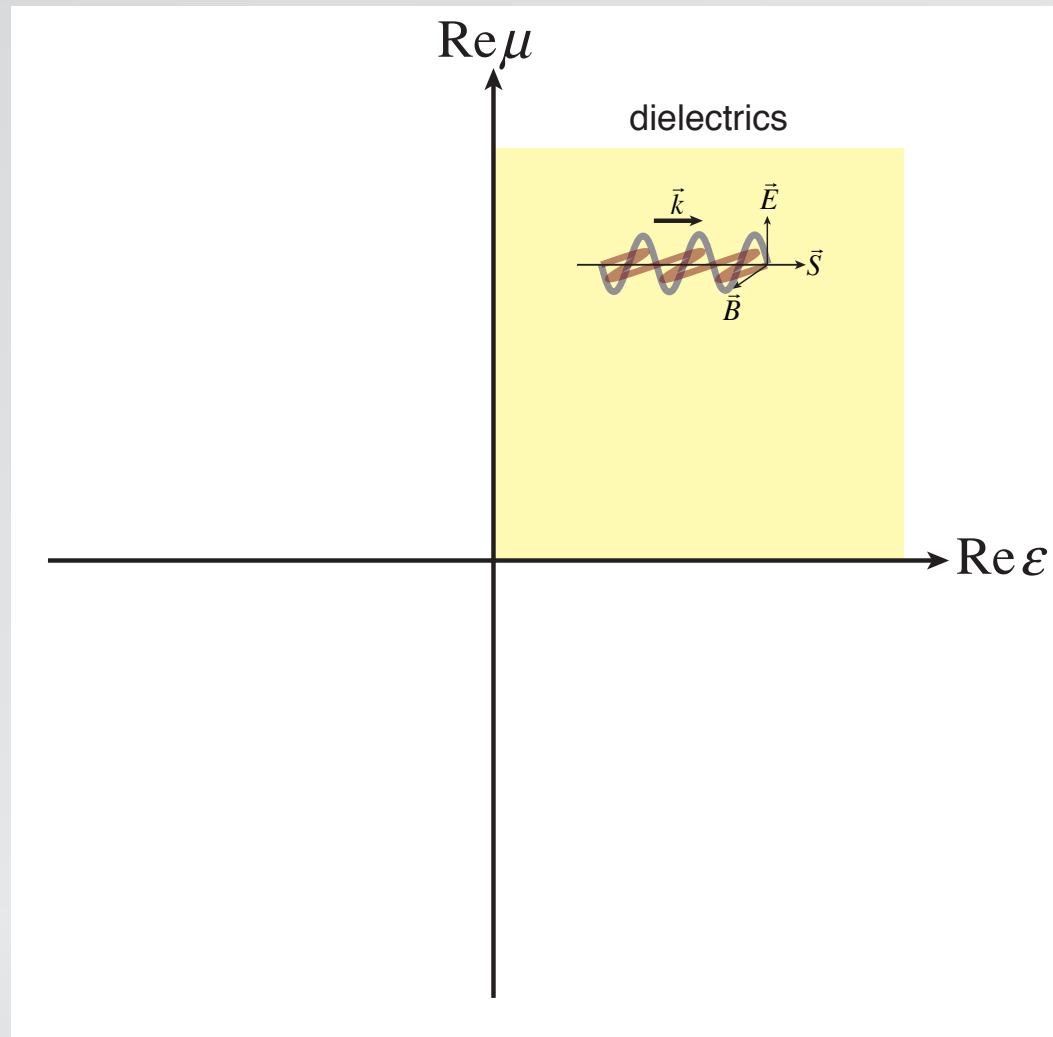
## classification of (non-lossy) materials



# classification of (non-lossy) materials

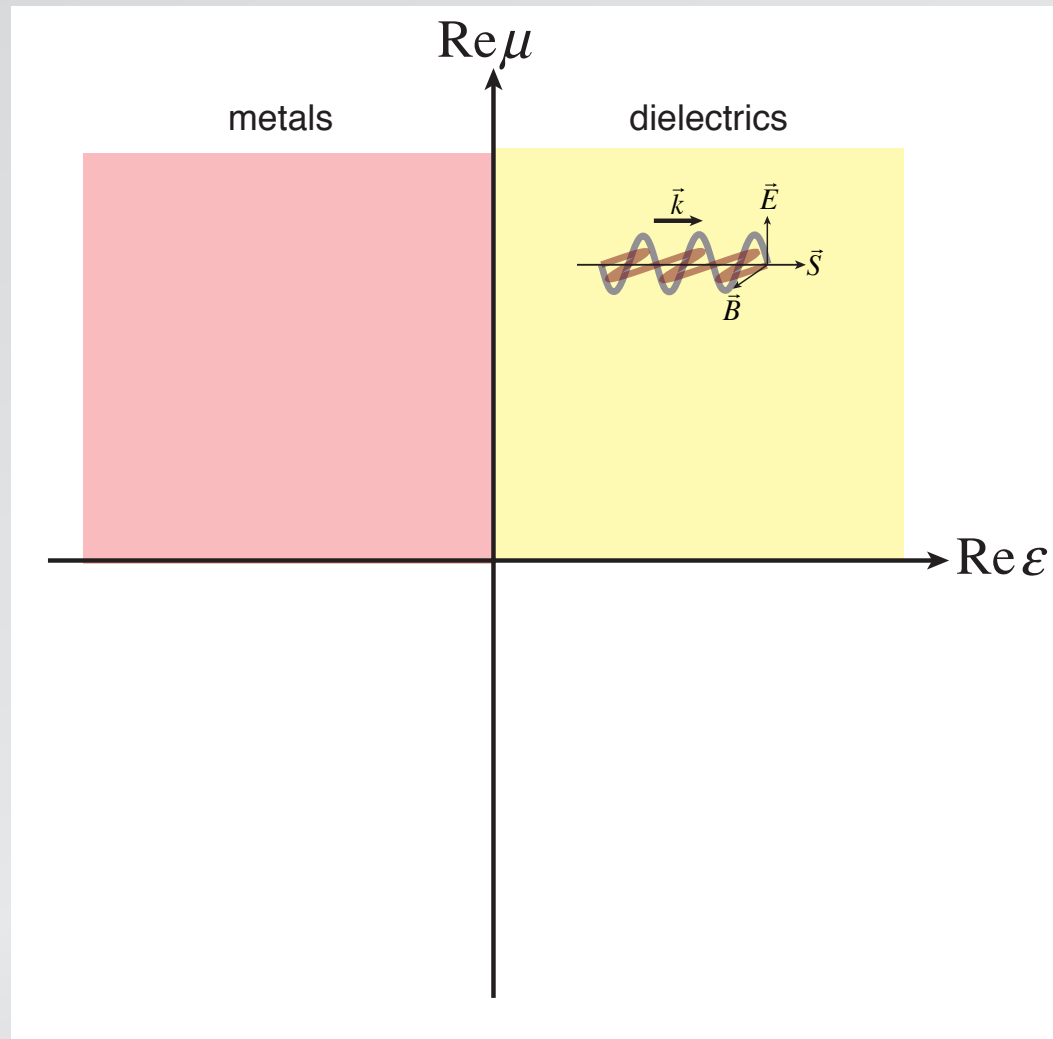


# classification of (non-lossy) materials

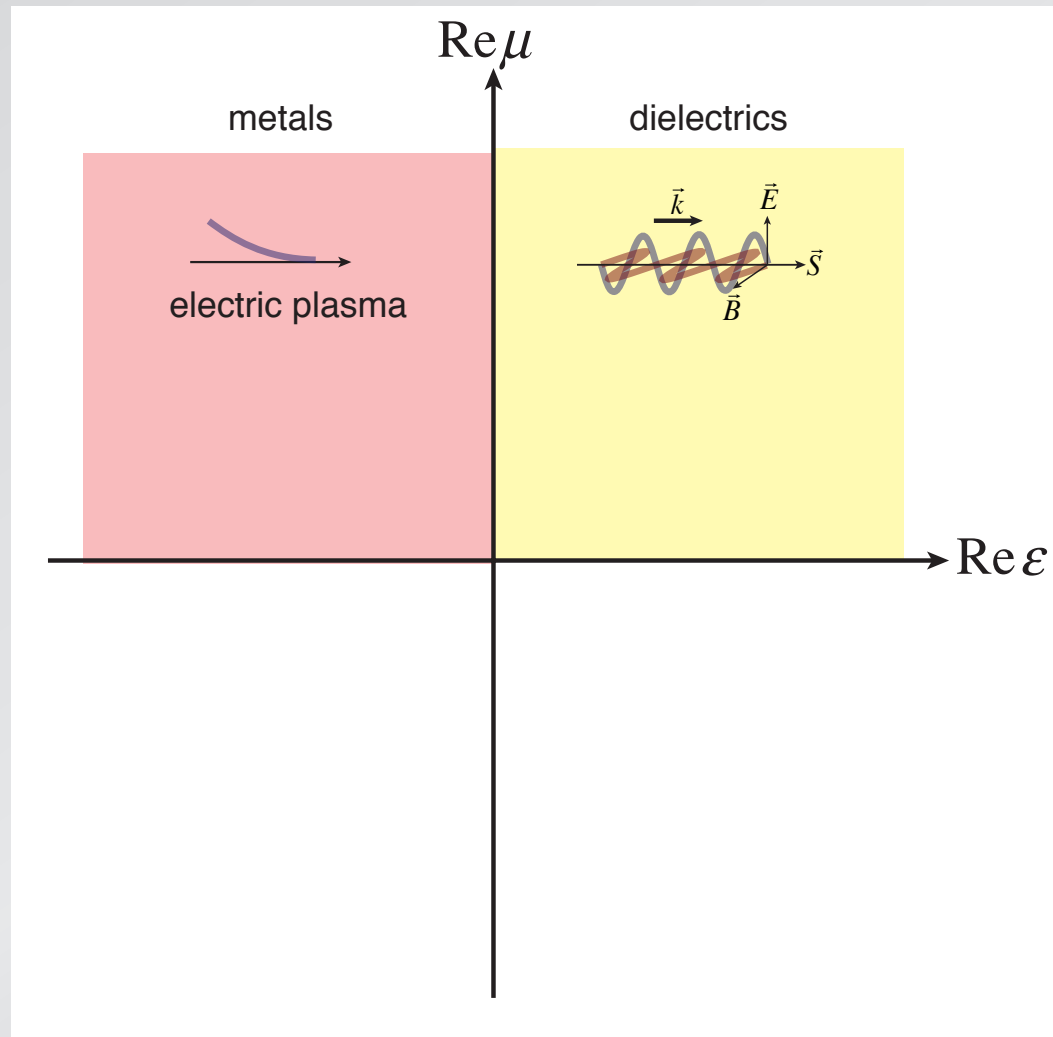




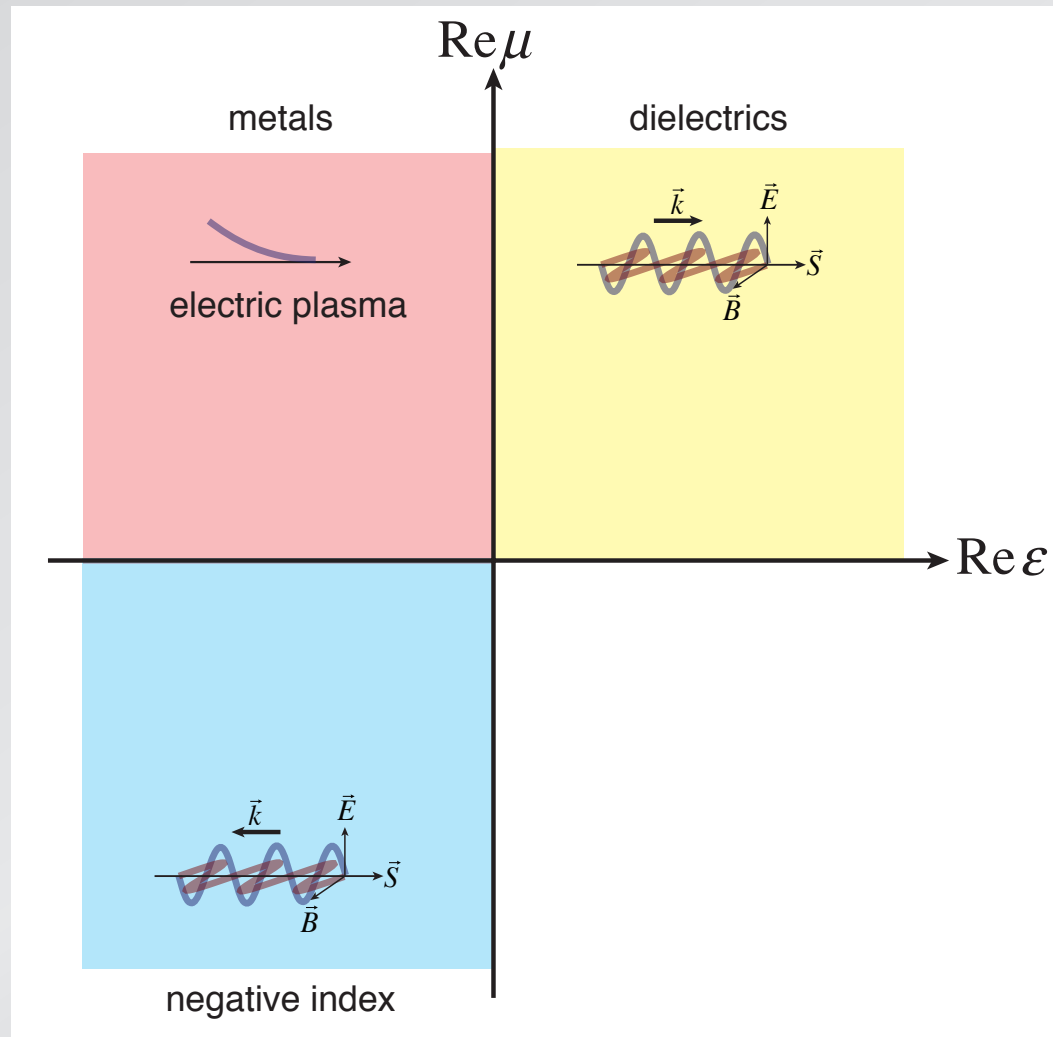
# classification of (non-lossy) materials



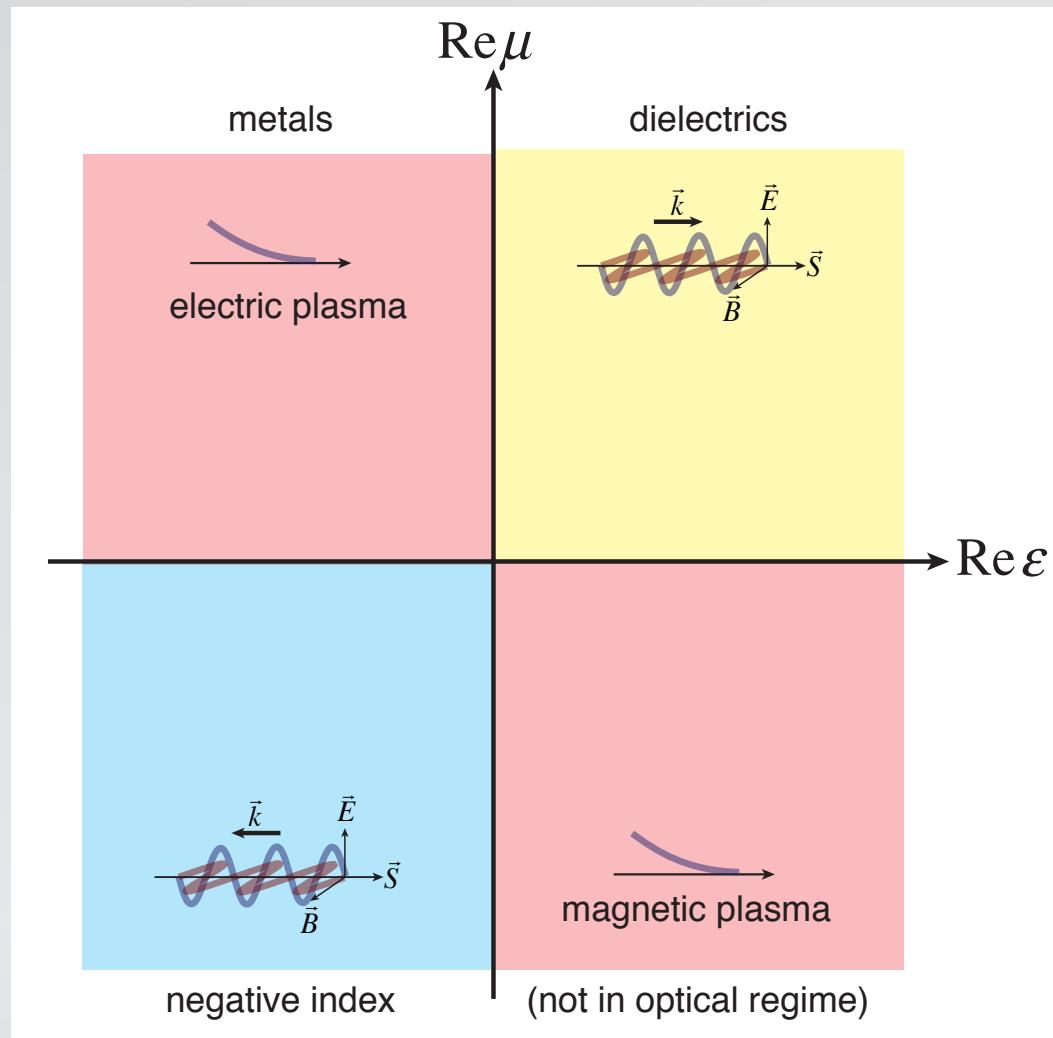
# classification of (non-lossy) materials



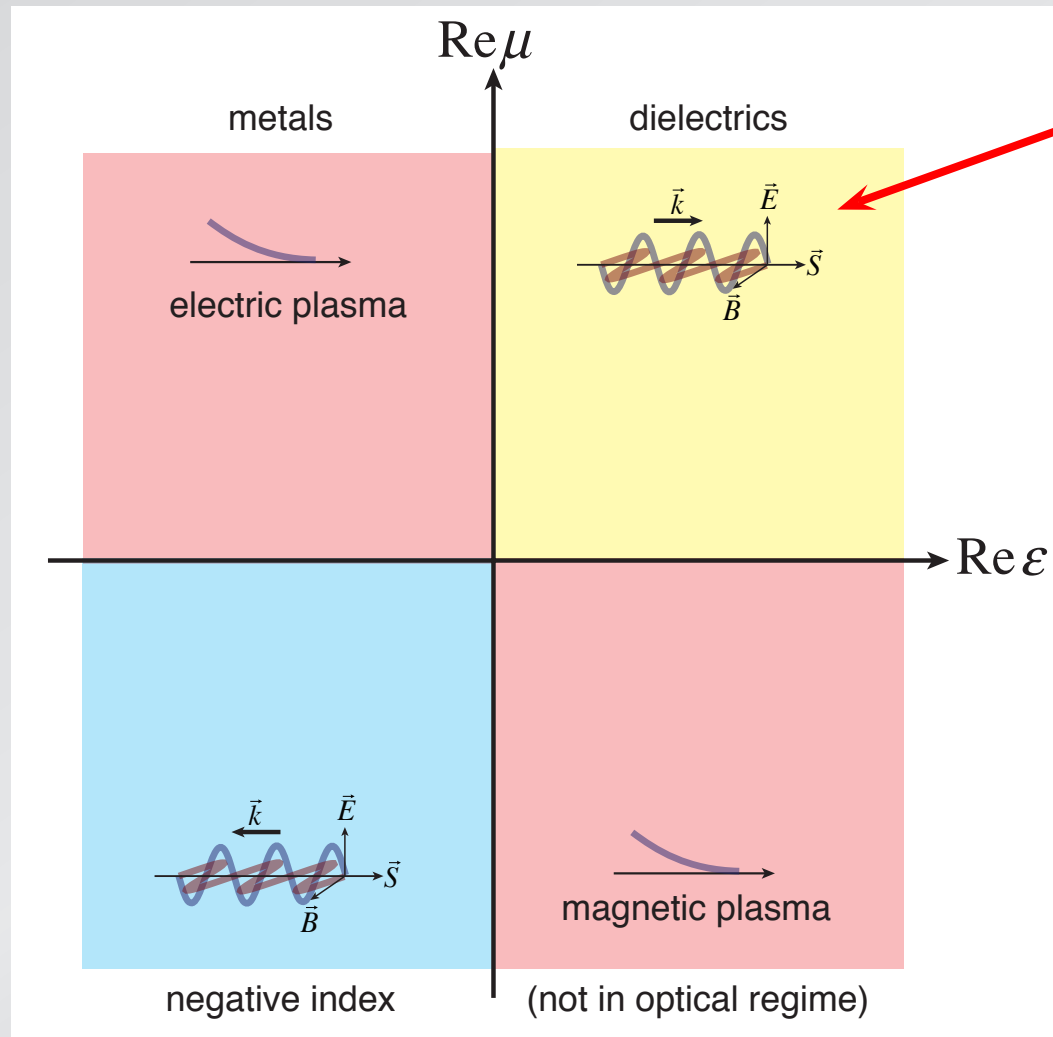
# classification of (non-lossy) materials



# classification of (non-lossy) materials



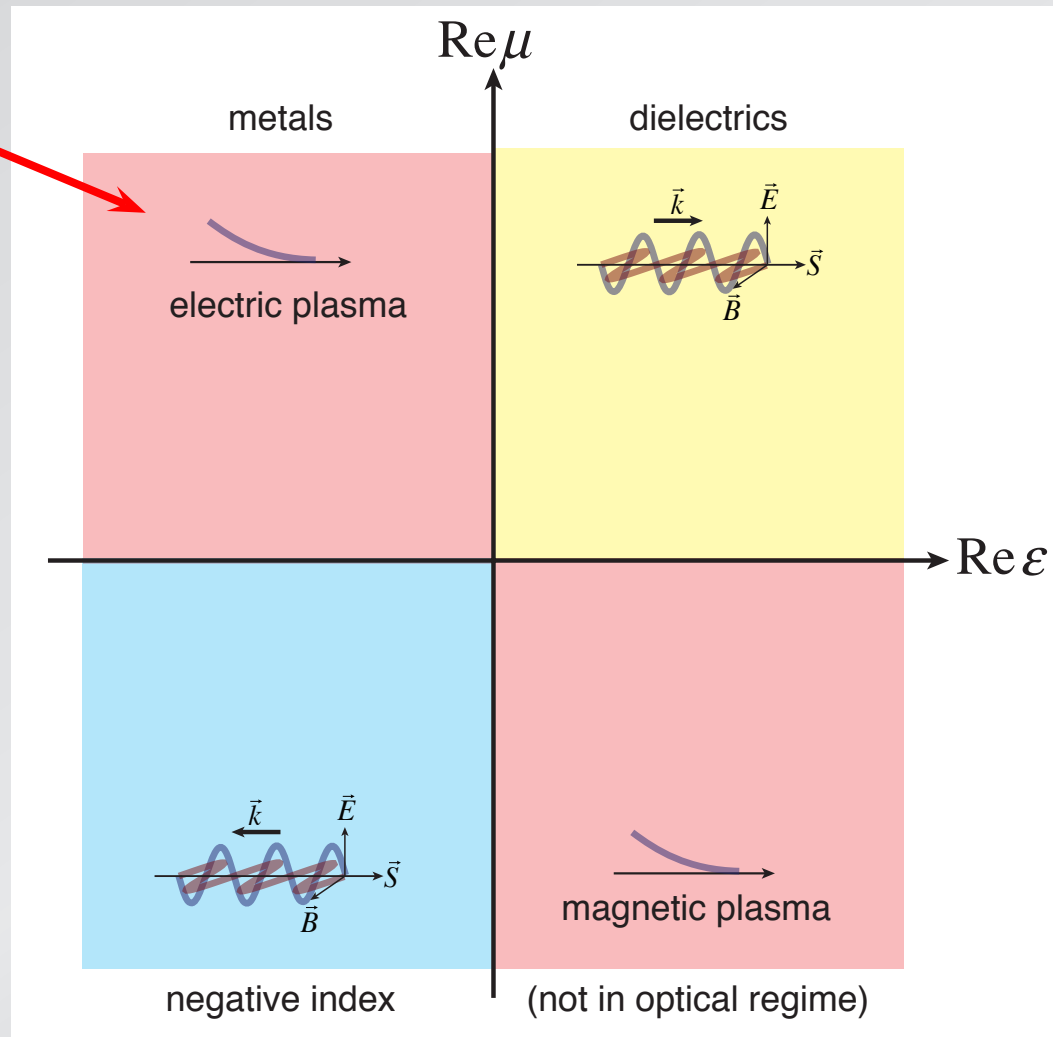
# classification of (non-lossy) materials



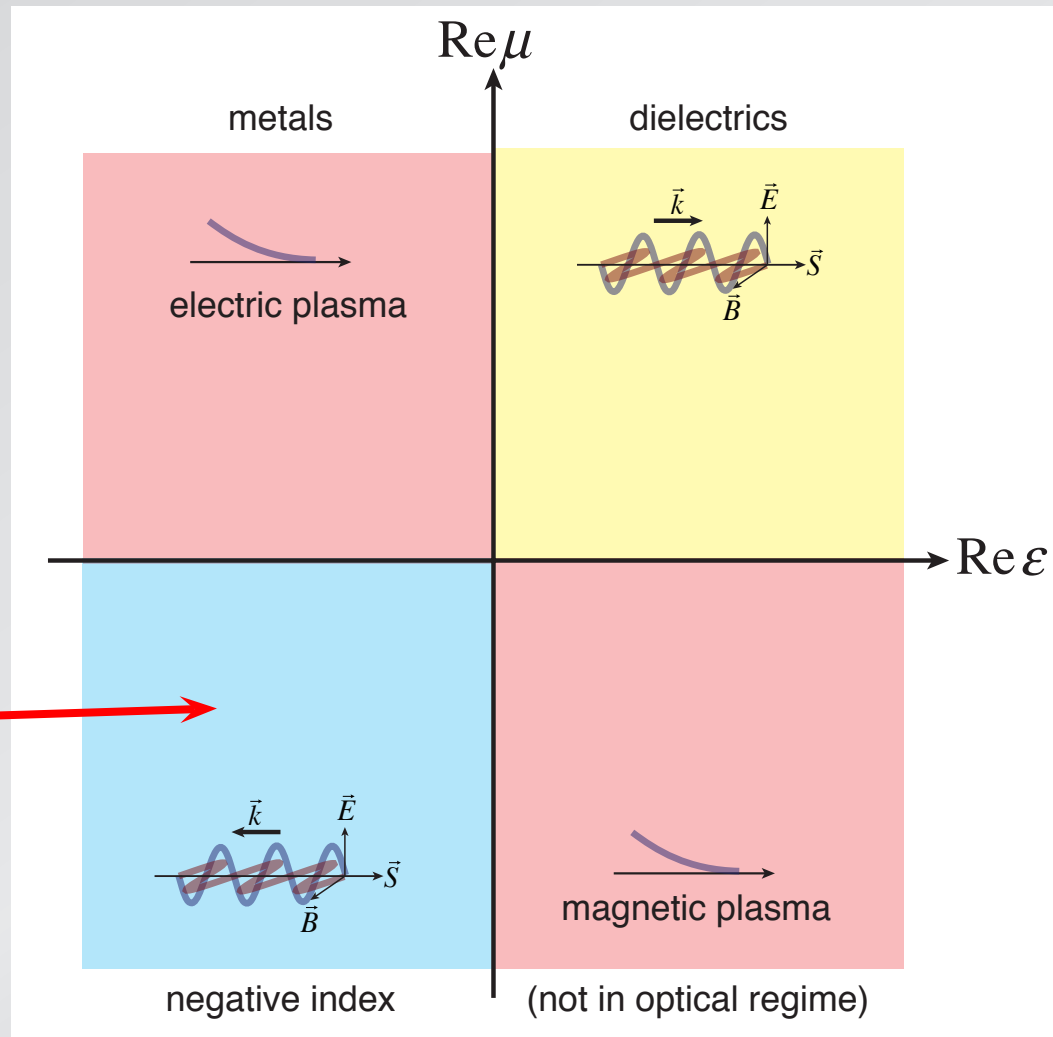
limited by diffraction

# classification of (non-lossy) materials

no propagation



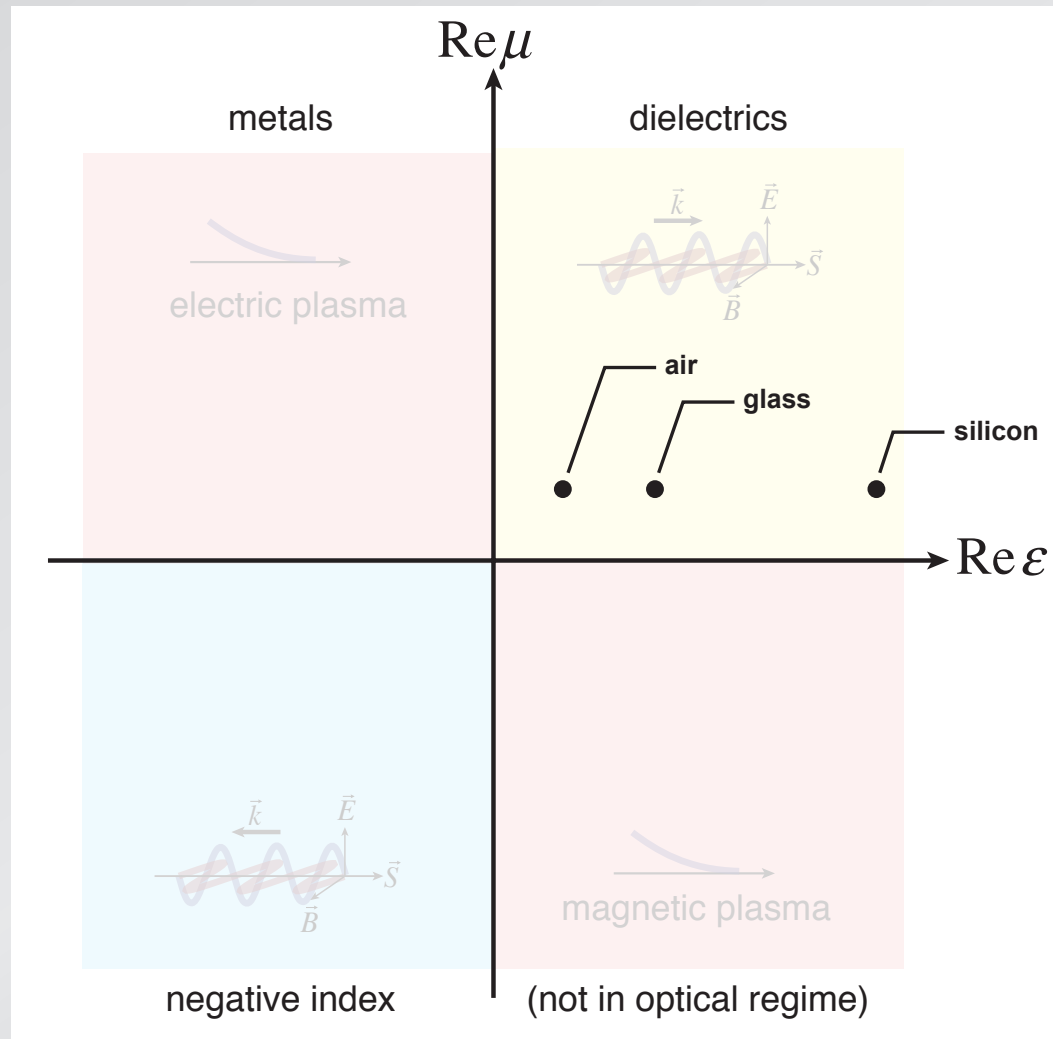
# classification of (non-lossy) materials



superlensing  
but...

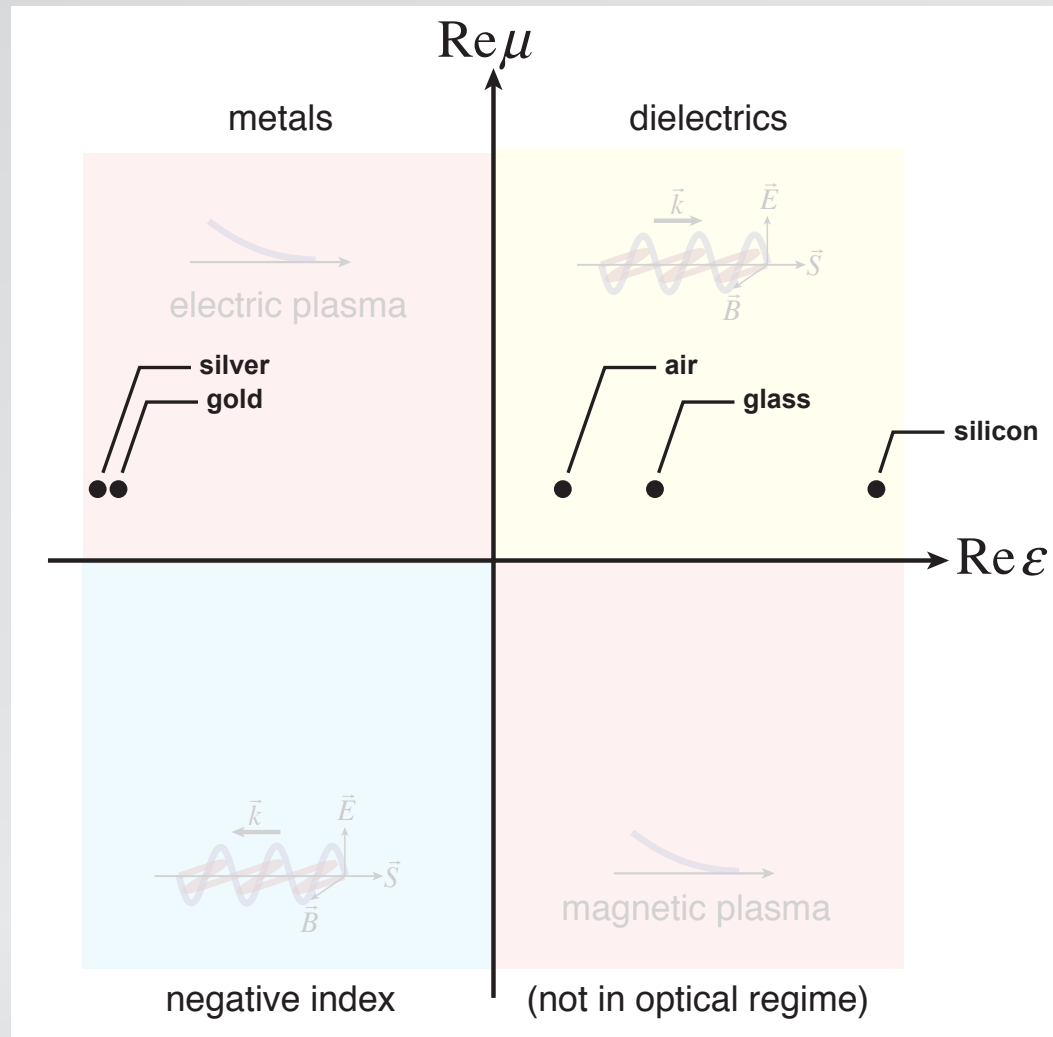


# common materials very limited

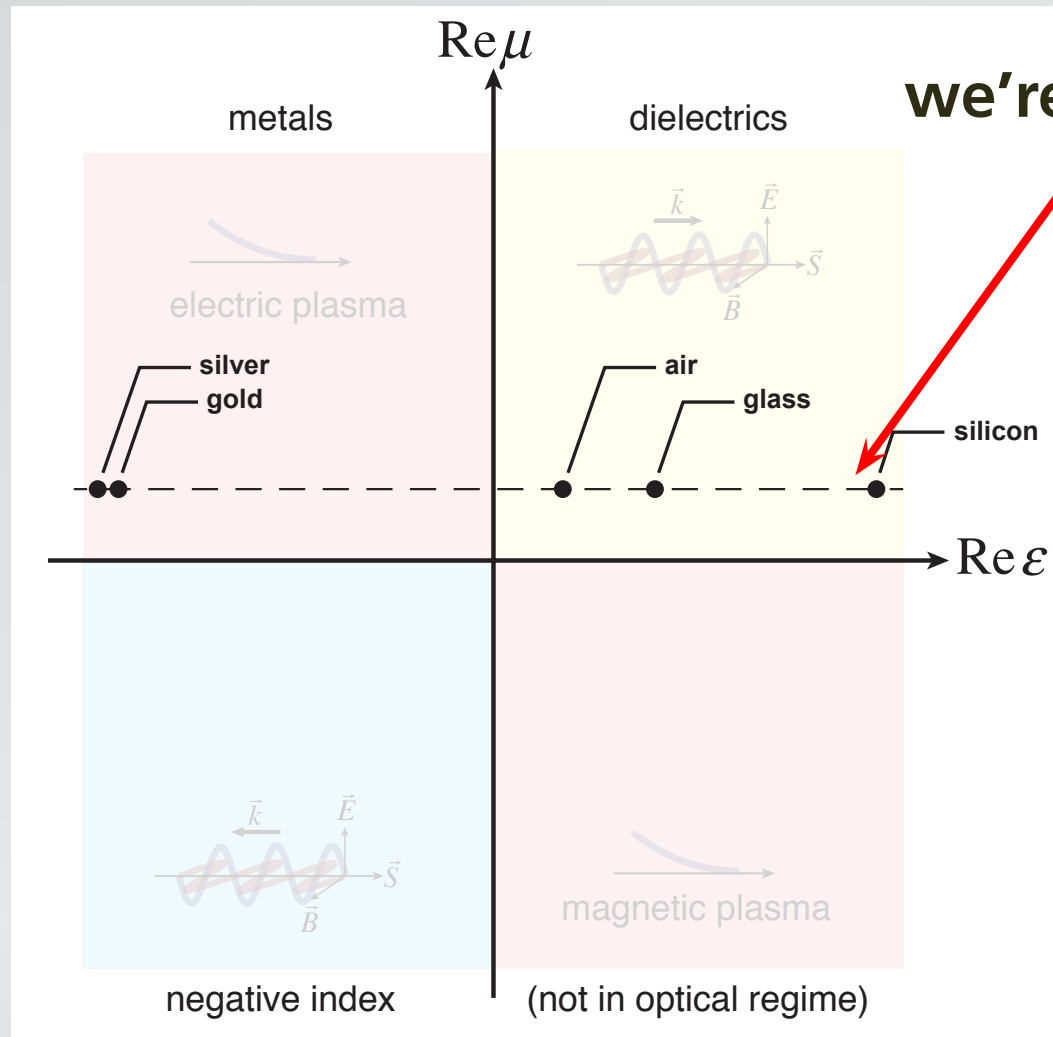




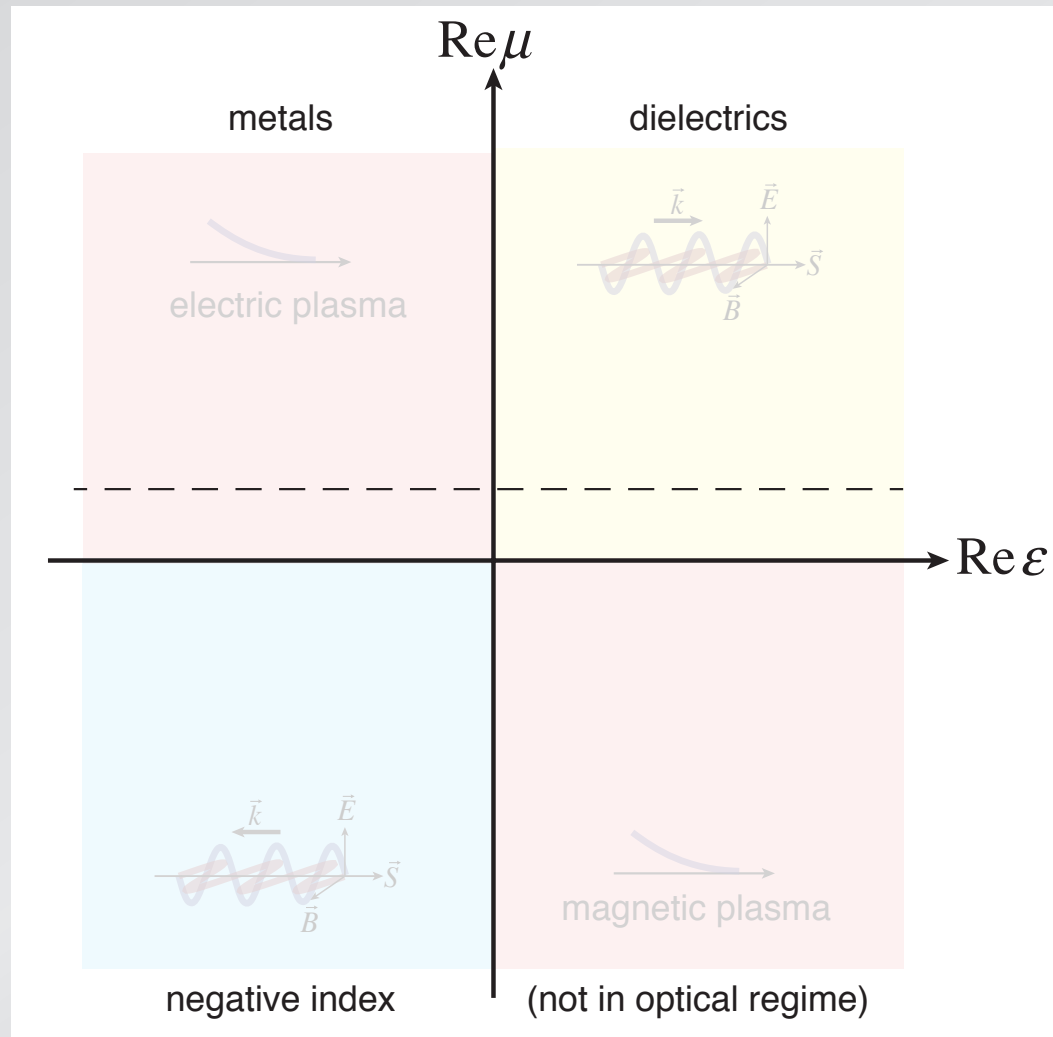
# common materials very limited



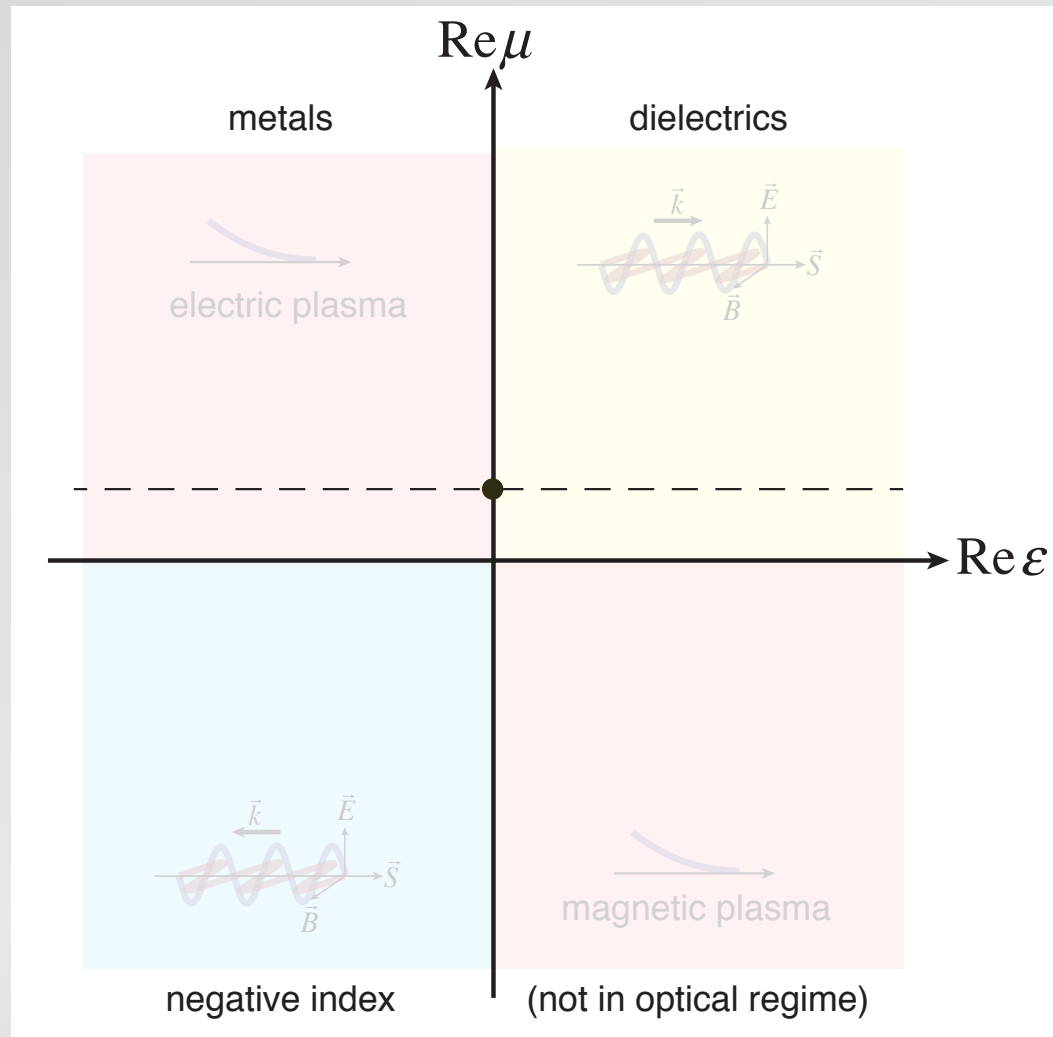
# common materials very limited



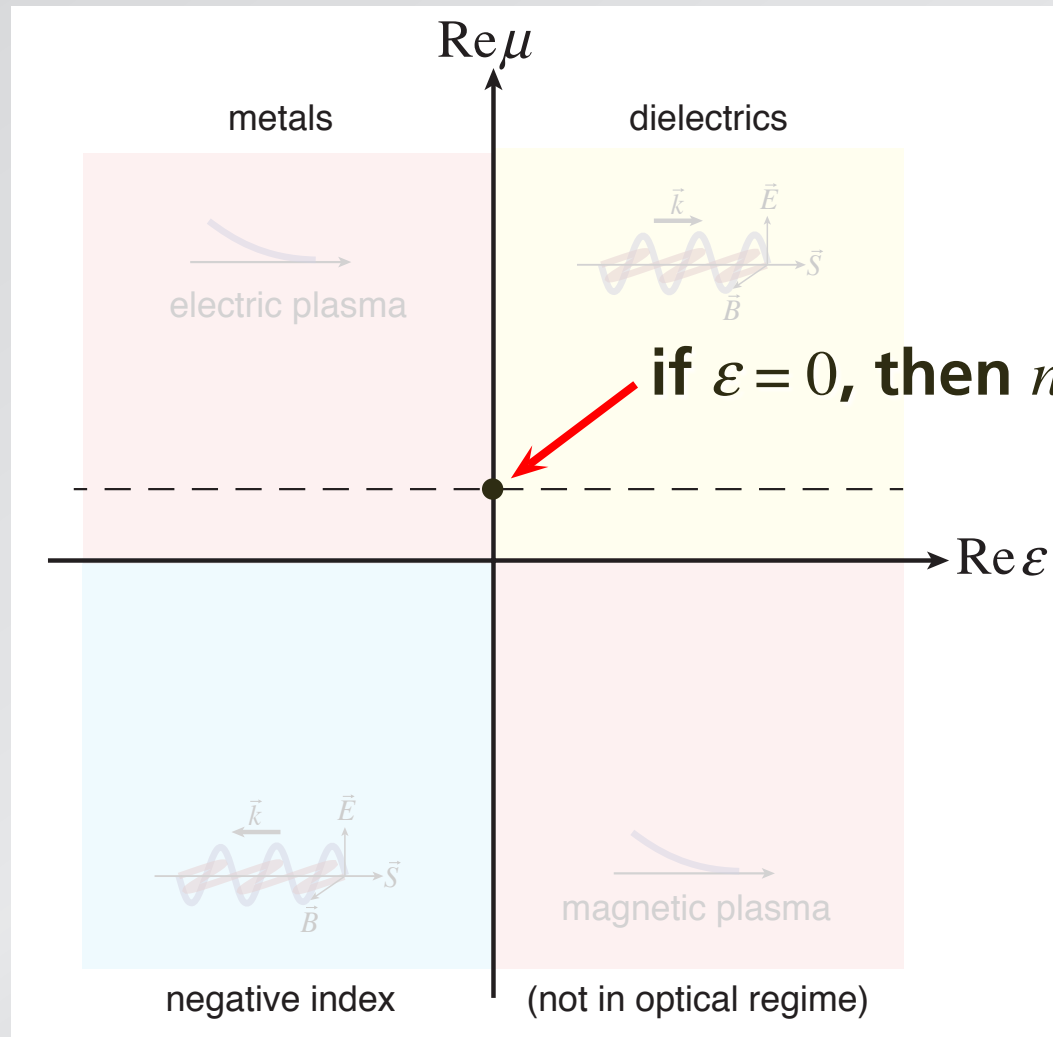
# What happens on the axes?



what if we let  $\varepsilon = 0$ ?



what if we let  $\varepsilon = 0$ ?



**Q: If  $n = 0$ , which of the following is true?**

- 1. the frequency goes to zero.**
- 2. the phase velocity becomes infinite.**
- 3. both of the above.**
- 4. neither of the above.**

## wave equation

$$\nabla^2 \vec{E} - \frac{\mu\epsilon}{c^2} \frac{\partial^2 \vec{E}}{\partial t^2} = 0$$

## solution

$$\vec{E} = \vec{E}_0 e^{i(kx - \omega t)}$$

## where

$$\frac{\omega}{k} = \frac{1}{\sqrt{\epsilon\mu}} c = \frac{1}{n} c$$

wave equation

$$\nabla^2 \vec{E} - \frac{\mu \epsilon}{c^2} \frac{\partial^2 \vec{E}}{\partial t^2} = 0$$

solution

$$\vec{E} = \vec{E}_0 e^{i(kx - \omega t)}$$

where

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wave equation

$$\nabla^2 \vec{E} - \frac{\mu \epsilon}{c^2} \frac{\partial^2 \vec{E}}{\partial t^2} = 0$$

solution

$$\vec{E} = \vec{E}_0 e^{i(kx - \omega t)} \longrightarrow \vec{E} = \vec{E}_0 e^{-i\omega t}$$

where

$$\frac{\omega}{k} = \frac{1}{\sqrt{\epsilon\mu}} c = \frac{1}{n} c$$

wave equation

$$\nabla^2 \vec{E} - \frac{\mu \epsilon}{c^2} \frac{\partial^2 \vec{E}}{\partial t^2} = 0$$

solution

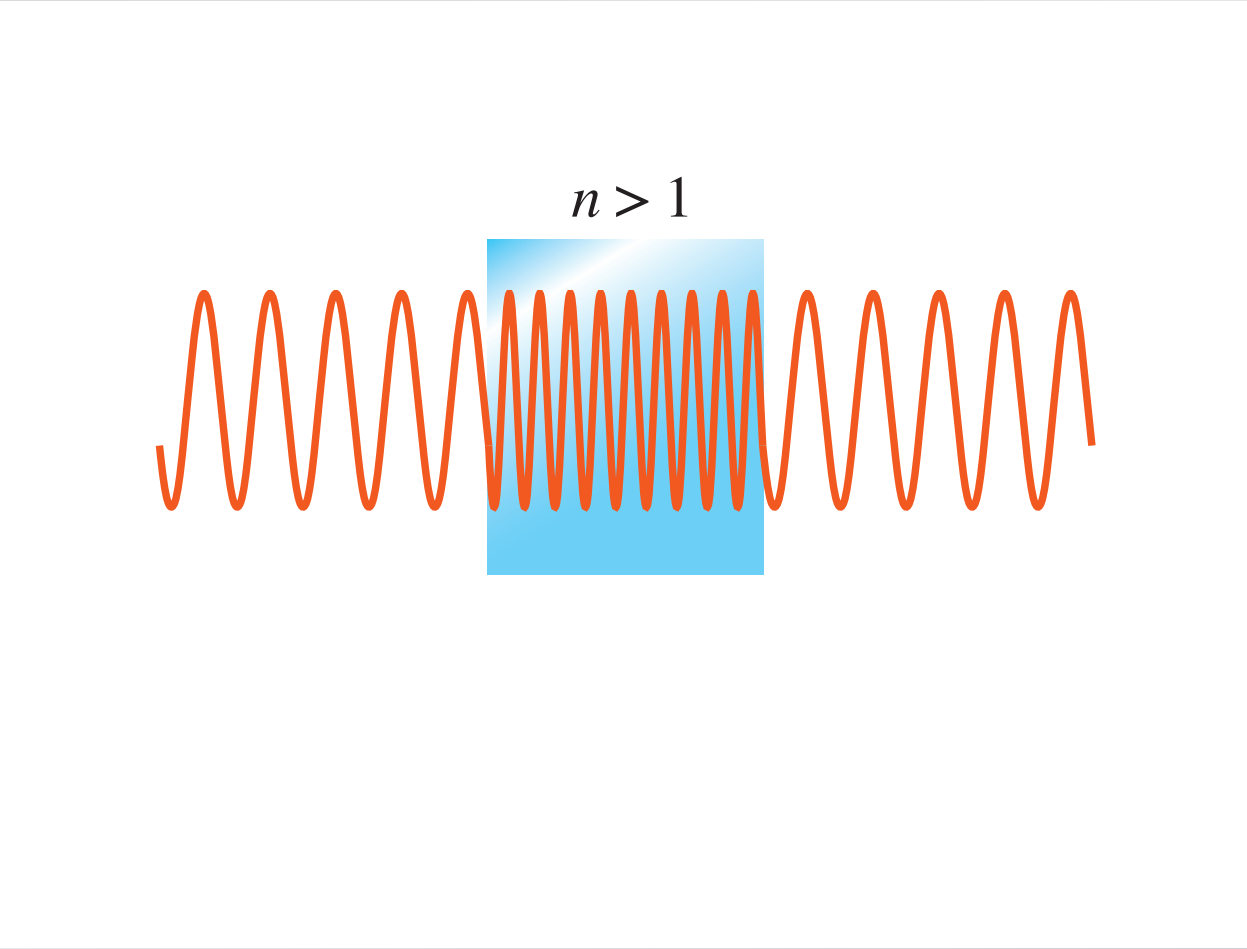
$$\vec{E} = \vec{E}_0 e^{i(kx - \omega t)} \longrightarrow \vec{E} = \vec{E}_0 e^{-i\omega t}$$

where

$$\frac{\omega}{k} = \frac{1}{\sqrt{\epsilon\mu}} c = \frac{1}{n} c \longrightarrow \infty$$

**Q: If  $n = 0$ , which of the following is true?**

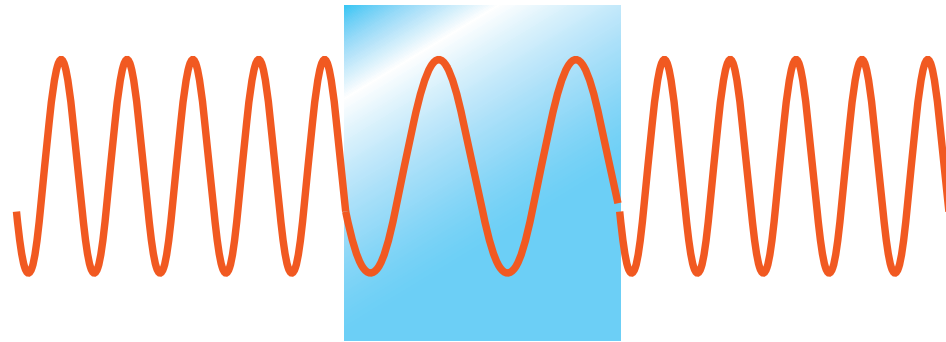
1. the frequency goes to zero.
- 2. the phase velocity becomes infinite. ✓**
3. both of the above.
4. neither of the above.



1 index

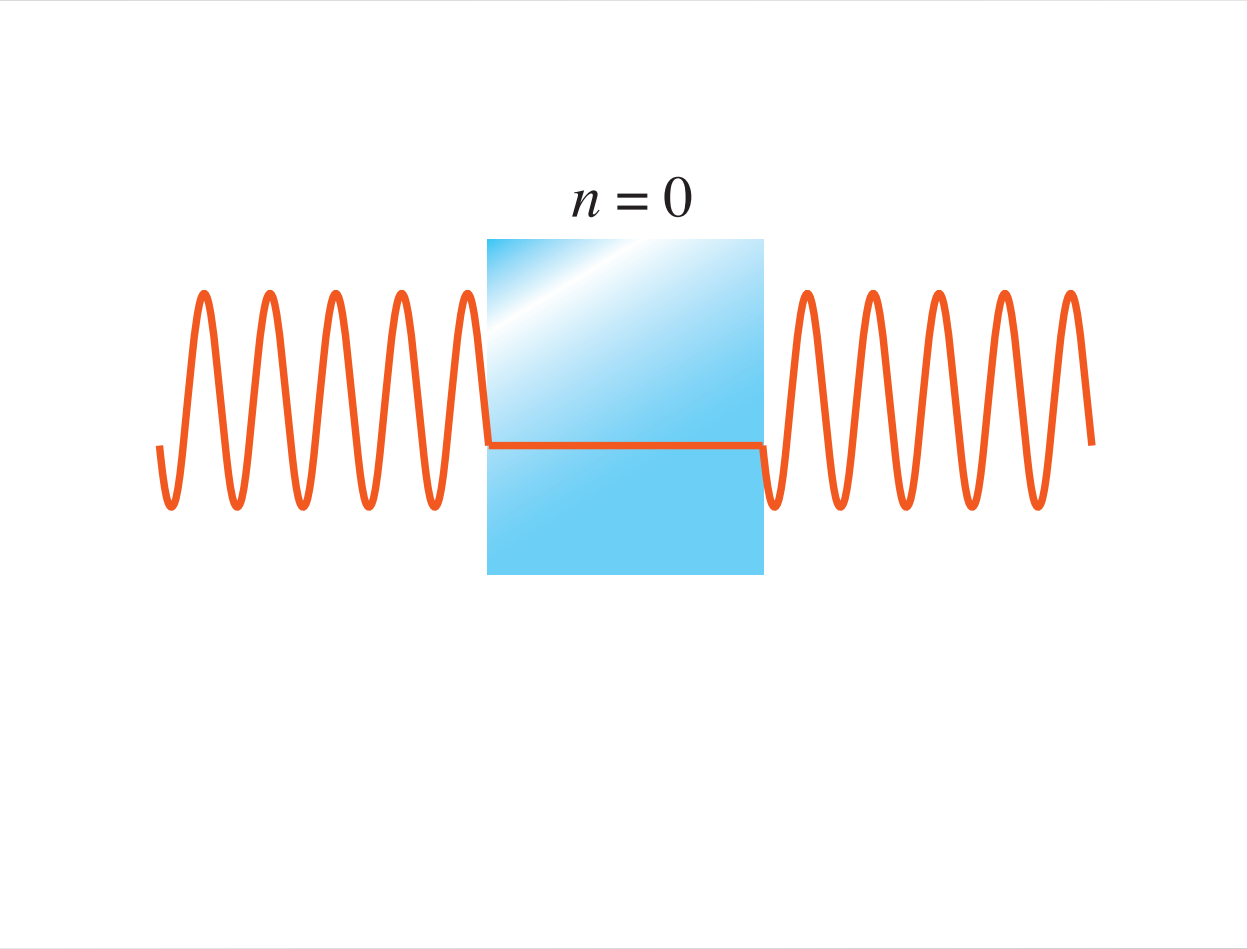
2 zero index

$$0 < n < 1$$



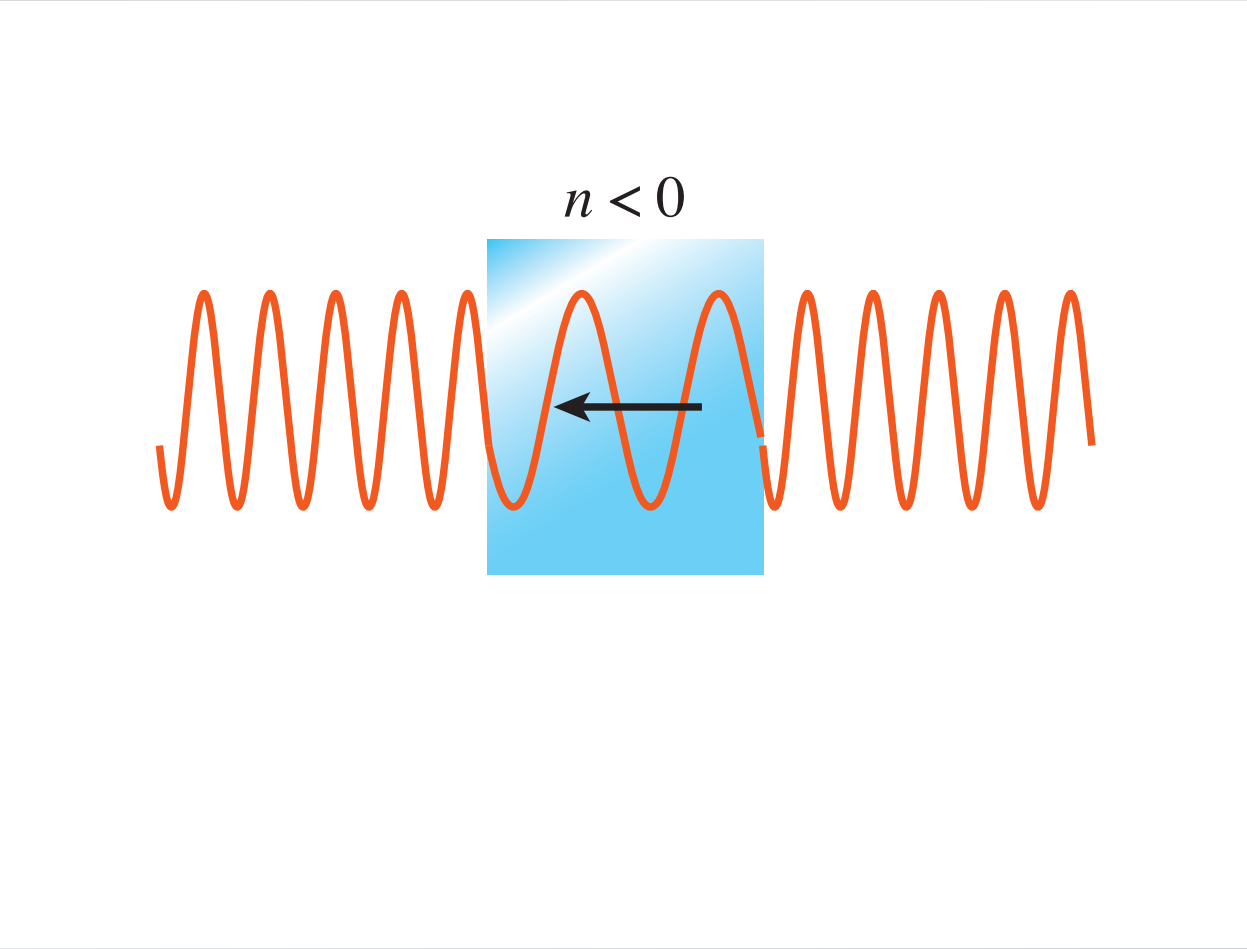
1 index

2 zero index



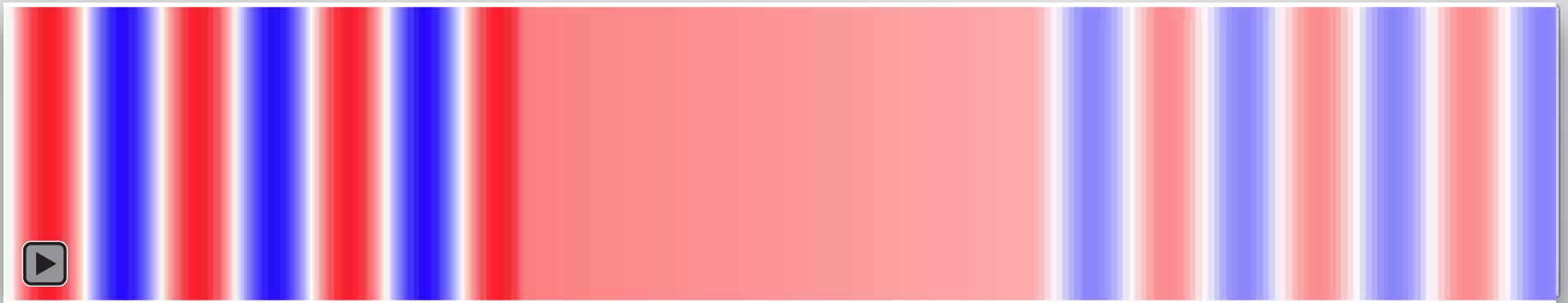
1 index

2 zero index



1 index

2 zero index



1 index

2 zero index

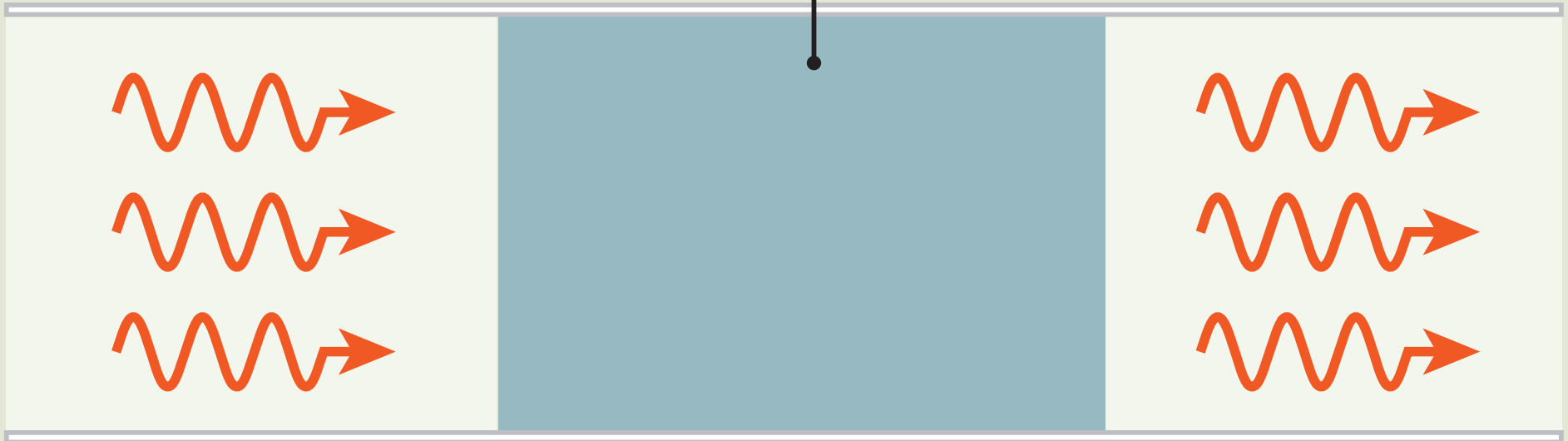


**What can we do with uniform phase?**

**1** index

**2** zero index

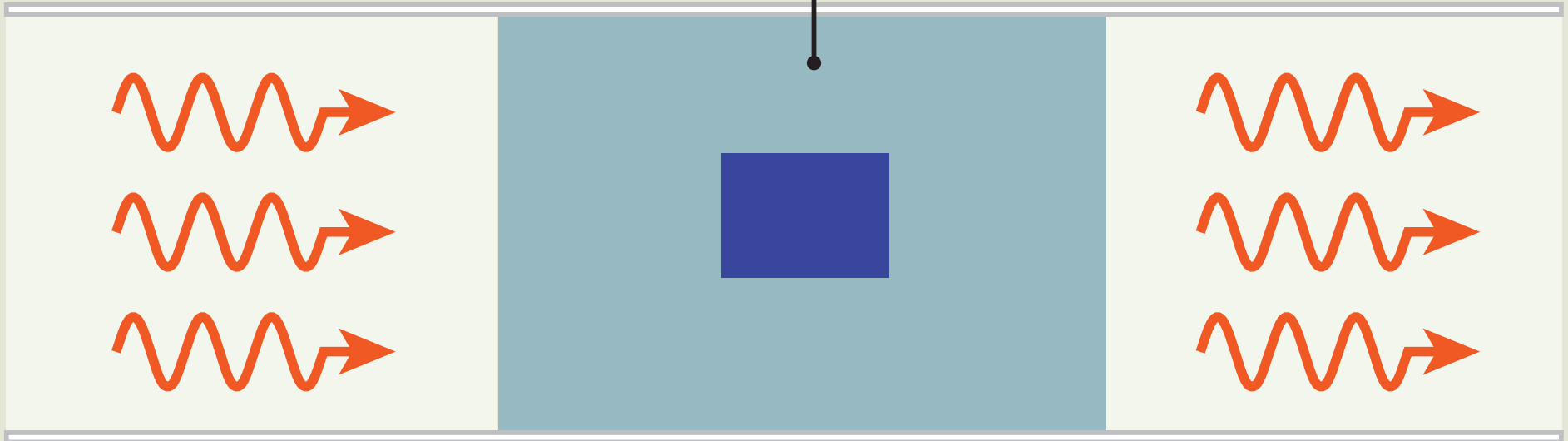
$$n = 0$$



1 index

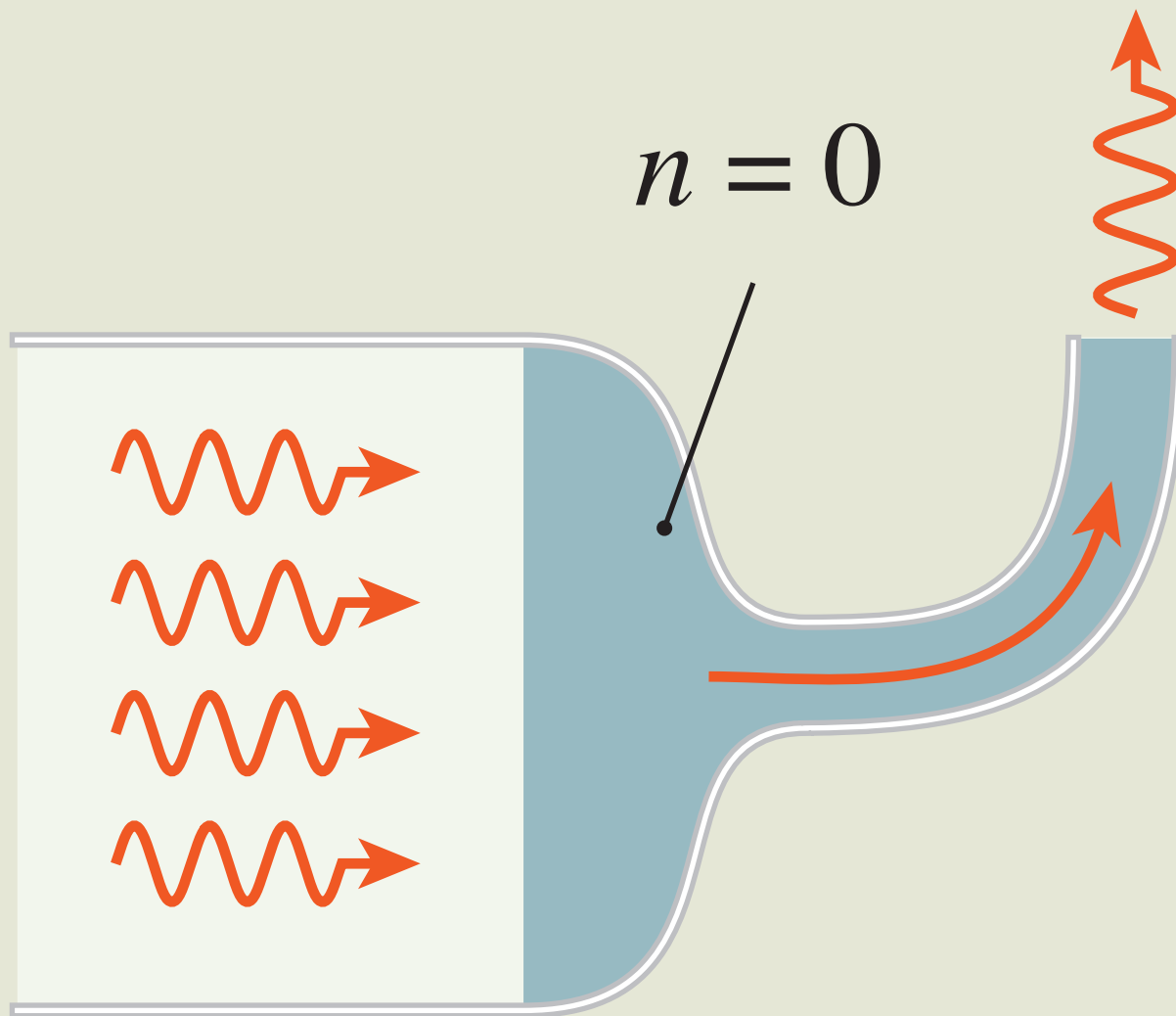
2 zero index

$$n = 0$$



1 index

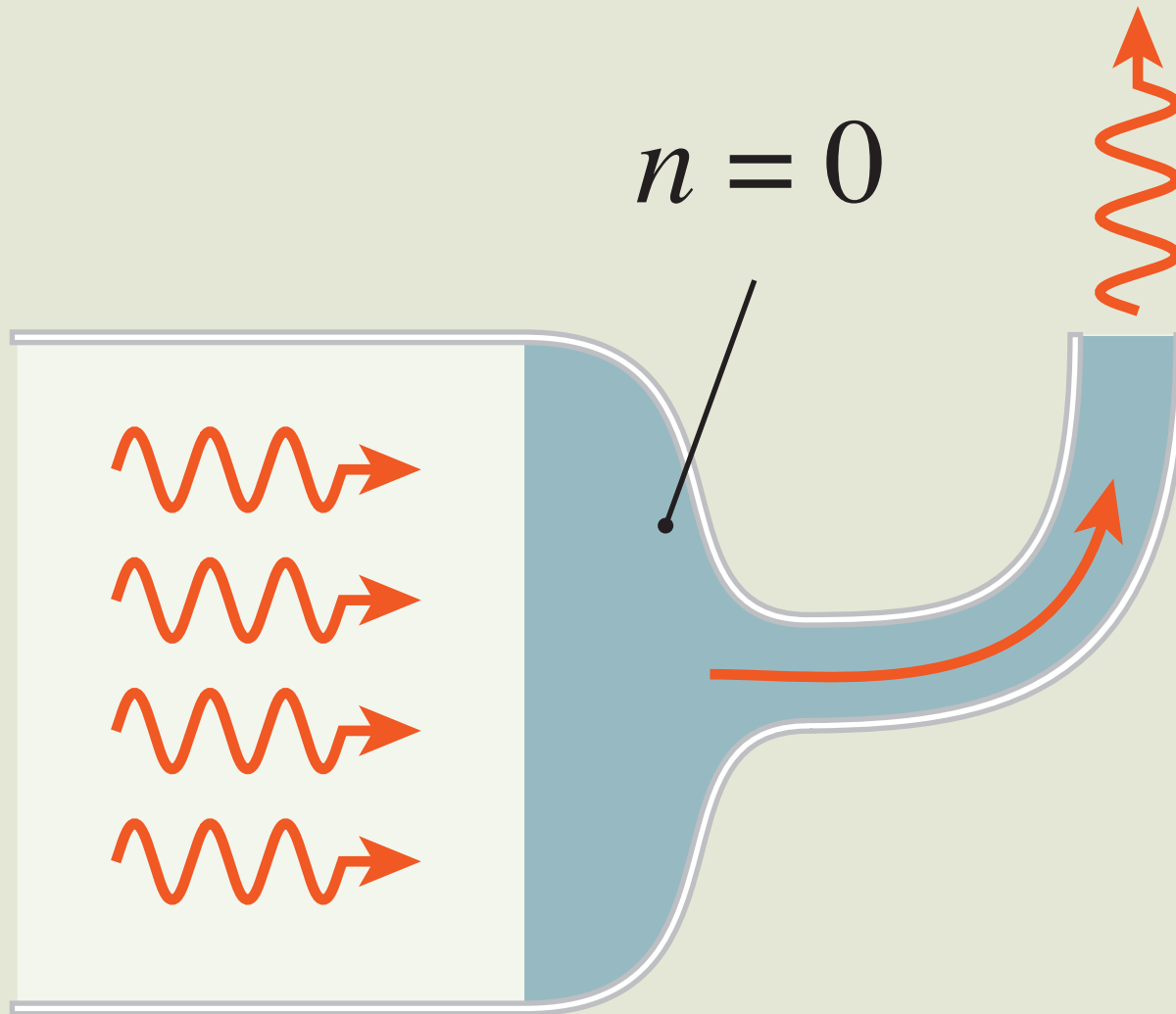
2 zero index



1 index

2 zero index

“tunneling with infinite decay length”



1 index

2 zero index

how?

$$n = \sqrt{\varepsilon\mu}$$

how?

$$n = \sqrt{\epsilon\mu}$$

but  $\epsilon$  and  $\mu$  also determine reflectivity

$$R = \frac{Z - 1}{Z + 1}$$

how?

$$n = \sqrt{\epsilon\mu}$$

but  $\epsilon$  and  $\mu$  also determine reflectivity

$$R = \frac{Z - 1}{Z + 1}$$

where

$$Z = \sqrt{\frac{\mu}{\epsilon}}$$



how?

$$\varepsilon \rightarrow 0$$

$$n = \sqrt{\varepsilon\mu} \rightarrow 0$$

but  $\varepsilon$  and  $\mu$  also determine reflectivity

$$R = \frac{Z - 1}{Z + 1}$$

where

$$Z = \sqrt{\frac{\mu}{\varepsilon}}$$

how?

$$\varepsilon \rightarrow 0$$

$$n = \sqrt{\varepsilon\mu} \rightarrow 0$$

but  $\varepsilon$  and  $\mu$  also determine reflectivity

$$R = \frac{Z - 1}{Z + 1}$$

where

$$Z = \sqrt{\frac{\mu}{\varepsilon}} \rightarrow \infty$$

how?

$$\varepsilon \rightarrow 0$$

$$n = \sqrt{\varepsilon\mu} \rightarrow 0$$

but  $\varepsilon$  and  $\mu$  also determine reflectivity

$$R = \frac{Z-1}{Z+1} \rightarrow 1$$

where

$$Z = \sqrt{\frac{\mu}{\varepsilon}} \rightarrow \infty$$

how?

$$\mu \rightarrow 0$$

$$n = \sqrt{\epsilon\mu} \rightarrow 0$$

but  $\epsilon$  and  $\mu$  also determine reflectivity

$$R = \frac{Z - 1}{Z + 1}$$

where

$$Z = \sqrt{\frac{\mu}{\epsilon}}$$

how?

$$\mu \rightarrow 0$$

$$n = \sqrt{\epsilon\mu} \rightarrow 0$$

but  $\epsilon$  and  $\mu$  also determine reflectivity

$$R = \frac{Z - 1}{Z + 1}$$

where

$$Z = \sqrt{\frac{\mu}{\epsilon}} \rightarrow 0$$

how?

$$\mu \rightarrow 0$$

$$n = \sqrt{\epsilon\mu} \rightarrow 0$$

but  $\epsilon$  and  $\mu$  also determine reflectivity

$$R = \frac{Z - 1}{Z + 1} \rightarrow -1$$

where

$$Z = \sqrt{\frac{\mu}{\epsilon}} \rightarrow 0$$

how?

$$\epsilon, \mu \rightarrow 0$$

$$n = \sqrt{\epsilon\mu} \rightarrow 0$$

but  $\epsilon$  and  $\mu$  also determine reflectivity

$$R = \frac{Z - 1}{Z + 1}$$

where

$$Z = \sqrt{\frac{\mu}{\epsilon}} \quad \text{finite!}$$

but  $\mu \neq 1$  requires a magnetic response!

1 index

2 zero index

3 experiments



# Engineering a magnetic response

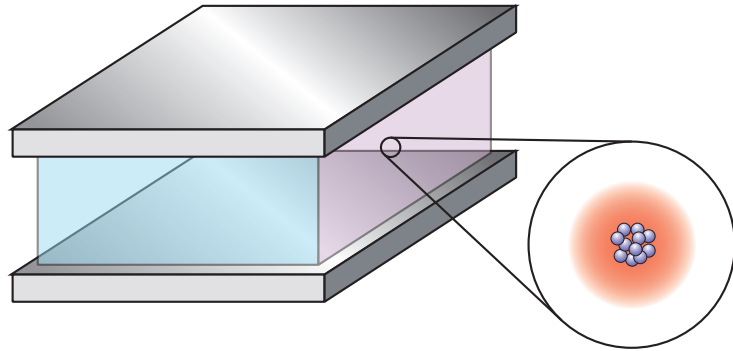
**1** index

**2** zero index

**3** experiments

# Engineering a magnetic response

**bulk material**



**properties derive from  
constituent atoms**

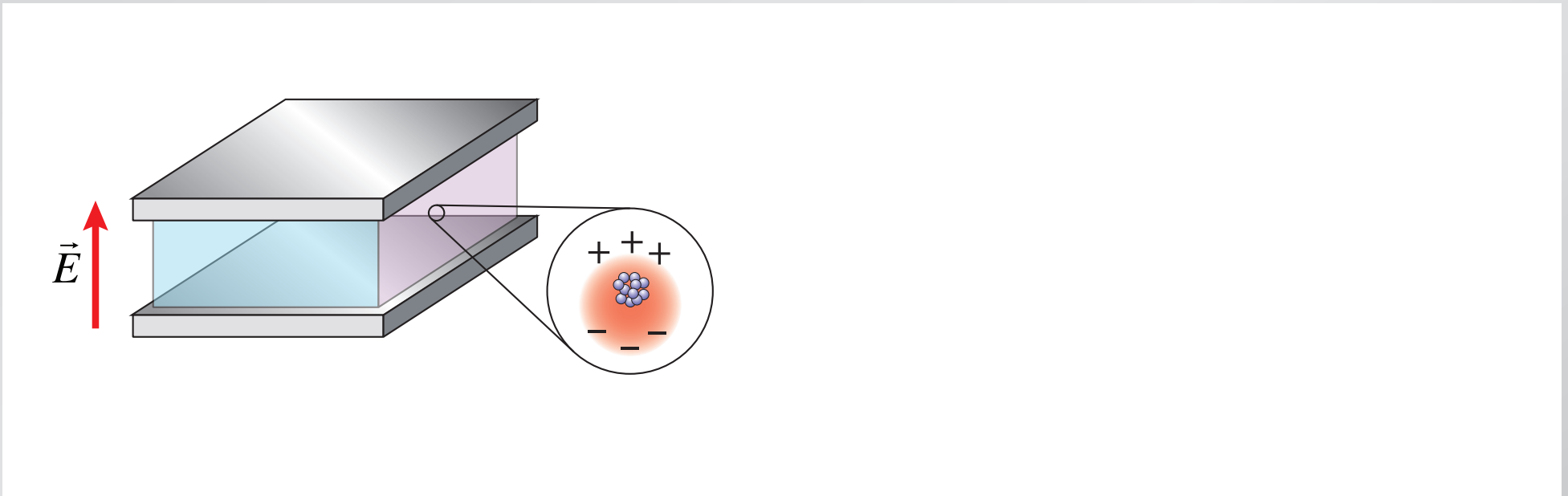
**1** index

**2** zero index

**3** experiments

# Engineering a magnetic response

bulk material



properties derive from  
constituent atoms

1 index

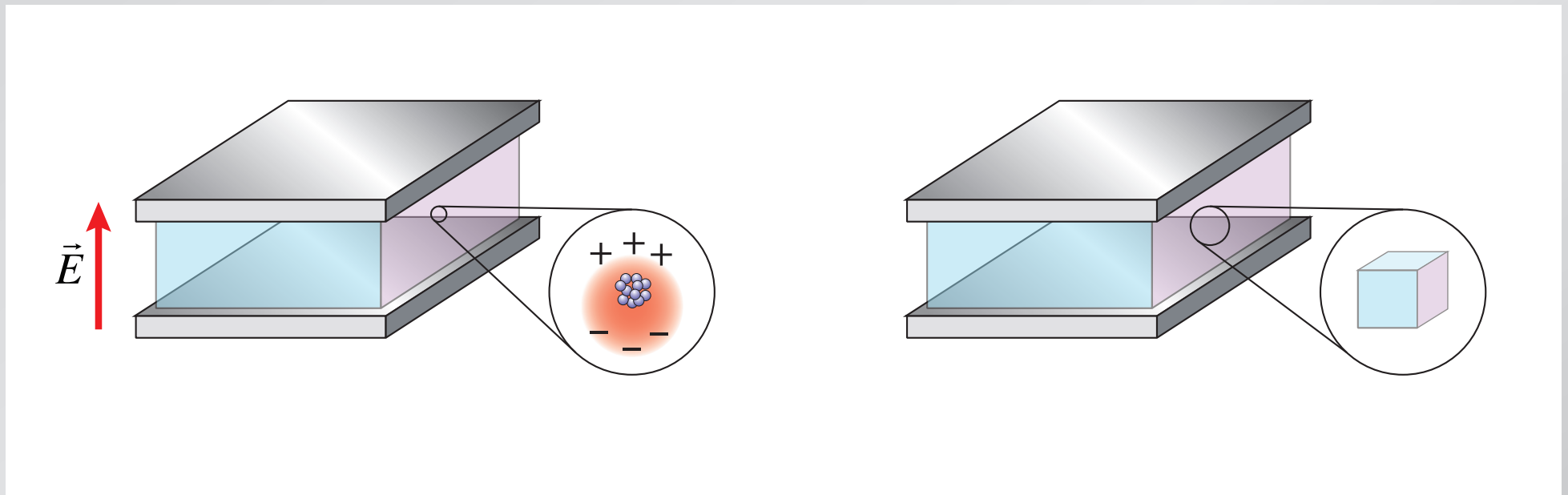
2 zero index

3 experiments

# Engineering a magnetic response

**bulk material**

**composite material**



properties derive from  
constituent atoms

properties derive from  
constituent units

**1** index

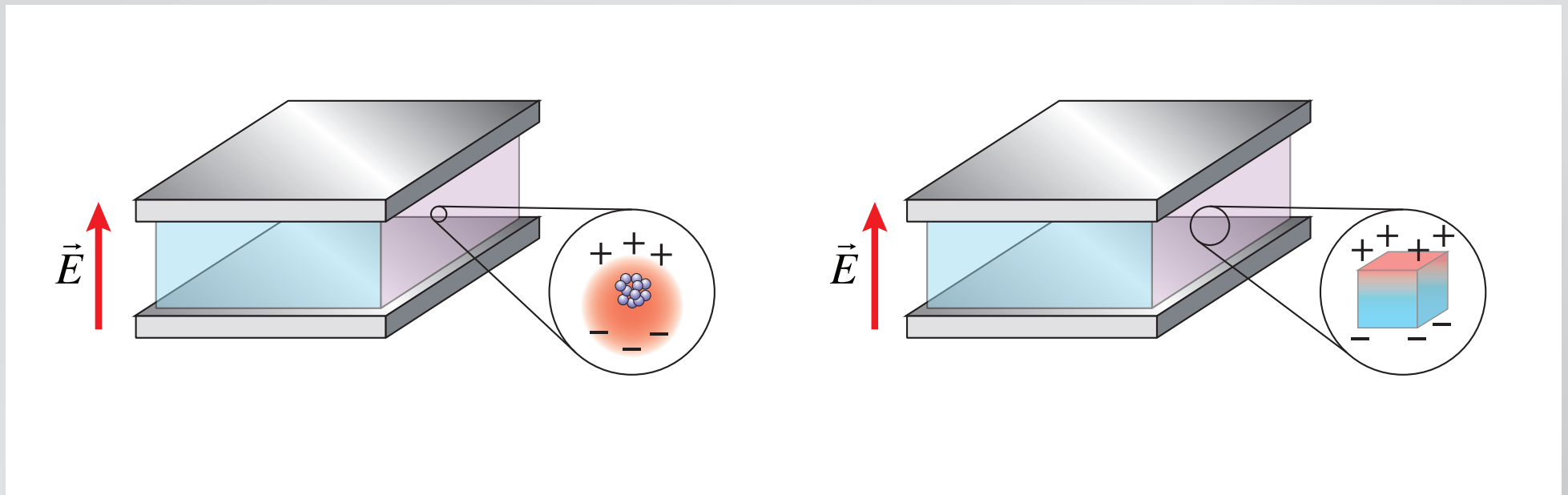
**2** zero index

**3** experiments

# Engineering a magnetic response

bulk material

composite material



properties derive from  
constituent atoms

properties derive from  
constituent units

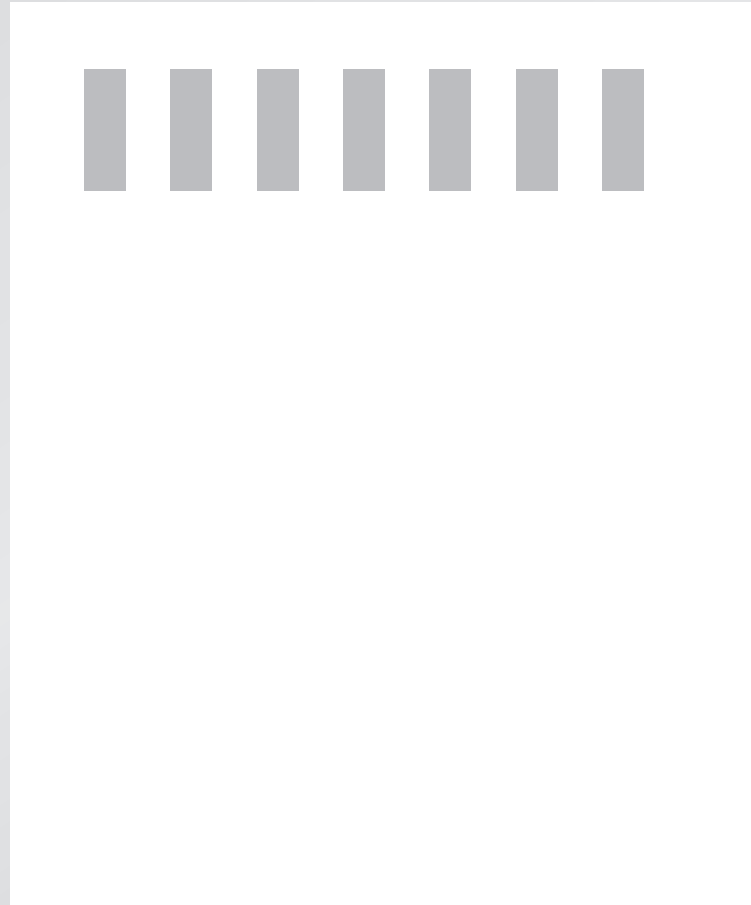
1 index

2 zero index

3 experiments

# Engineering a magnetic response

use array of dielectric rods



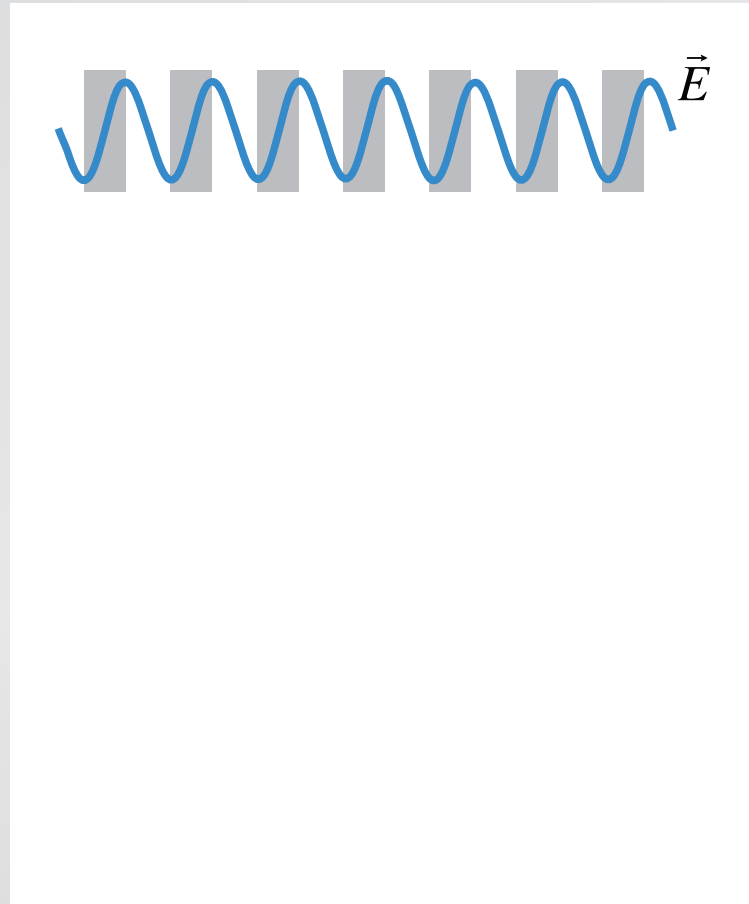
**1** index

**2** zero index

**3** experiments

# Engineering a magnetic response

incident electromagnetic wave ( $\lambda_{\text{eff}} \approx a$ )

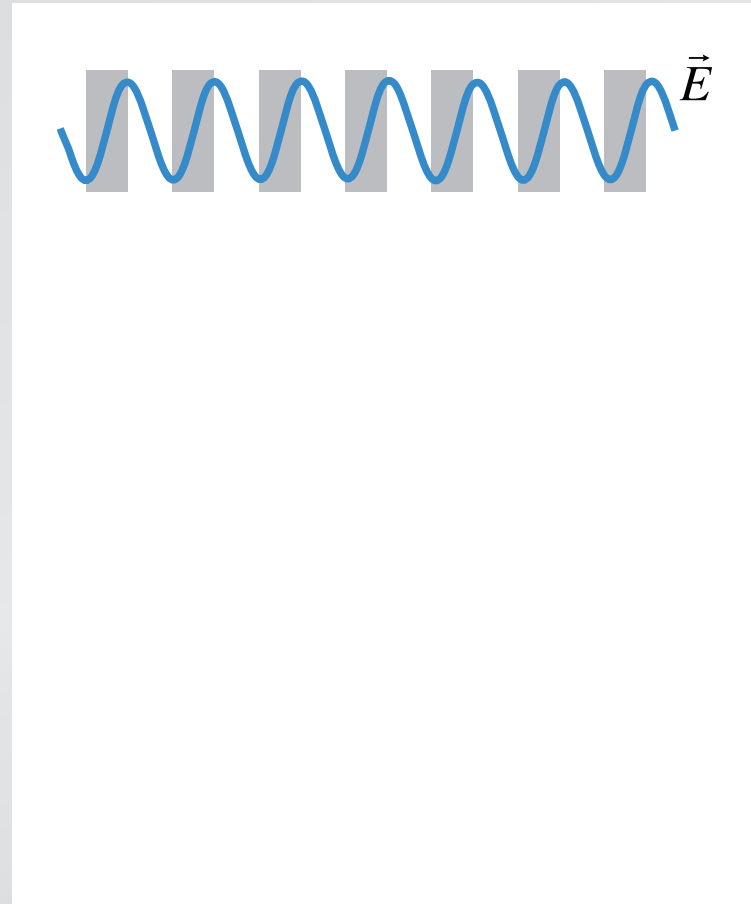


1 index

2 zero index

# Engineering a magnetic response

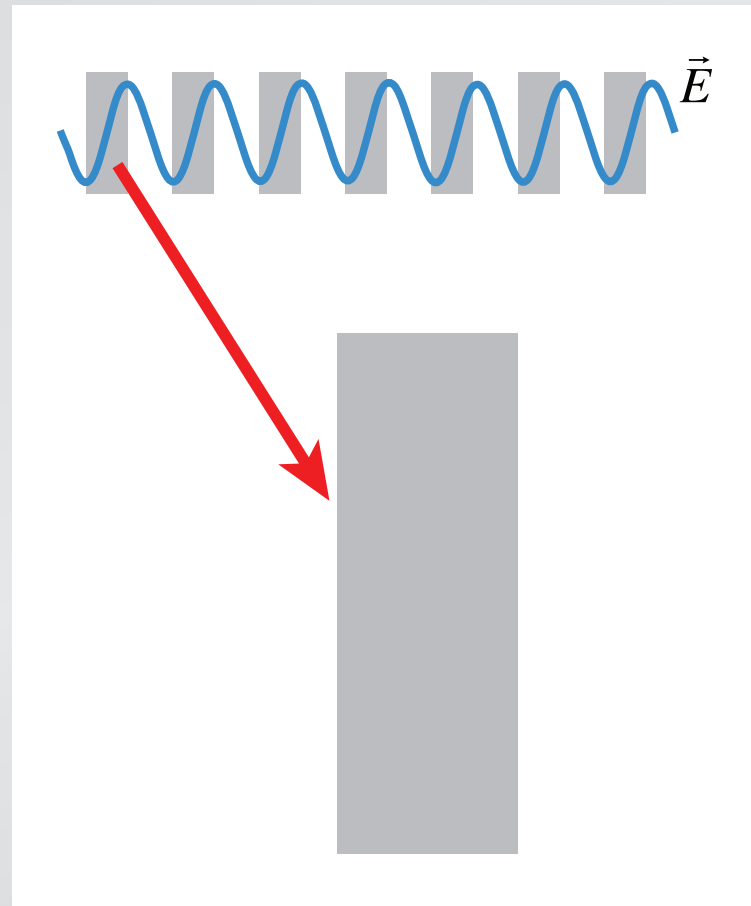
produces an electric response...





# Engineering a magnetic response

... but different electric fields front and back...



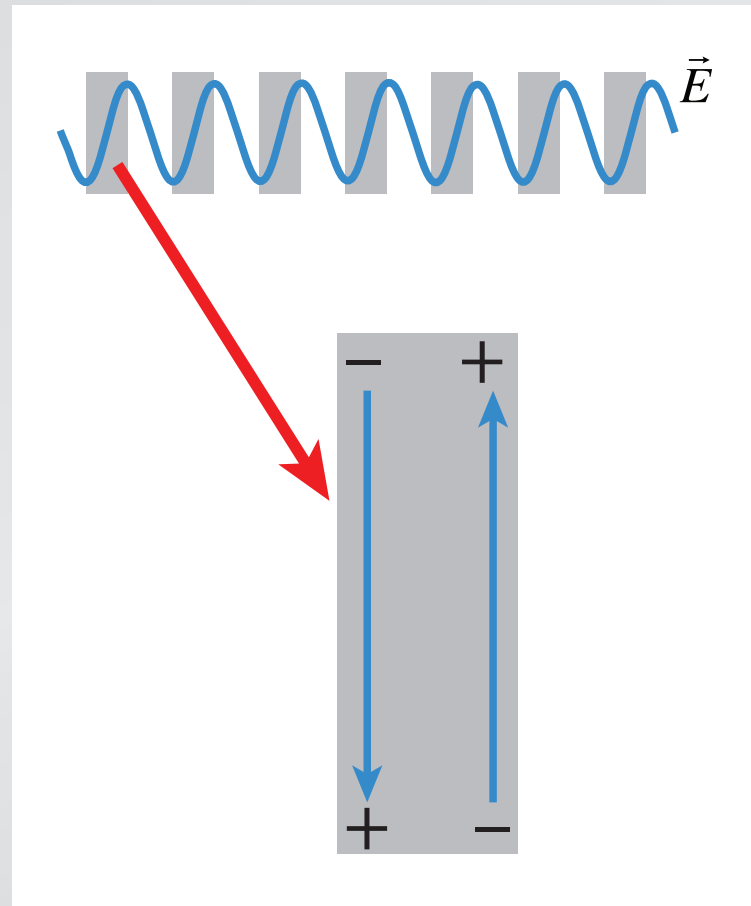
1 index

2 zero index

3 experiments

# Engineering a magnetic response

...induce different polarizations on opposite sides...



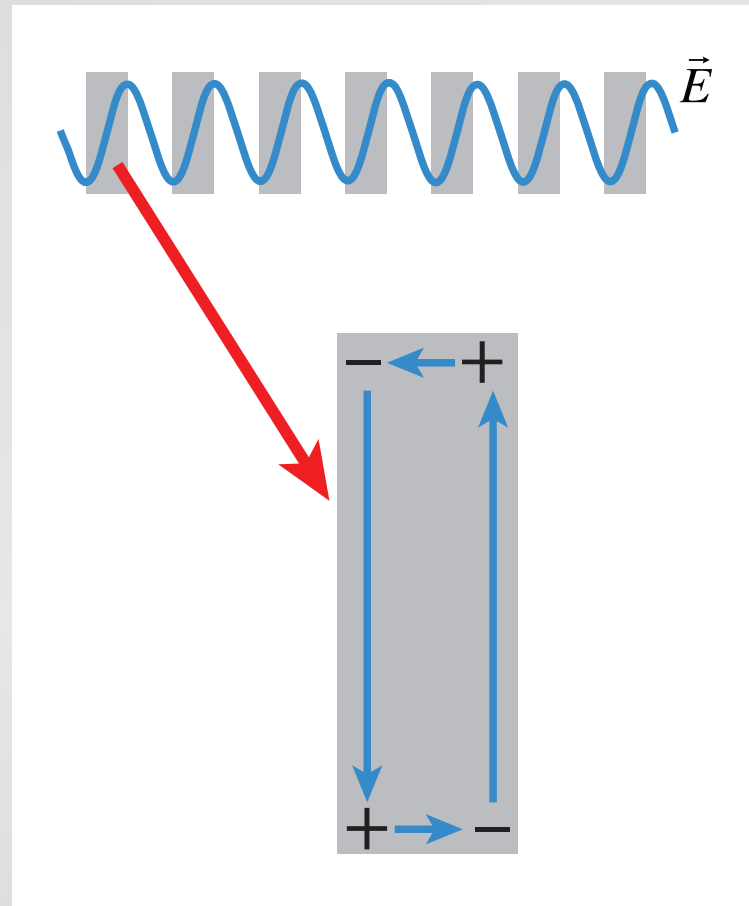
1 index

2 zero index

3 experiments

# Engineering a magnetic response

...causing a current loop...



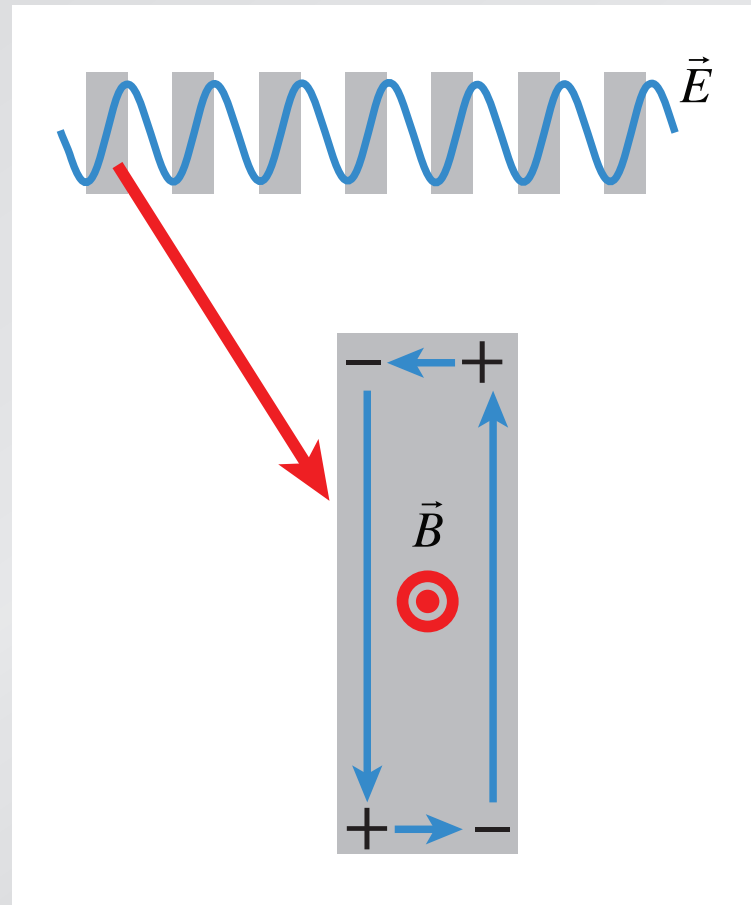
1 index

2 zero index

3 experiments

# Engineering a magnetic response

...which, in turn, produces an induced magnetic field



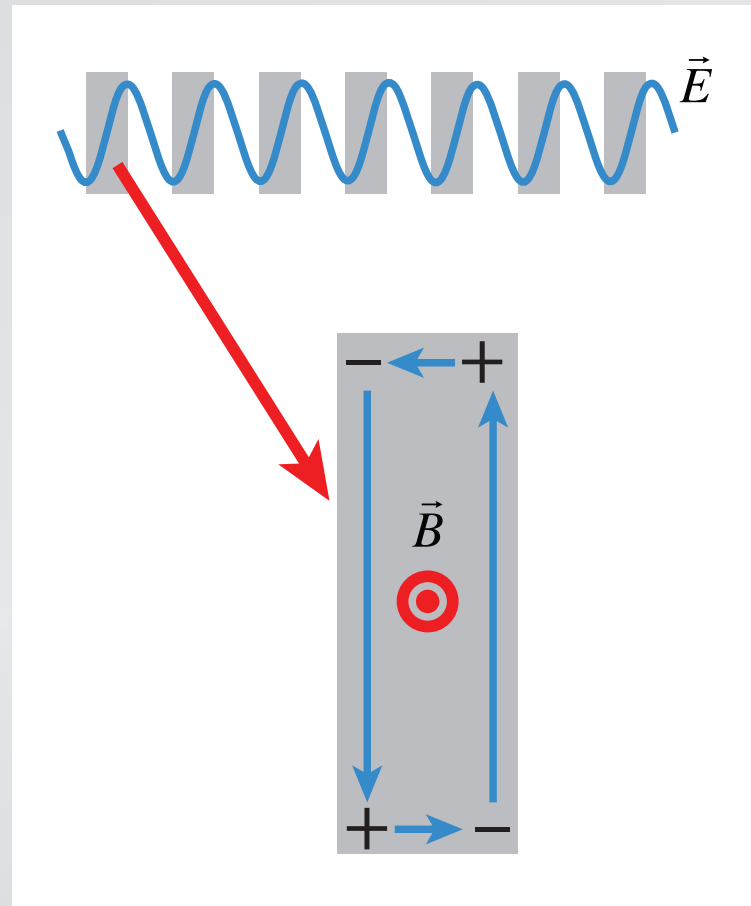
1 index

2 zero index

3 experiments

# Engineering a magnetic response

adjust design so electrical and magnetic resonances coincide



1 index

2 zero index

3 experiments

# Engineering a magnetic response

adjustable parameters



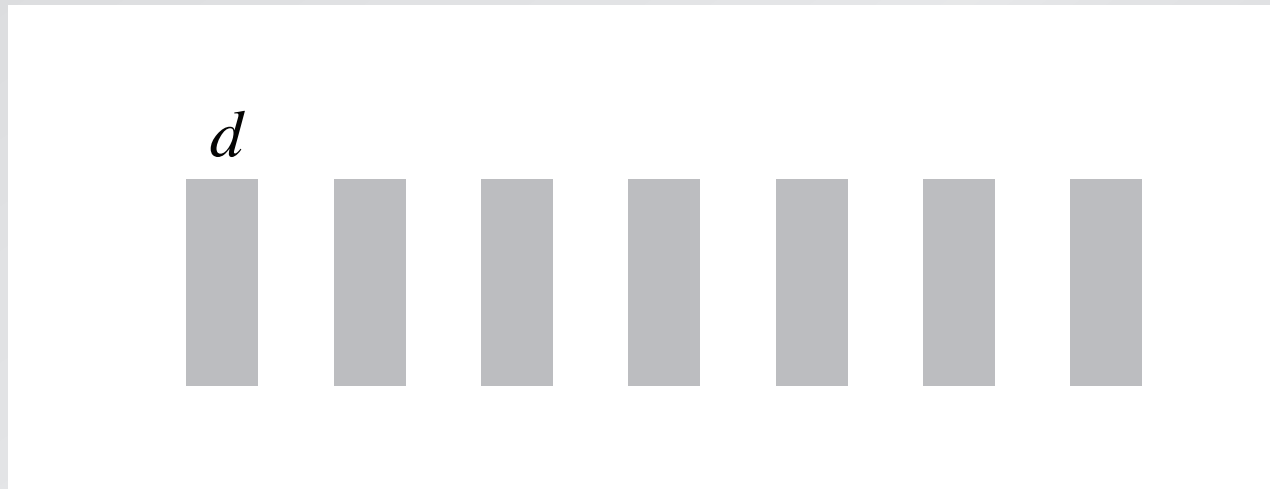
**1** index

**2** zero index

**3** experiments

# Engineering a magnetic response

adjustable parameters



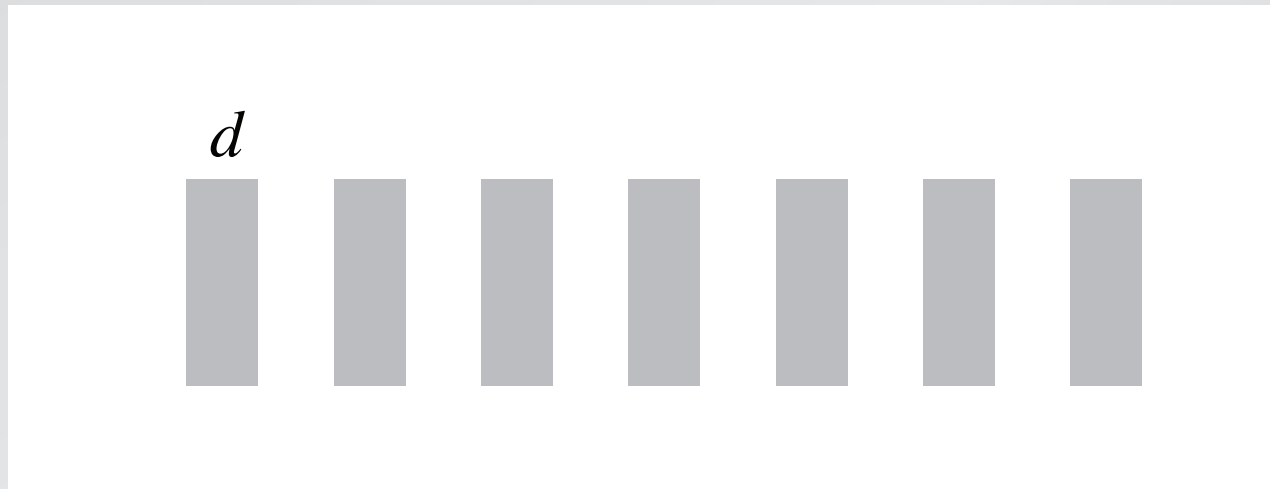
1 index

2 zero index

3 experiments

# Engineering a magnetic response

adjustable parameters



1 index

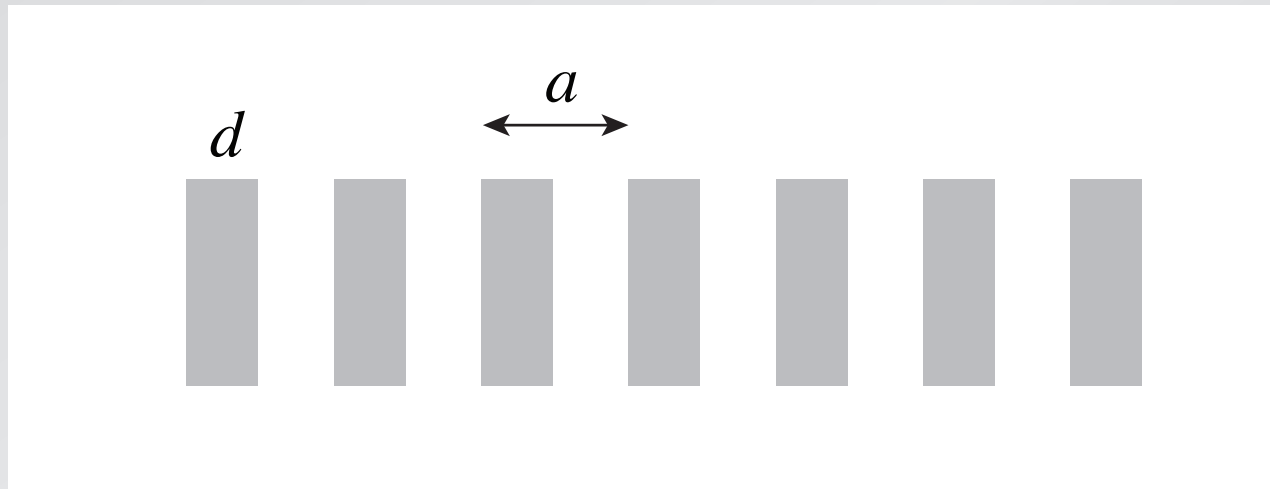
2 zero index

3 experiments



# Engineering a magnetic response

adjustable parameters



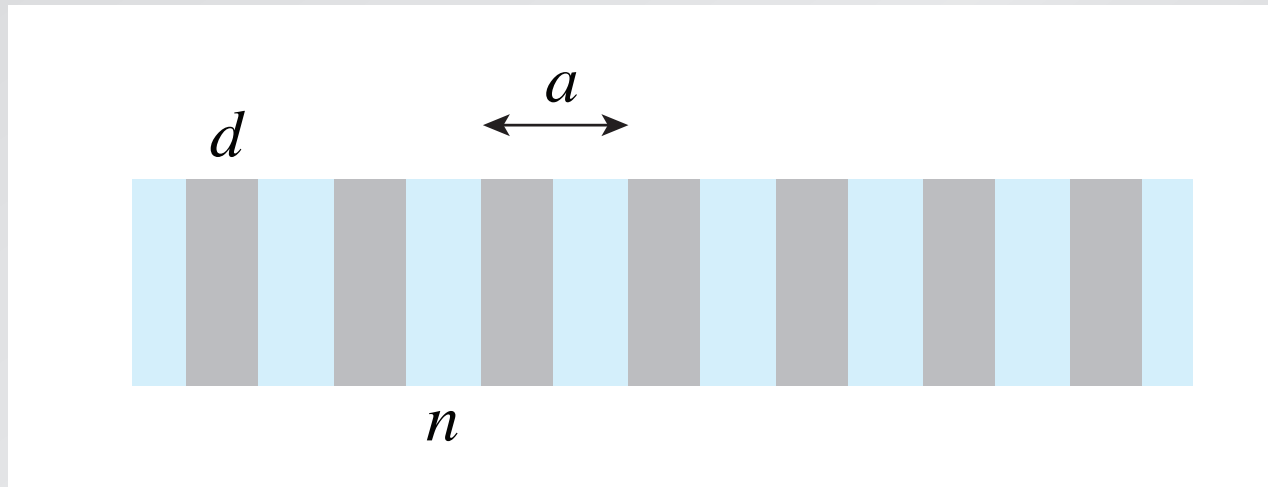
1 index

2 zero index

3 experiments

# Engineering a magnetic response

adjustable parameters



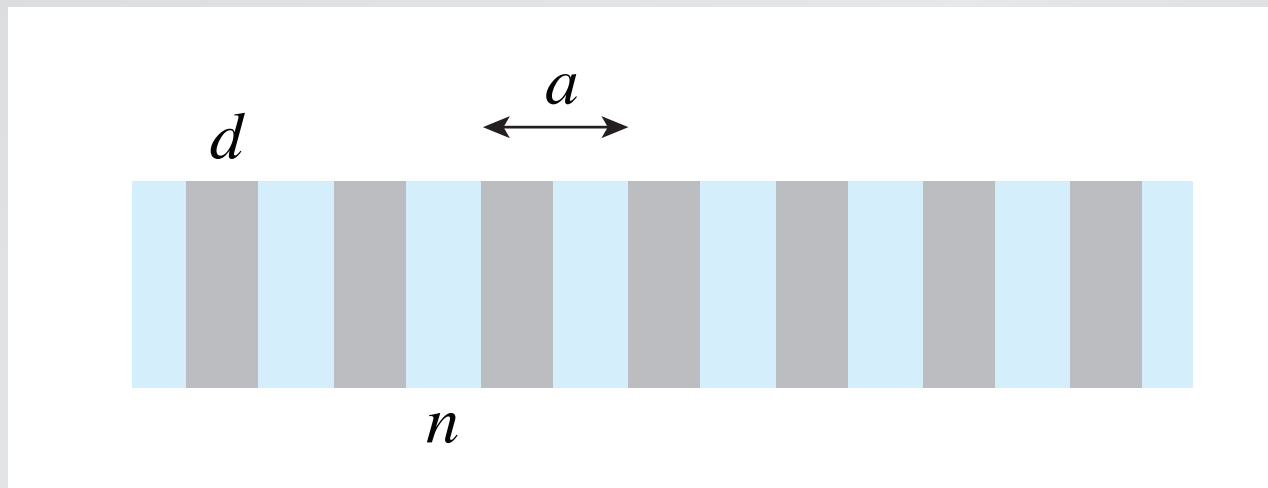
1 index

2 zero index

3 experiments

# Engineering a magnetic response

adjustable parameters

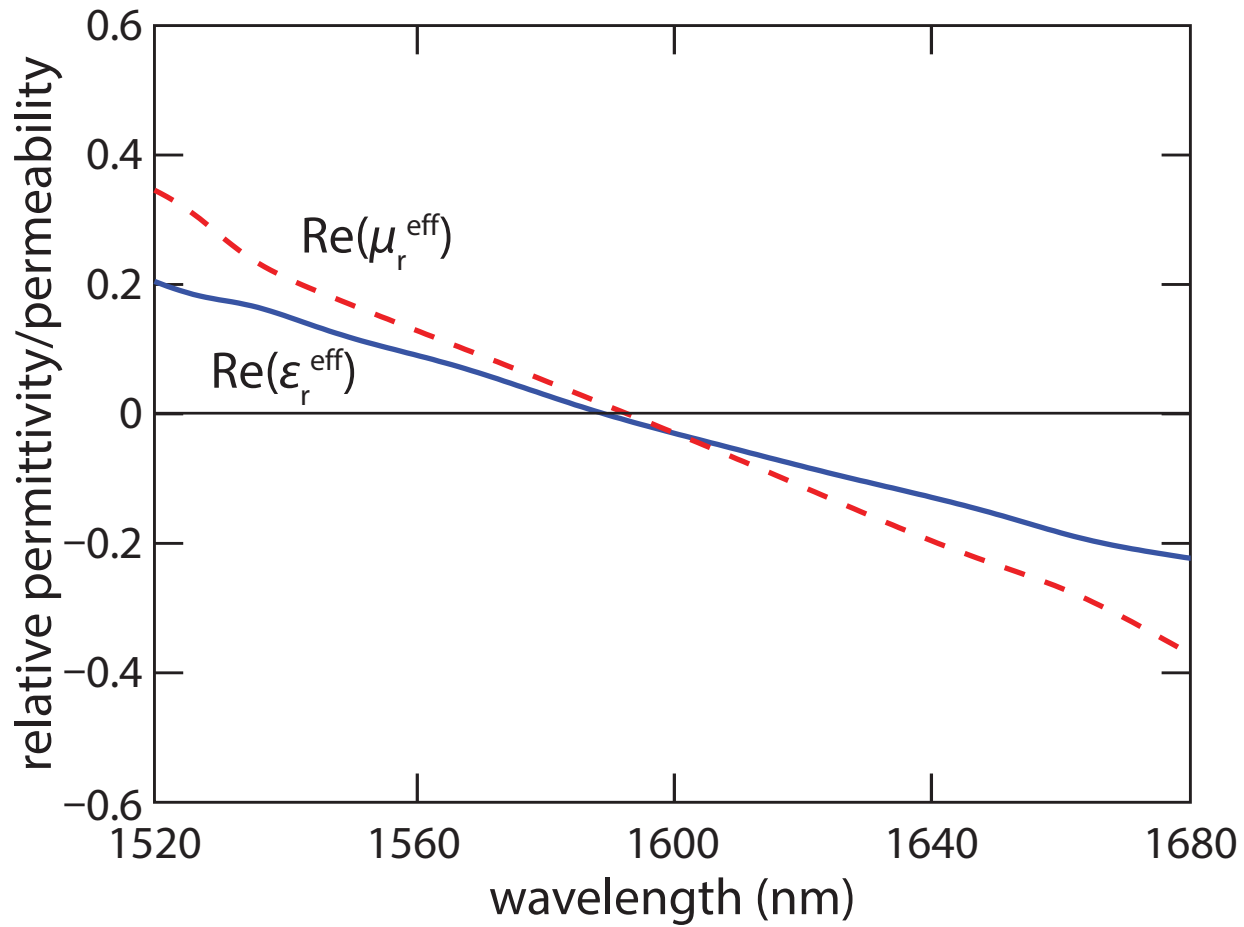


$$d = 422 \text{ nm}, \quad a = 690 \text{ nm}, \quad n = 1.57 \text{ (SU8)}$$

1 index

2 zero index

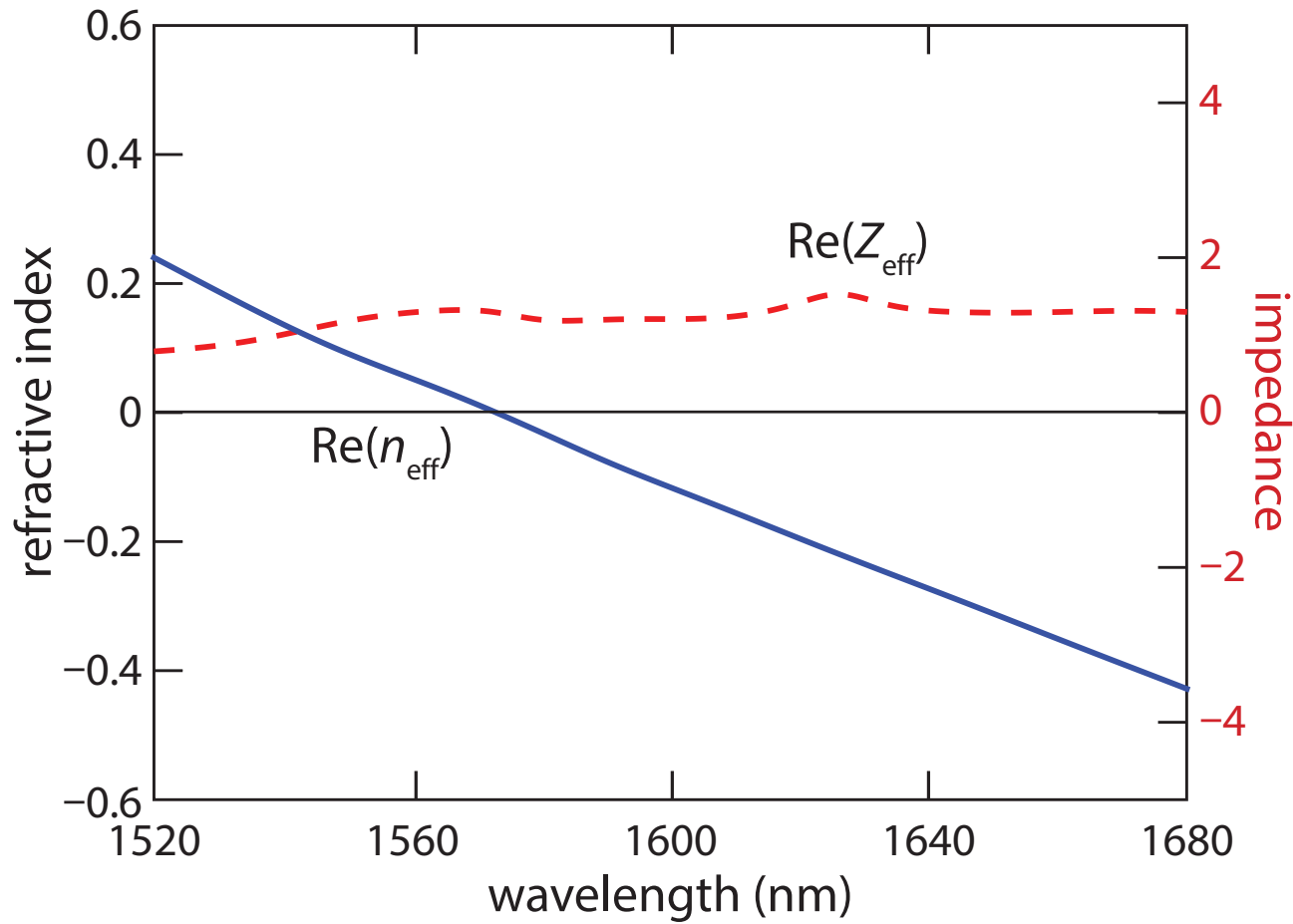
3 experiments



1 index

2 zero index

3 experiments

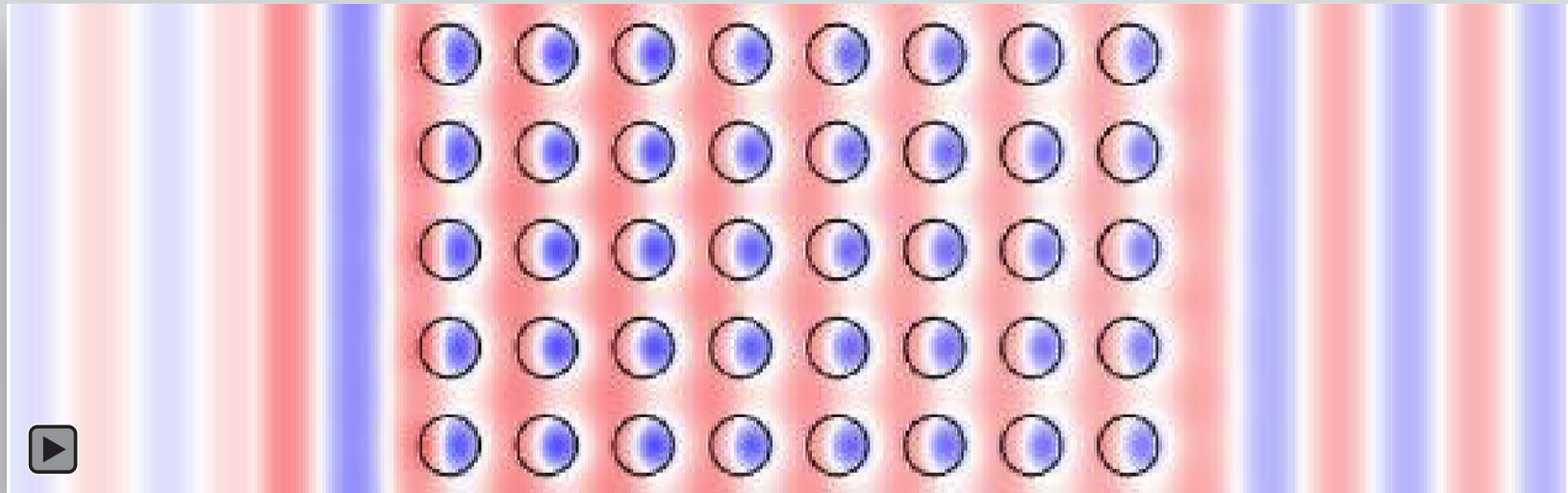


1 index

2 zero index

3 experiments

at design wavelength (1590 nm)

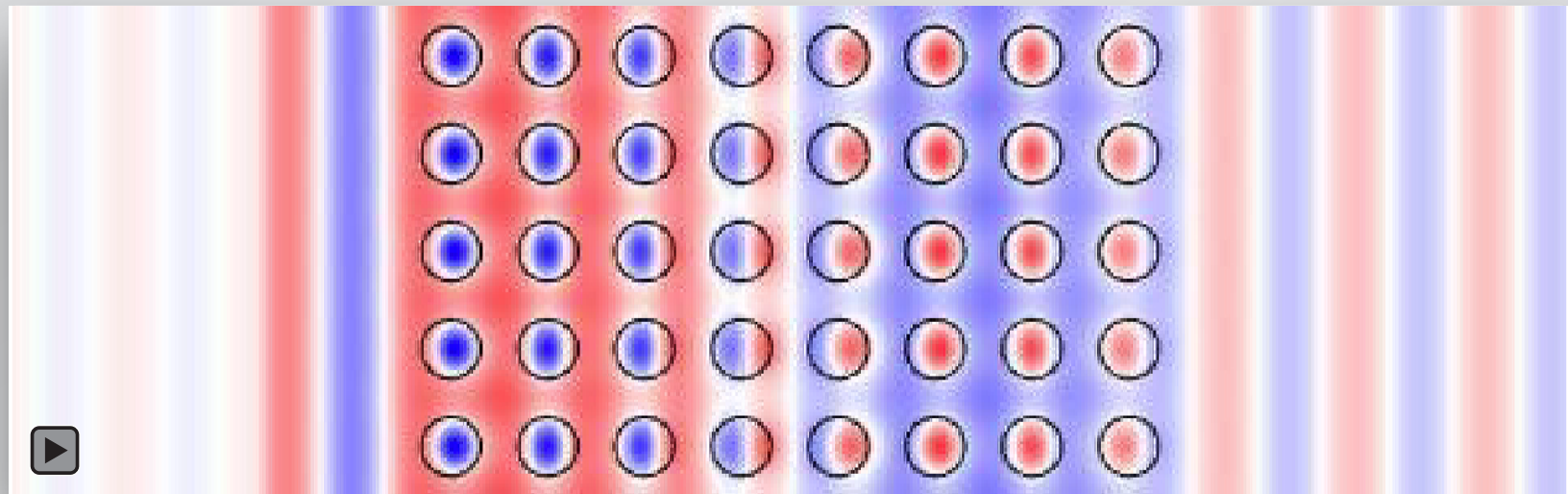


1 index

2 zero index

3 experiments

below design wavelength (1530 nm)

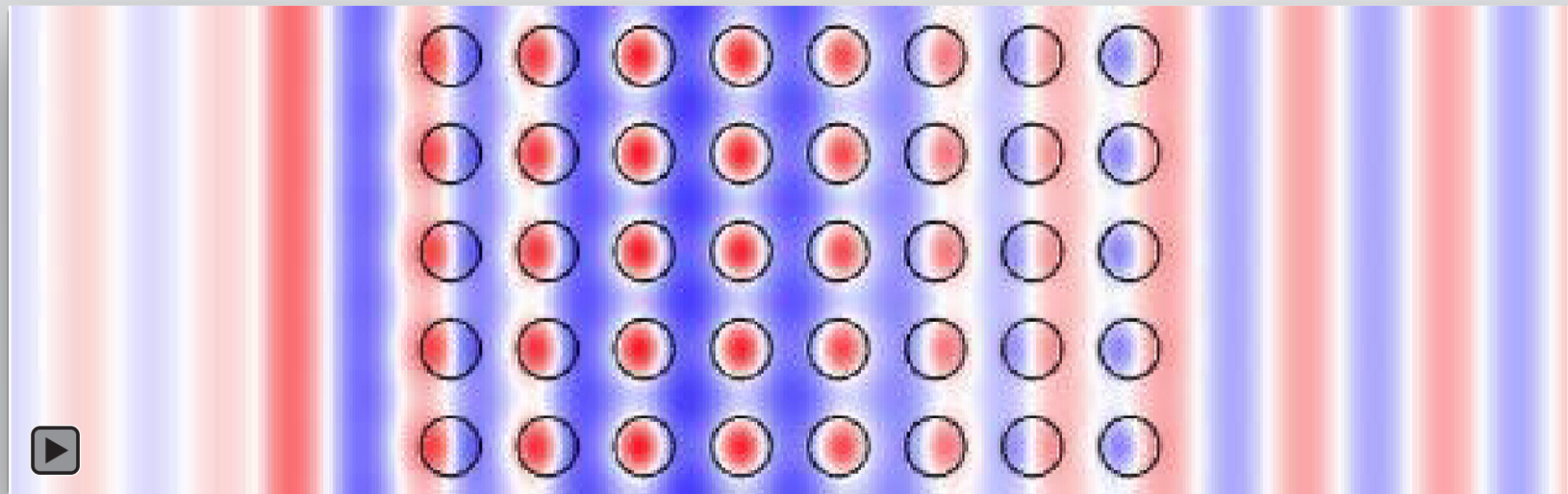


1 index

2 zero index

3 experiments

above design wavelength (1650 nm)



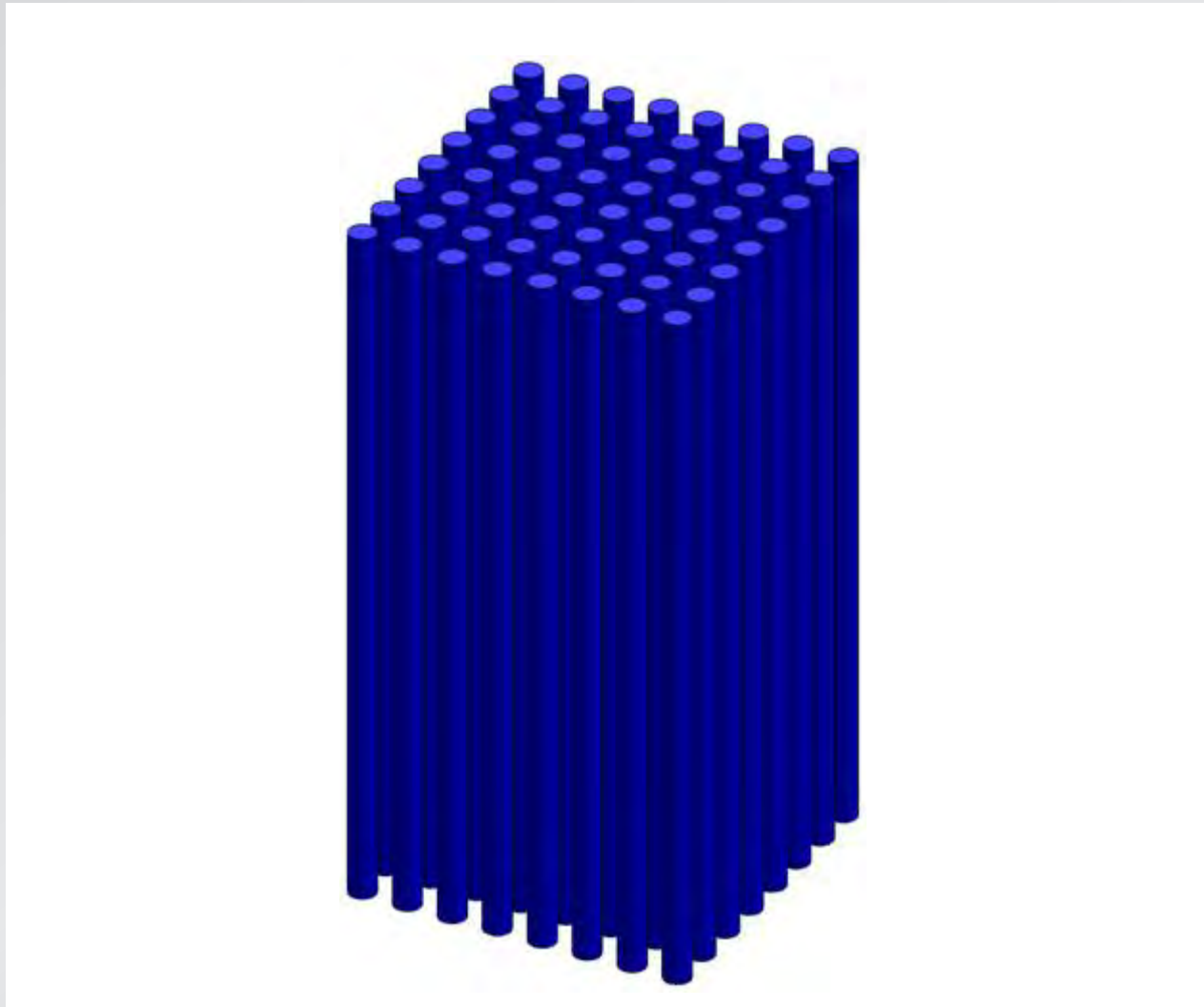
1 index

2 zero index

3 experiments



# How to fabricate?

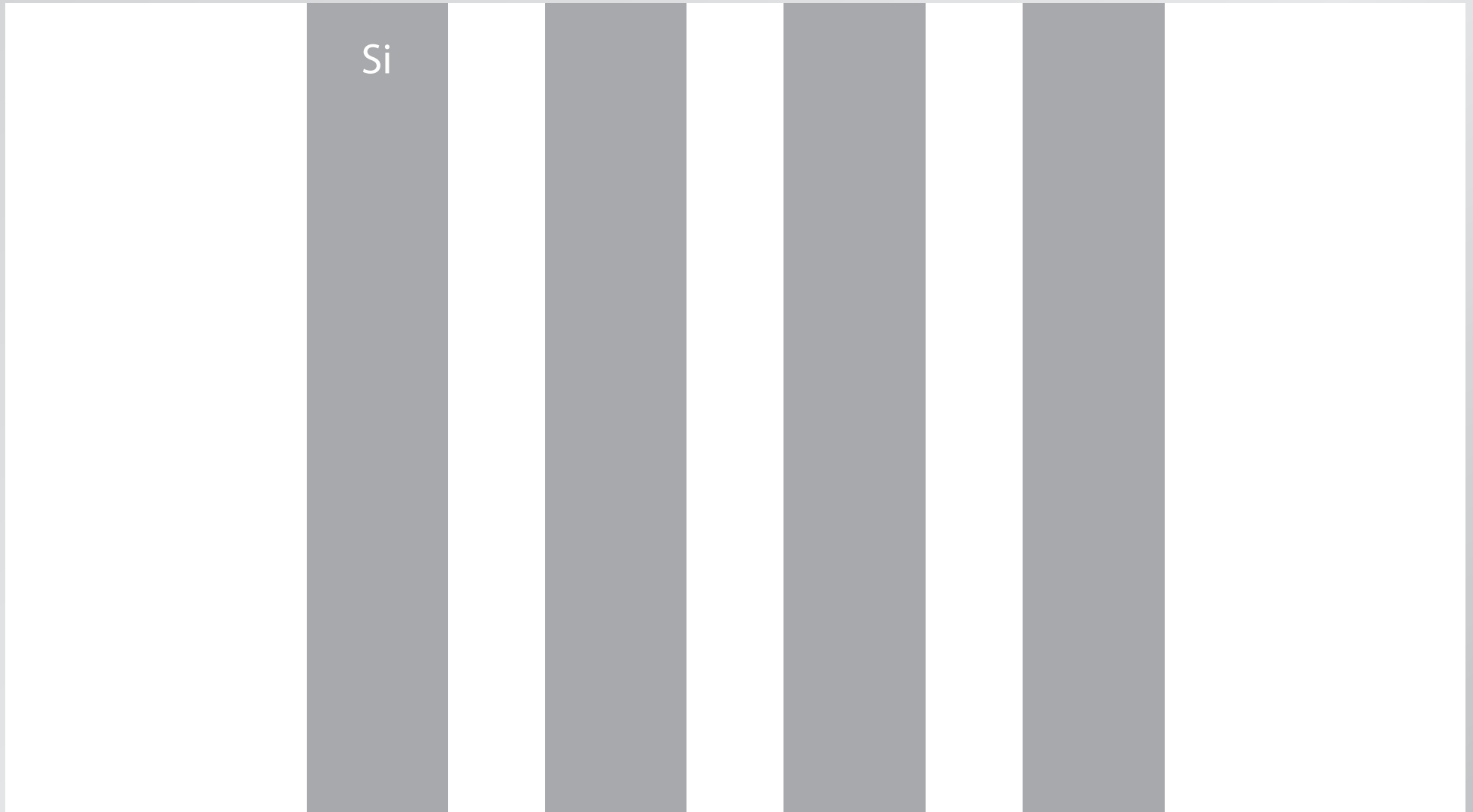


1 index

2 zero index

3 experiments

# On-chip zero-index fabrication



**1** index

**2** zero index

**3** experiments

# On-chip zero-index fabrication



1 index

2 zero index

3 experiments

# On-chip zero-index fabrication

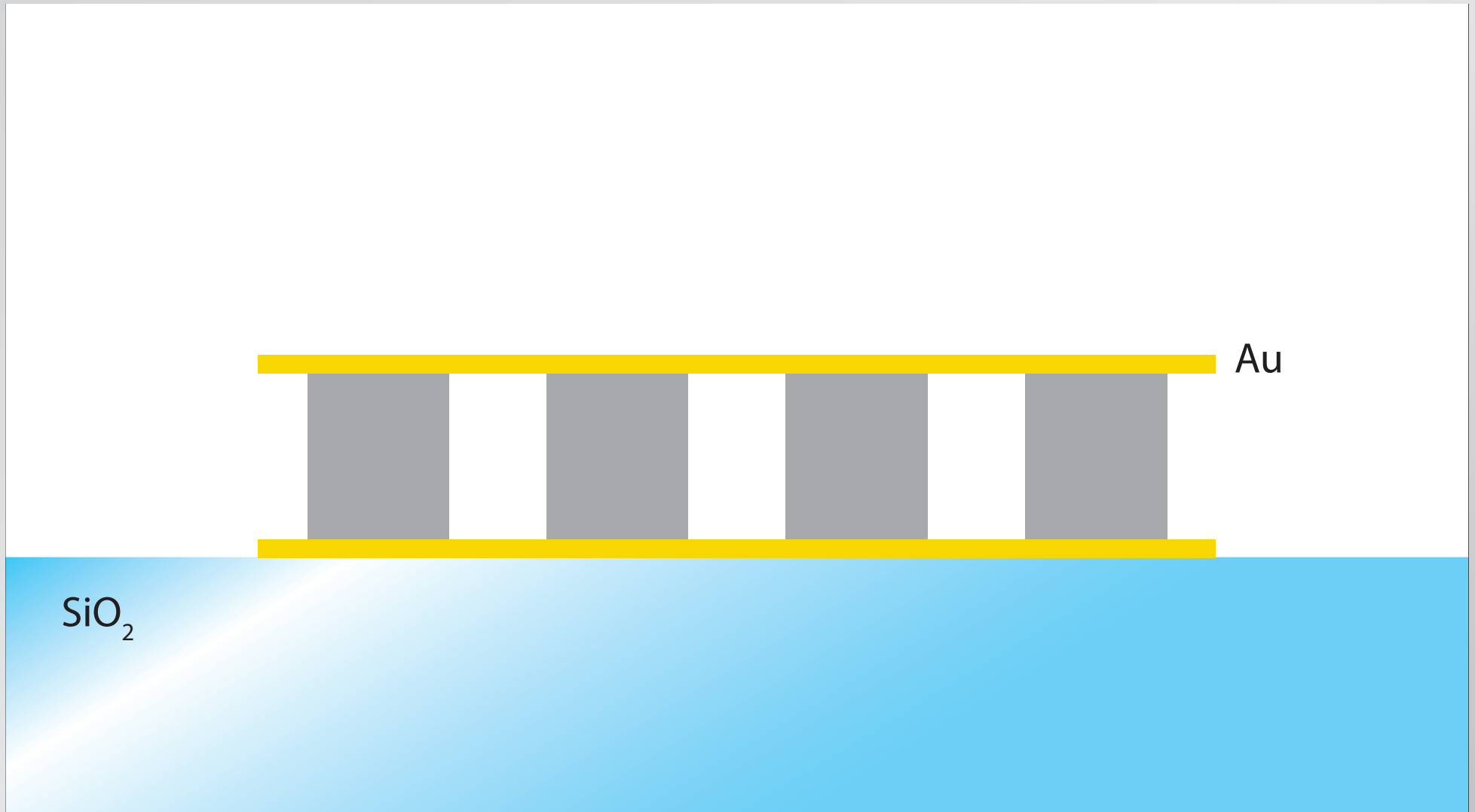


1 index

2 zero index

3 experiments

# On-chip zero-index fabrication



1 index

2 zero index

3 experiments

# On-chip zero-index fabrication

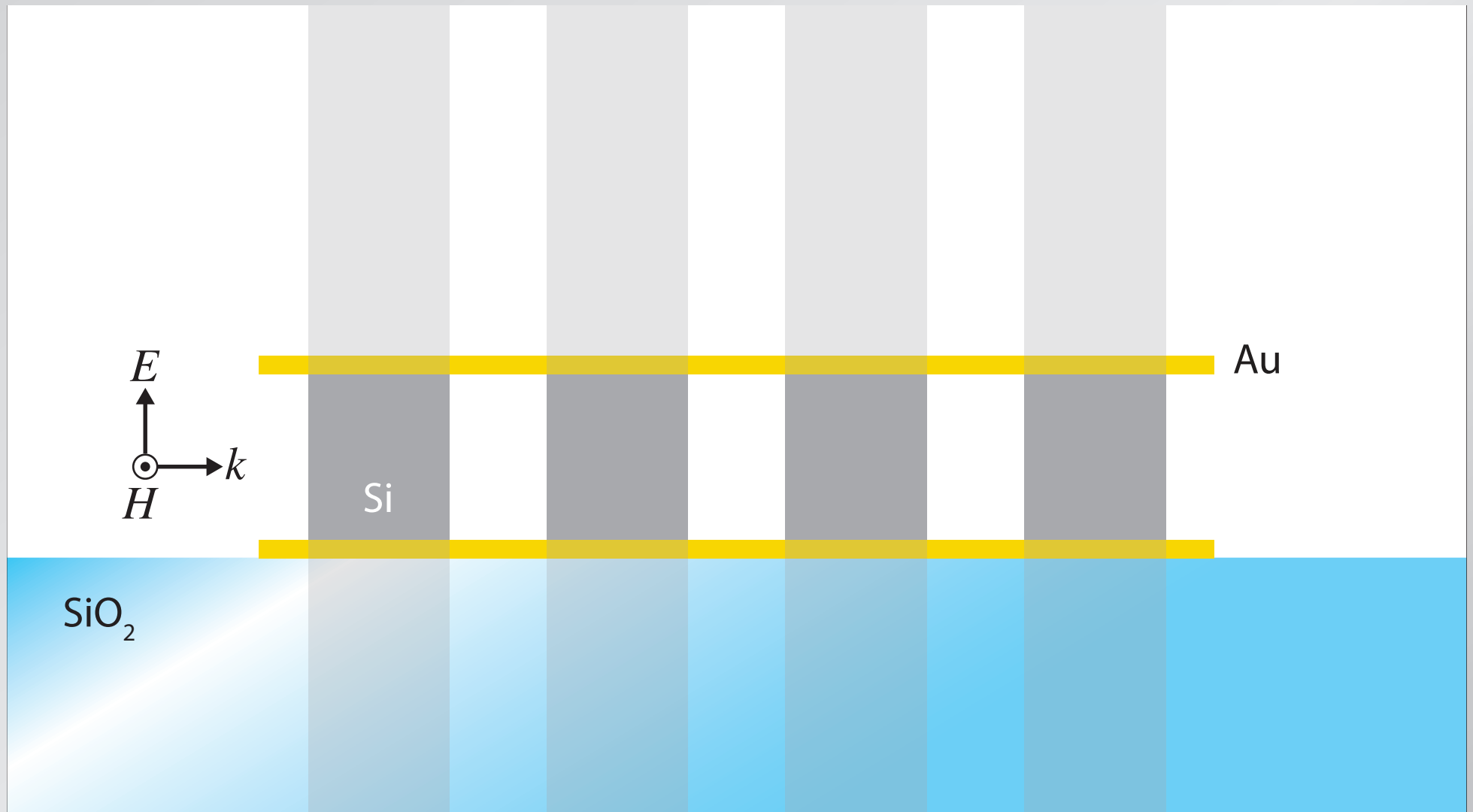


1 index

2 zero index

3 experiments

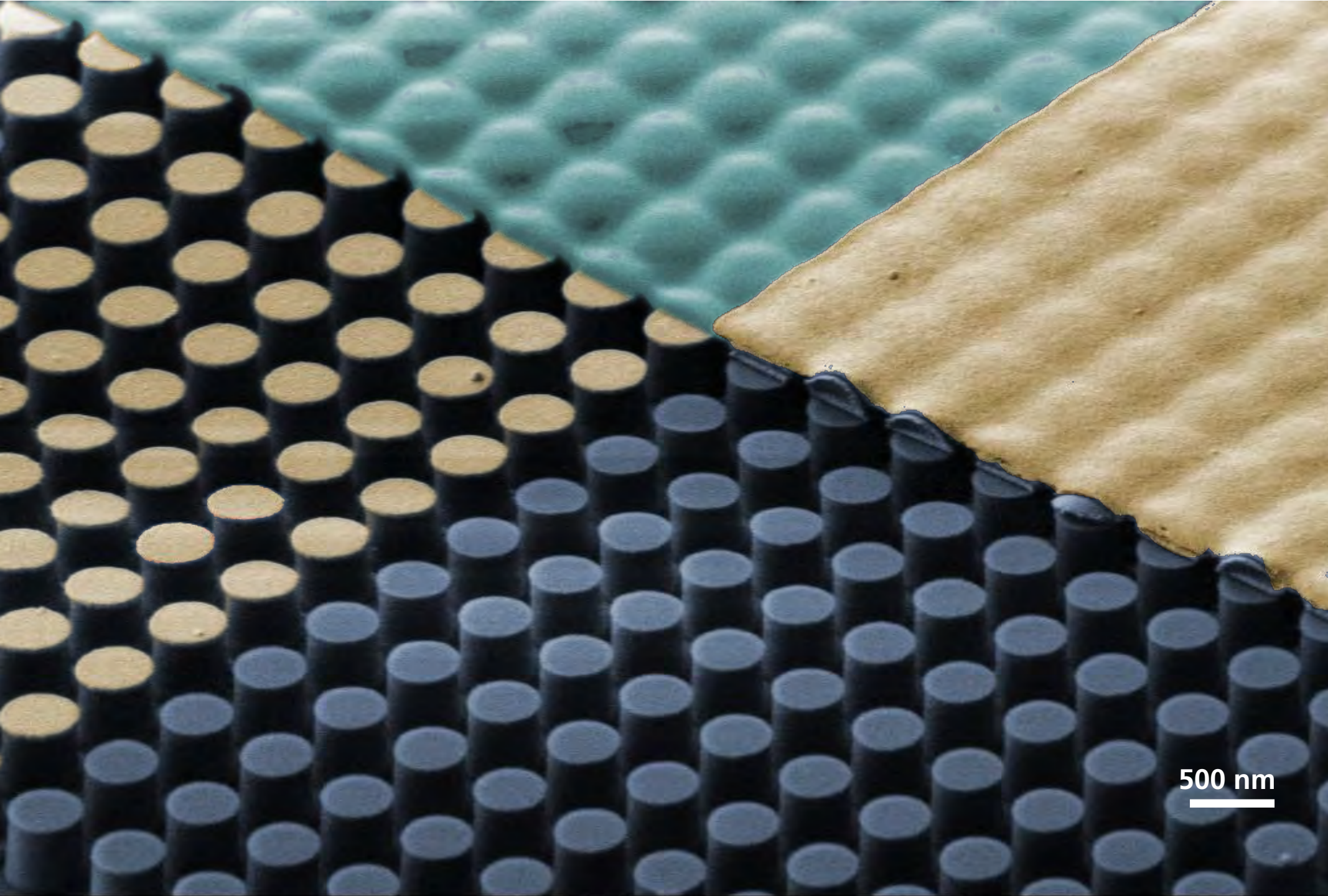
# On-chip zero-index fabrication



1 index

2 zero index

3 experiments



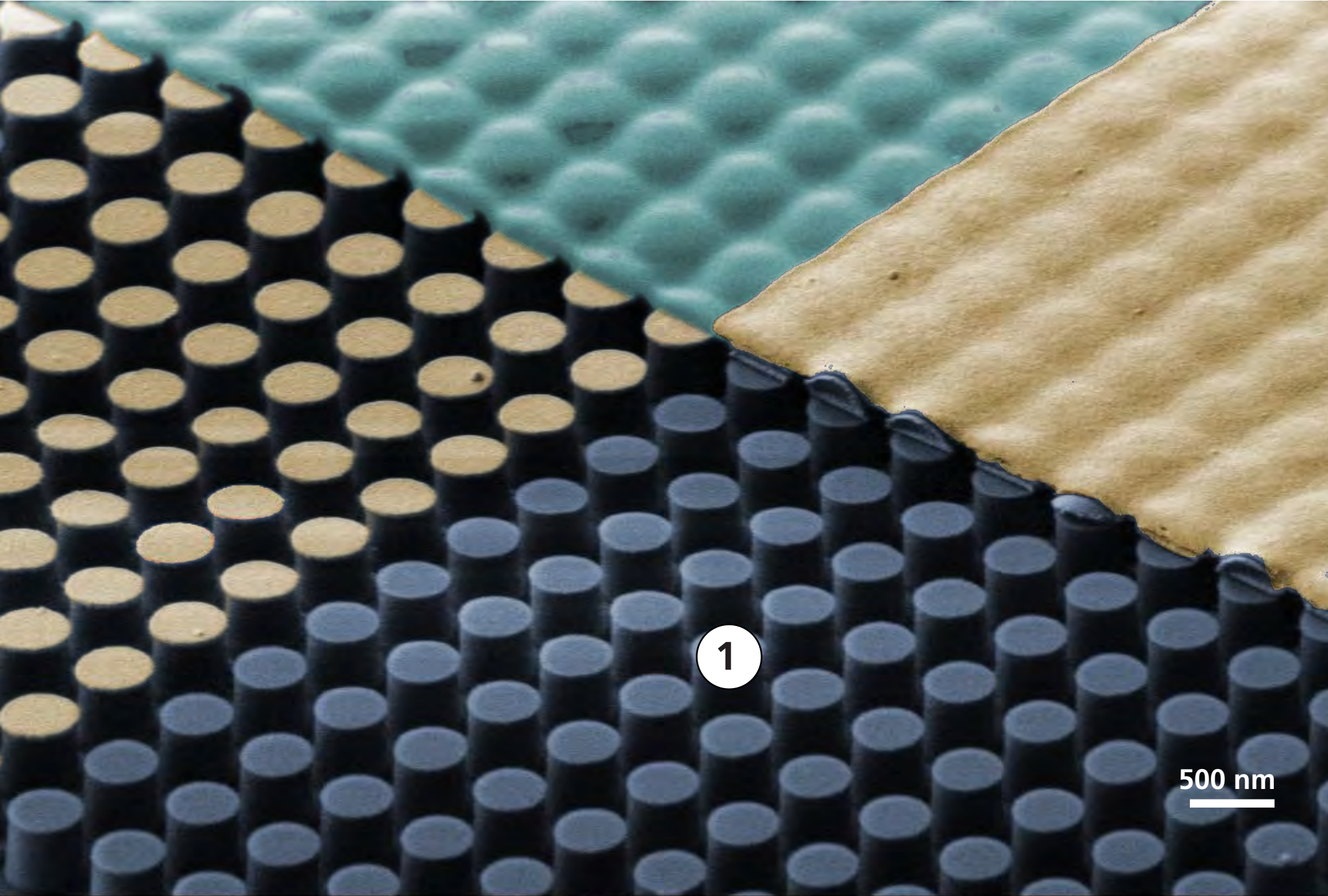
500 nm

**1** index

**2** zero index

**3** experiments





1

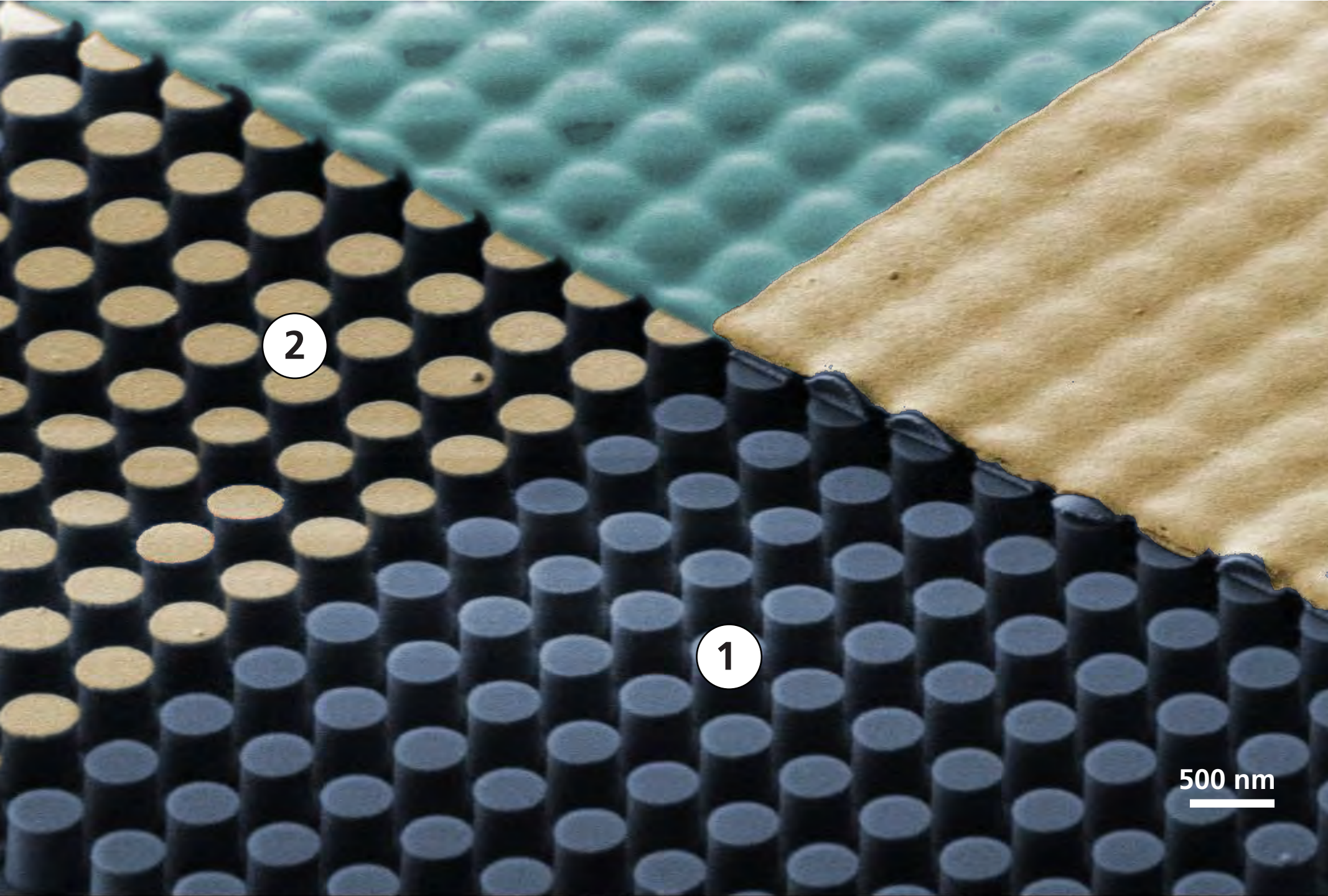
500 nm

1 index

2 zero index

3 experiments



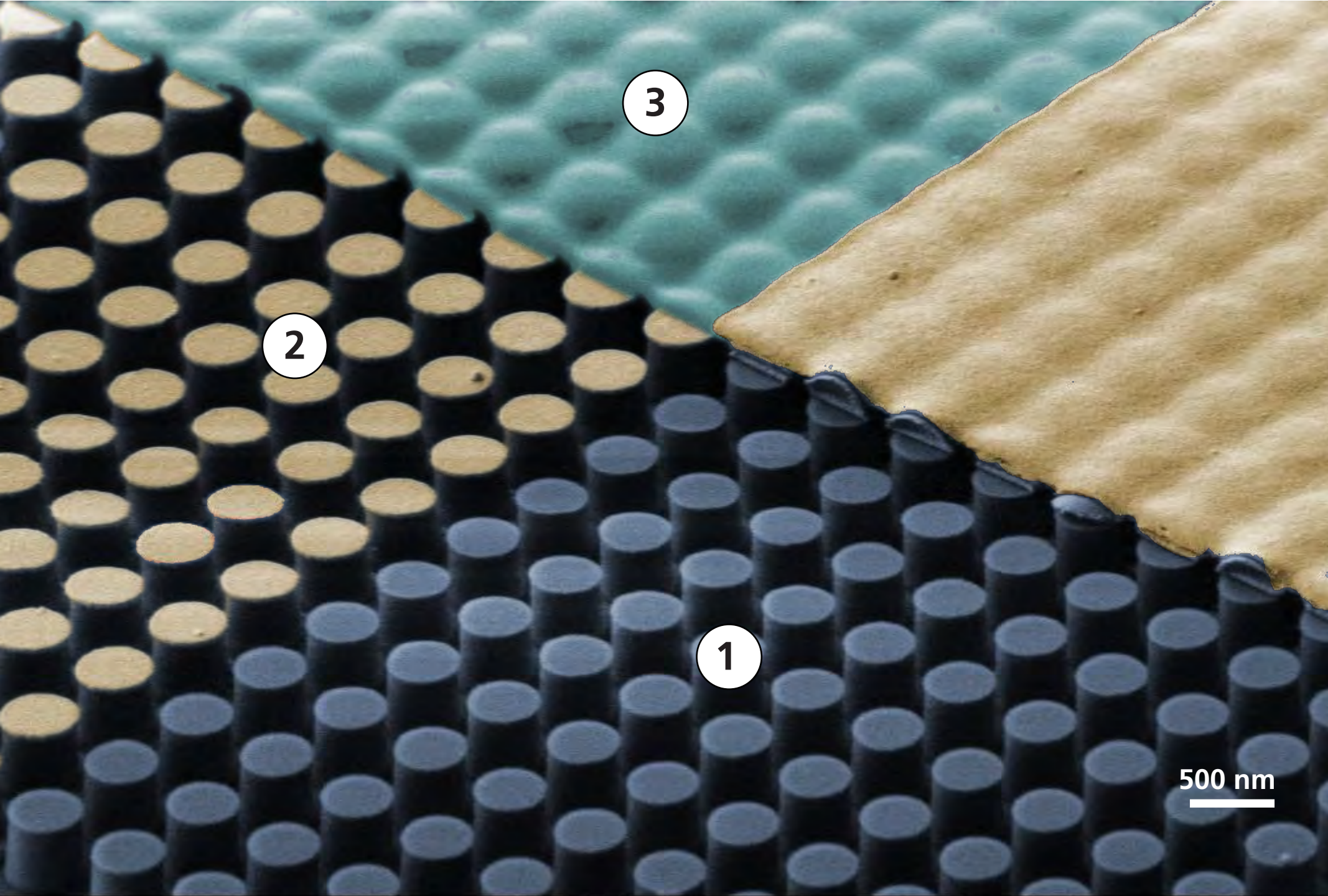


**1** index

**2** zero index

**3** experiments



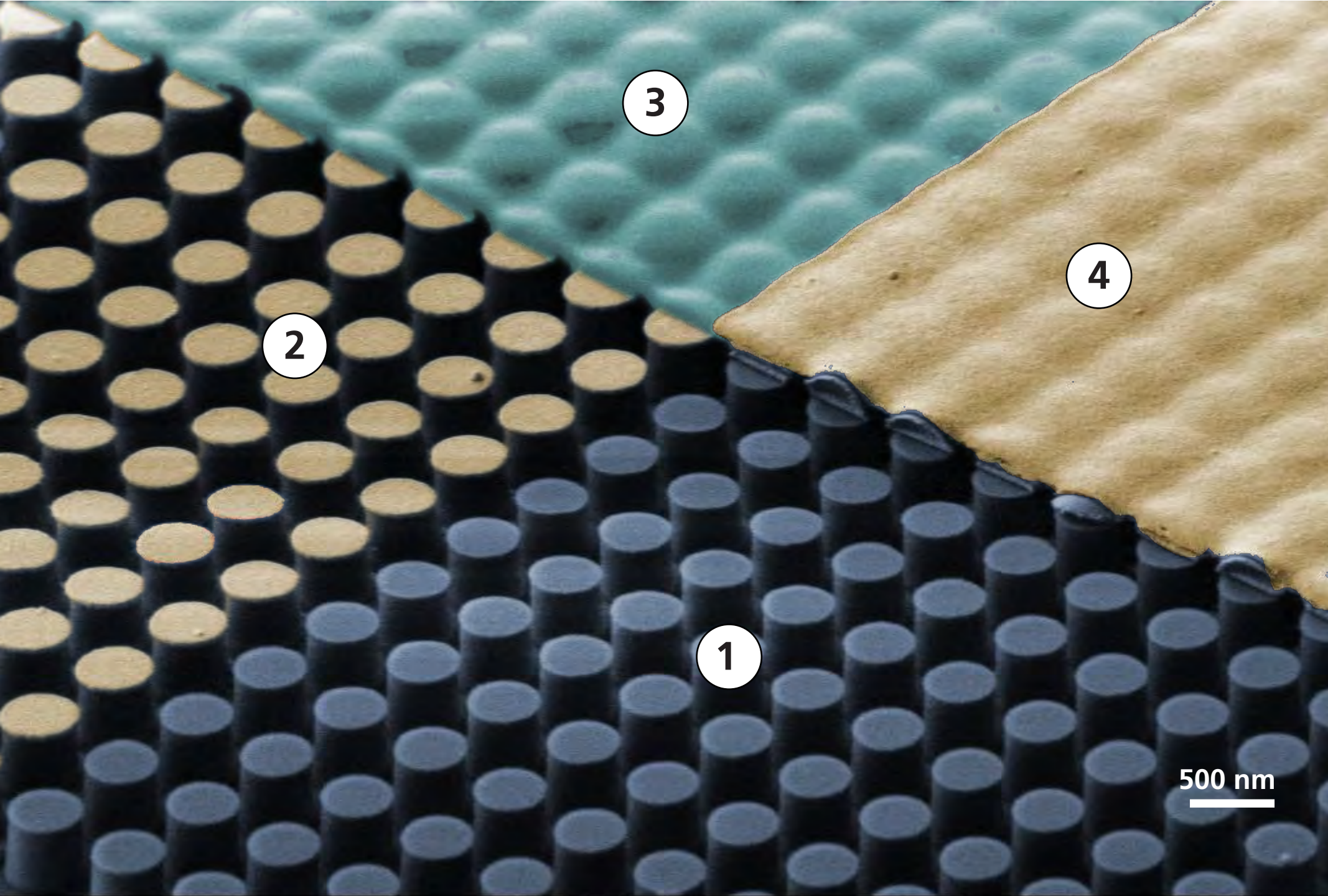


**1** index

**2** zero index

**3** experiments



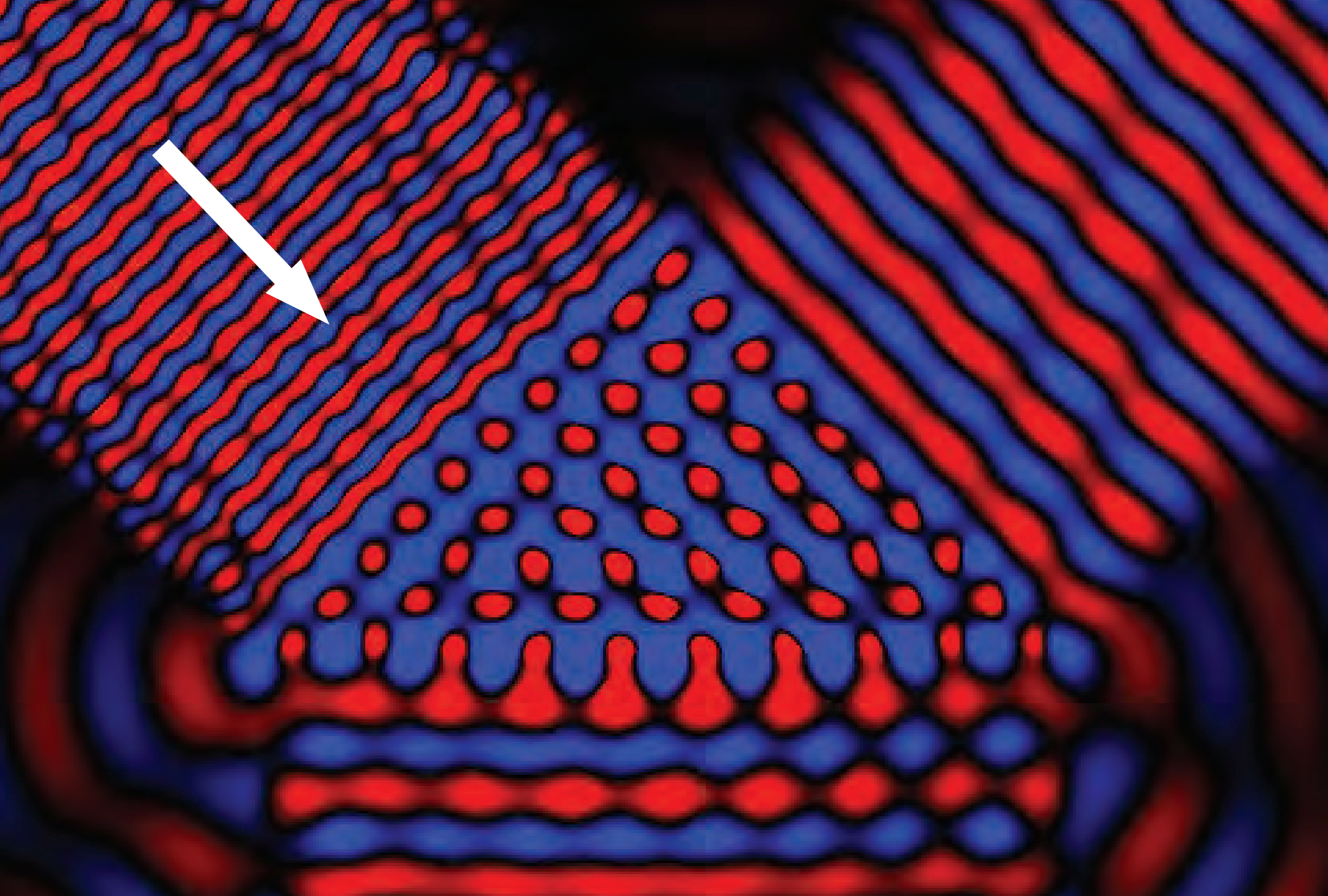


500 nm

1 index

2 zero index

3 experiments



1 index

2 zero index

3 experiments

# On-chip zero-index prism

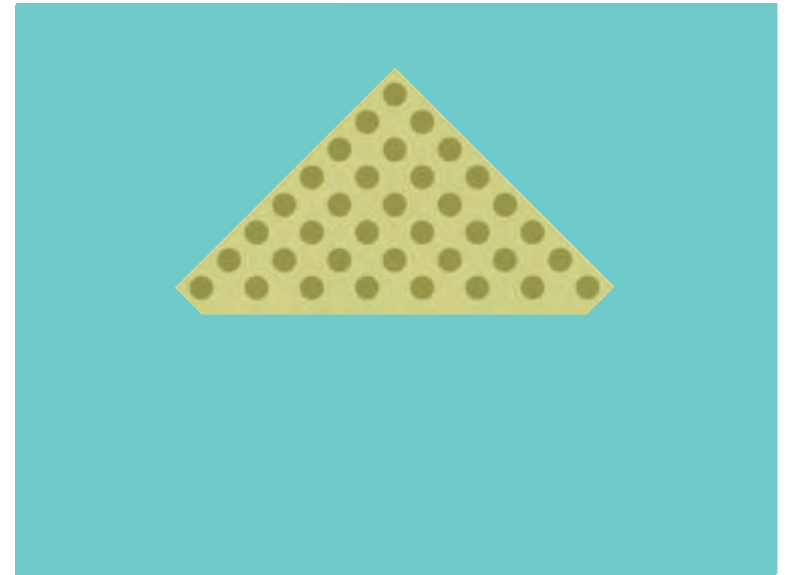


1 index

2 zero index

3 experiments

# On-chip zero-index prism

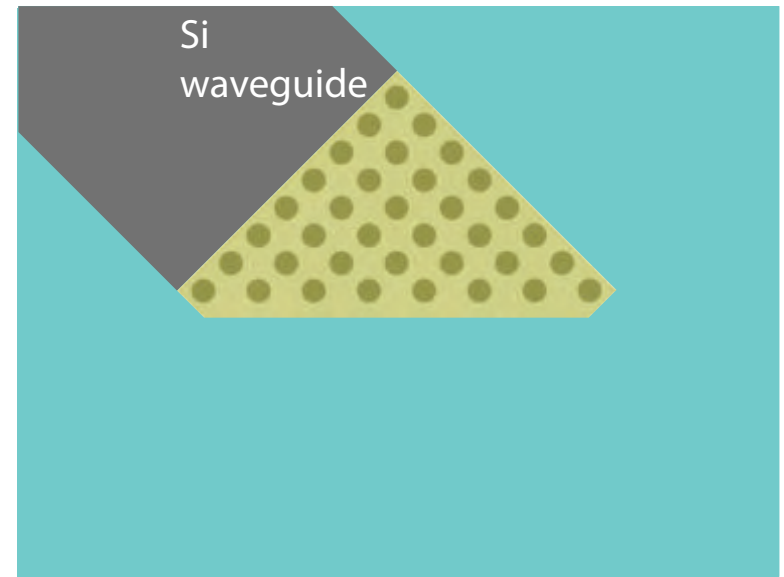


1 index

2 zero index

3 experiments

# On-chip zero-index prism



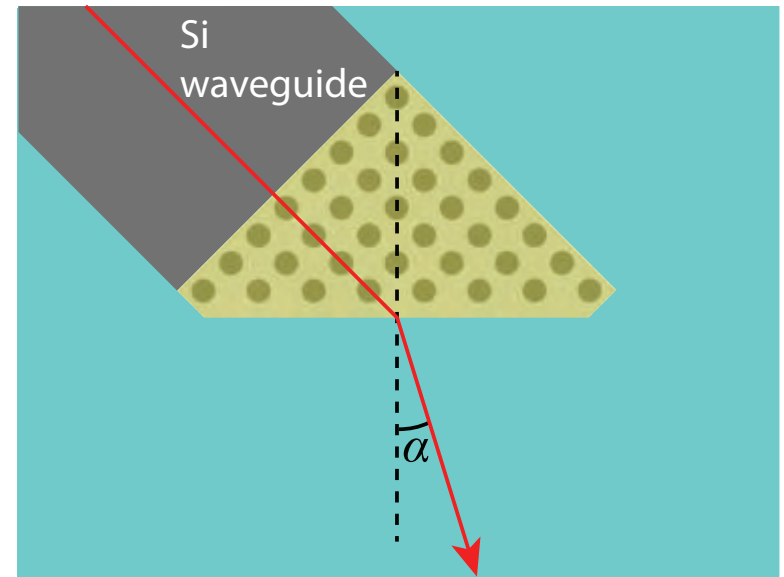
1 index

2 zero index

3 experiments



# On-chip zero-index prism

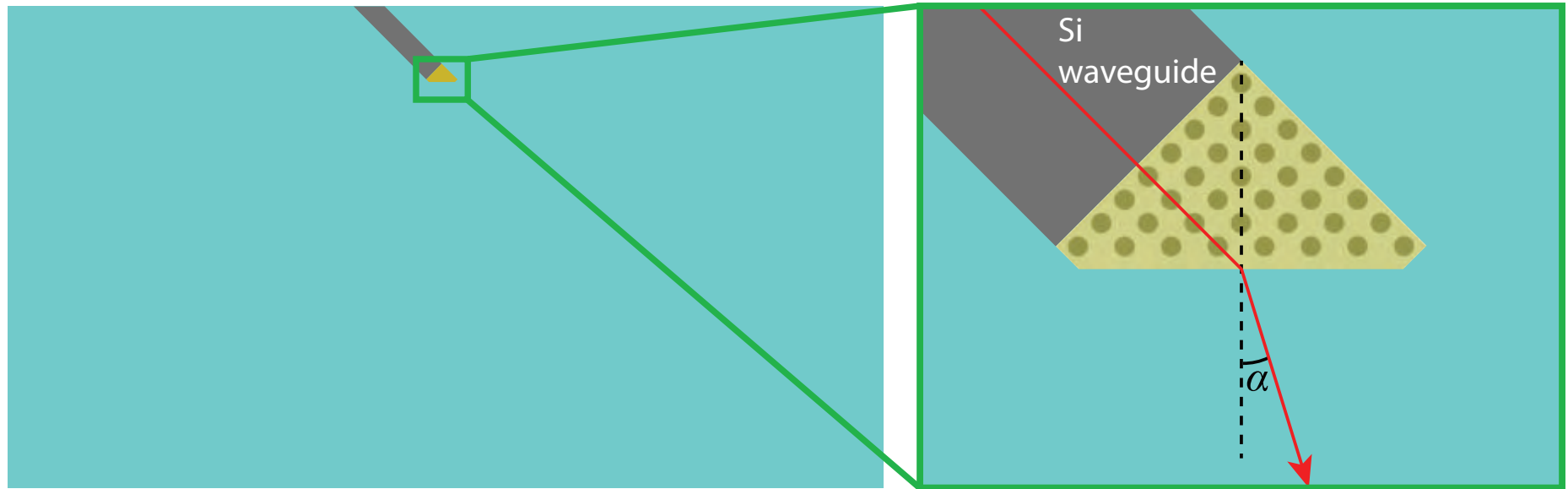


1 index

2 zero index

3 experiments

# On-chip zero-index prism

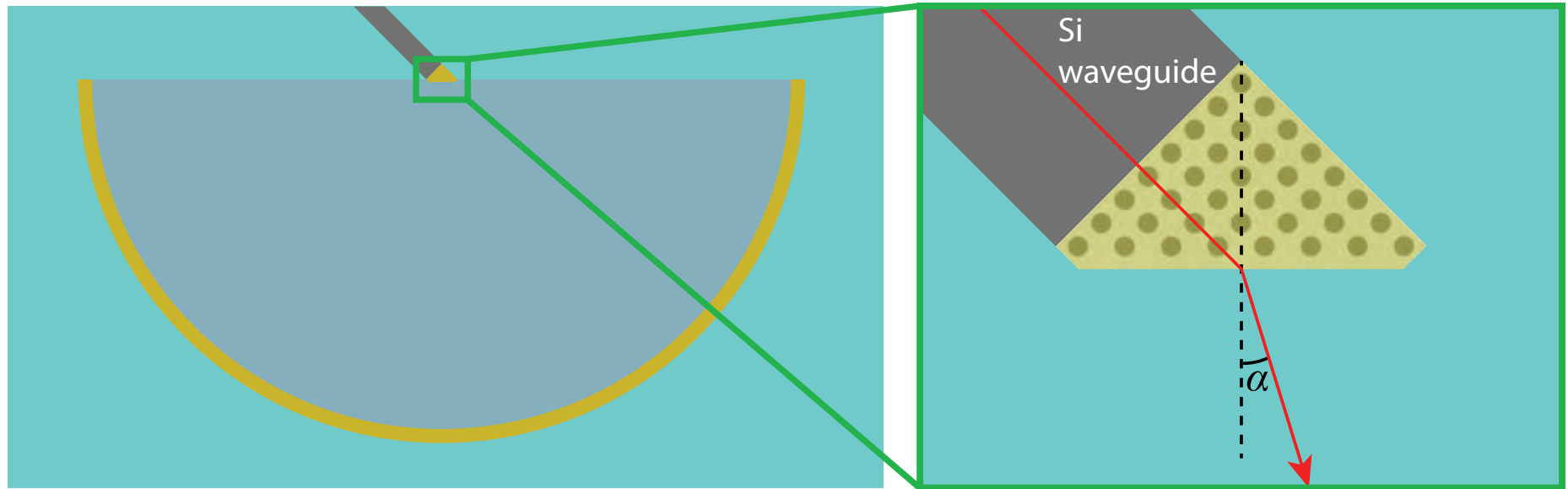


1 index

2 zero index

3 experiments

# On-chip zero-index prism

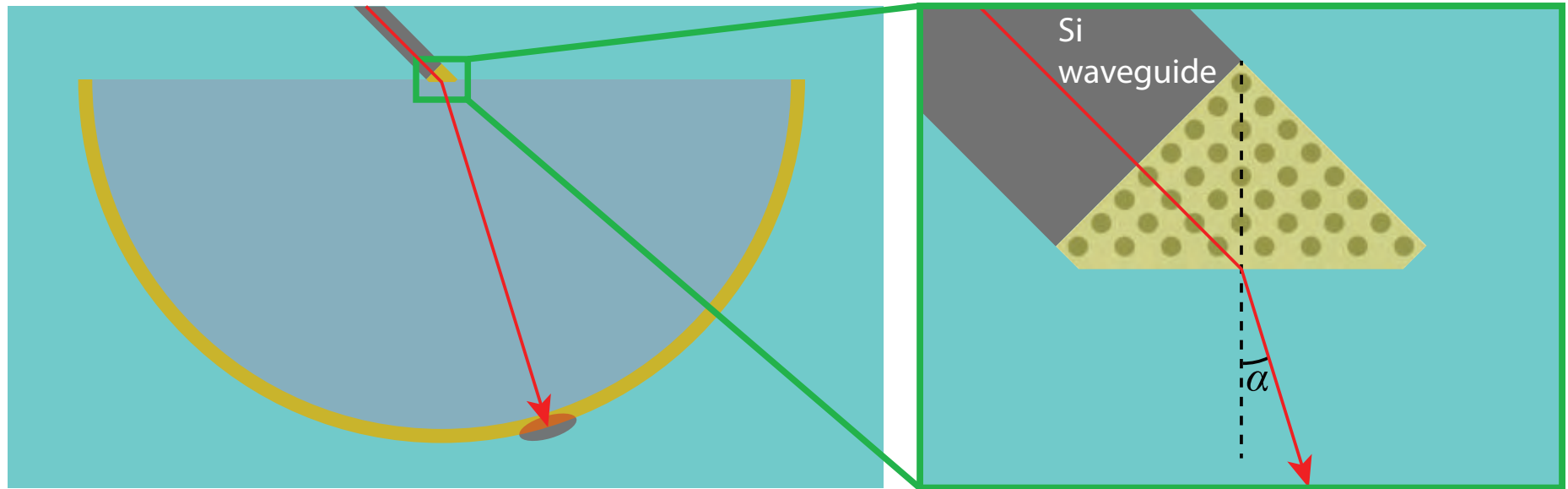


1 index

2 zero index

3 experiments

# On-chip zero-index prism

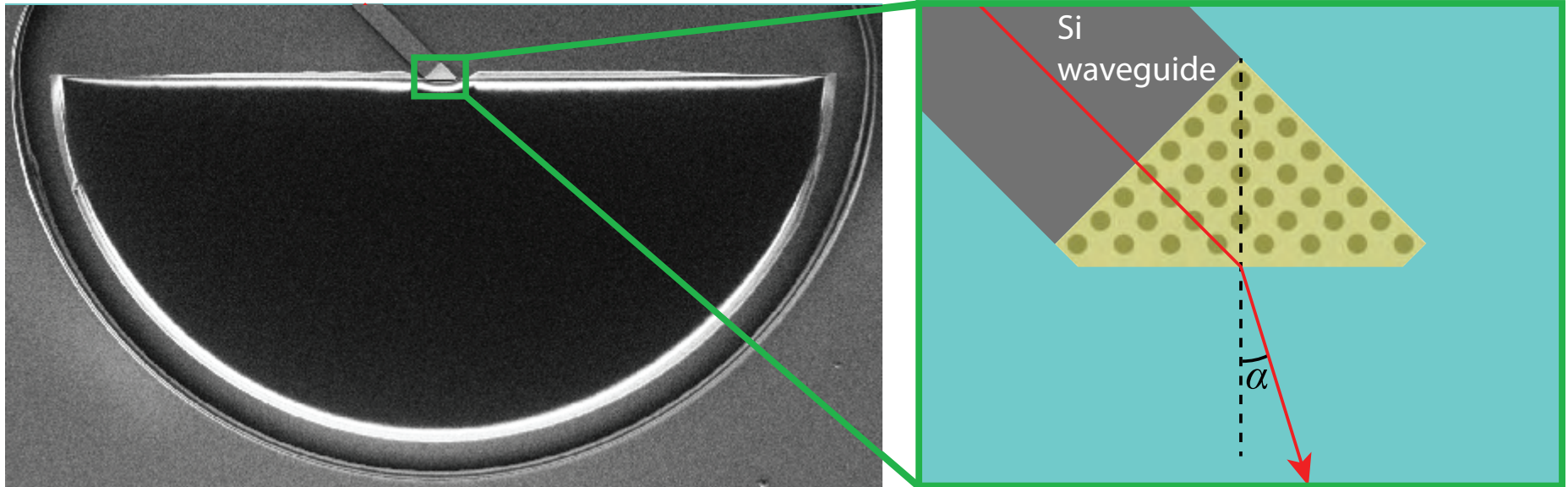


1 index

2 zero index

3 experiments

# On-chip zero-index prism

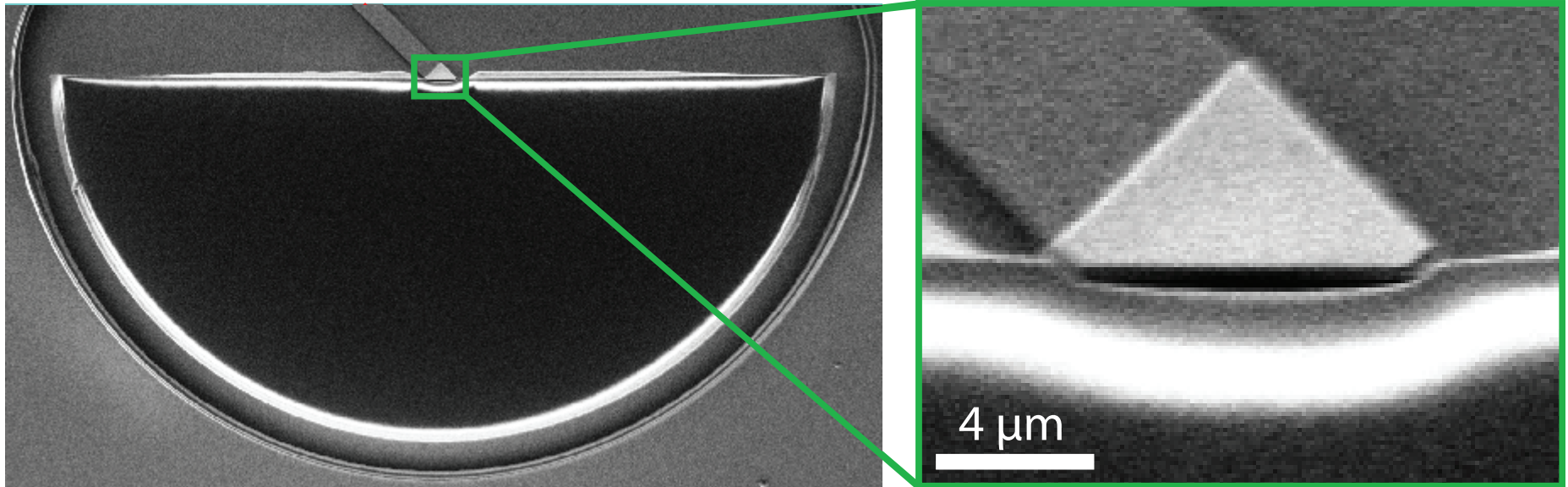


1 index

2 zero index

3 experiments

# On-chip zero-index prism

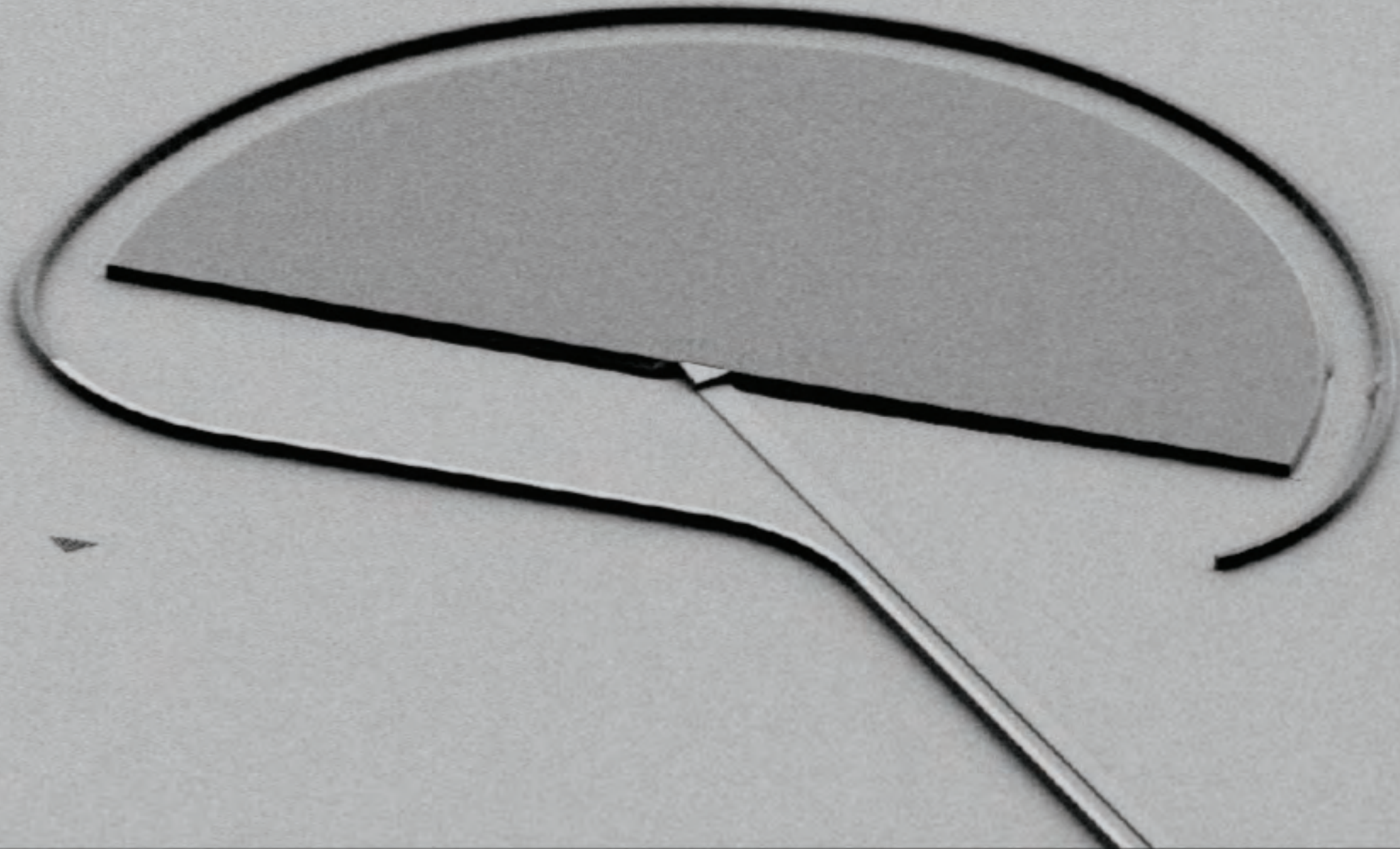


1 index

2 zero index

3 experiments



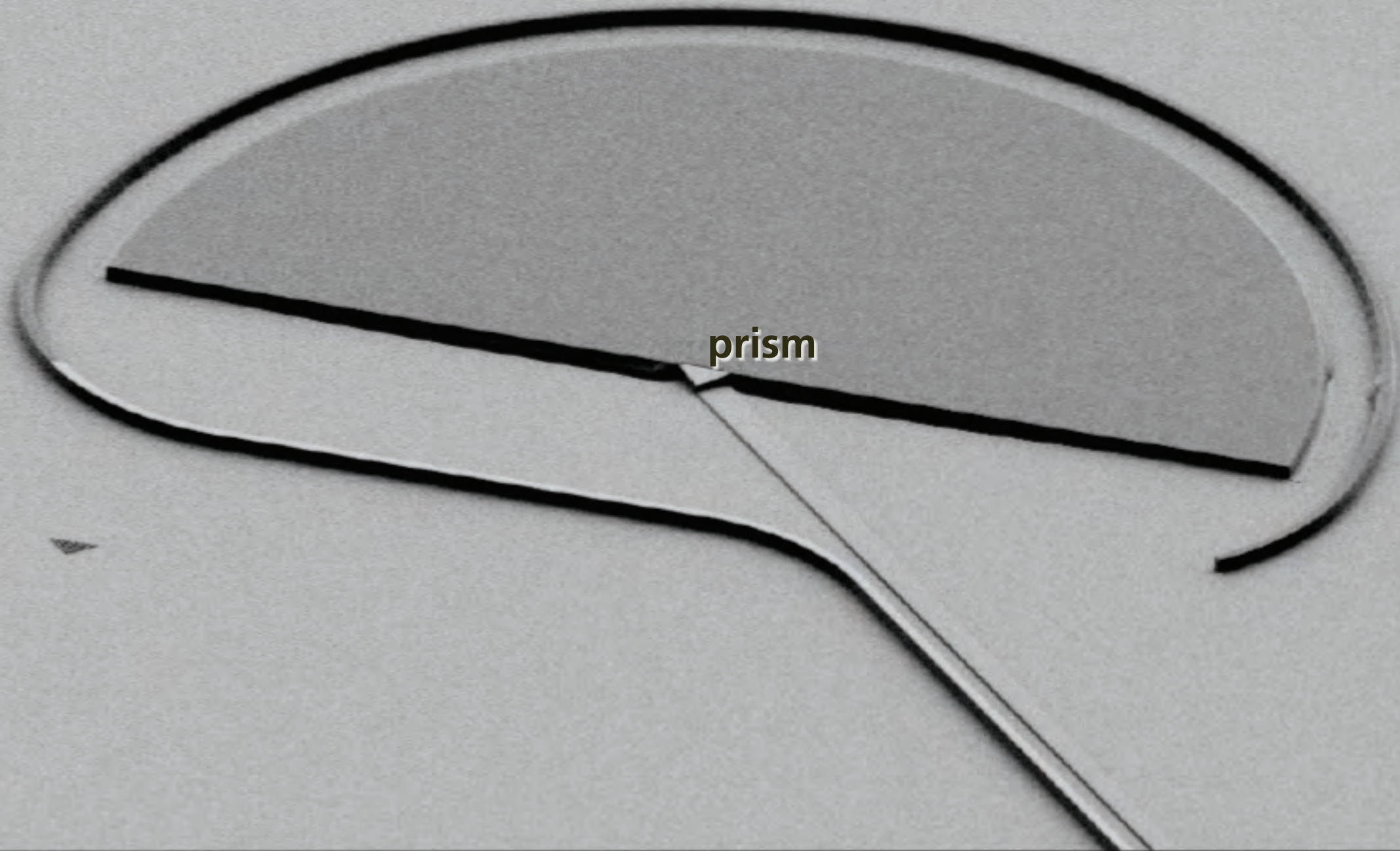


**1** index

**2** zero index

**3** experiments



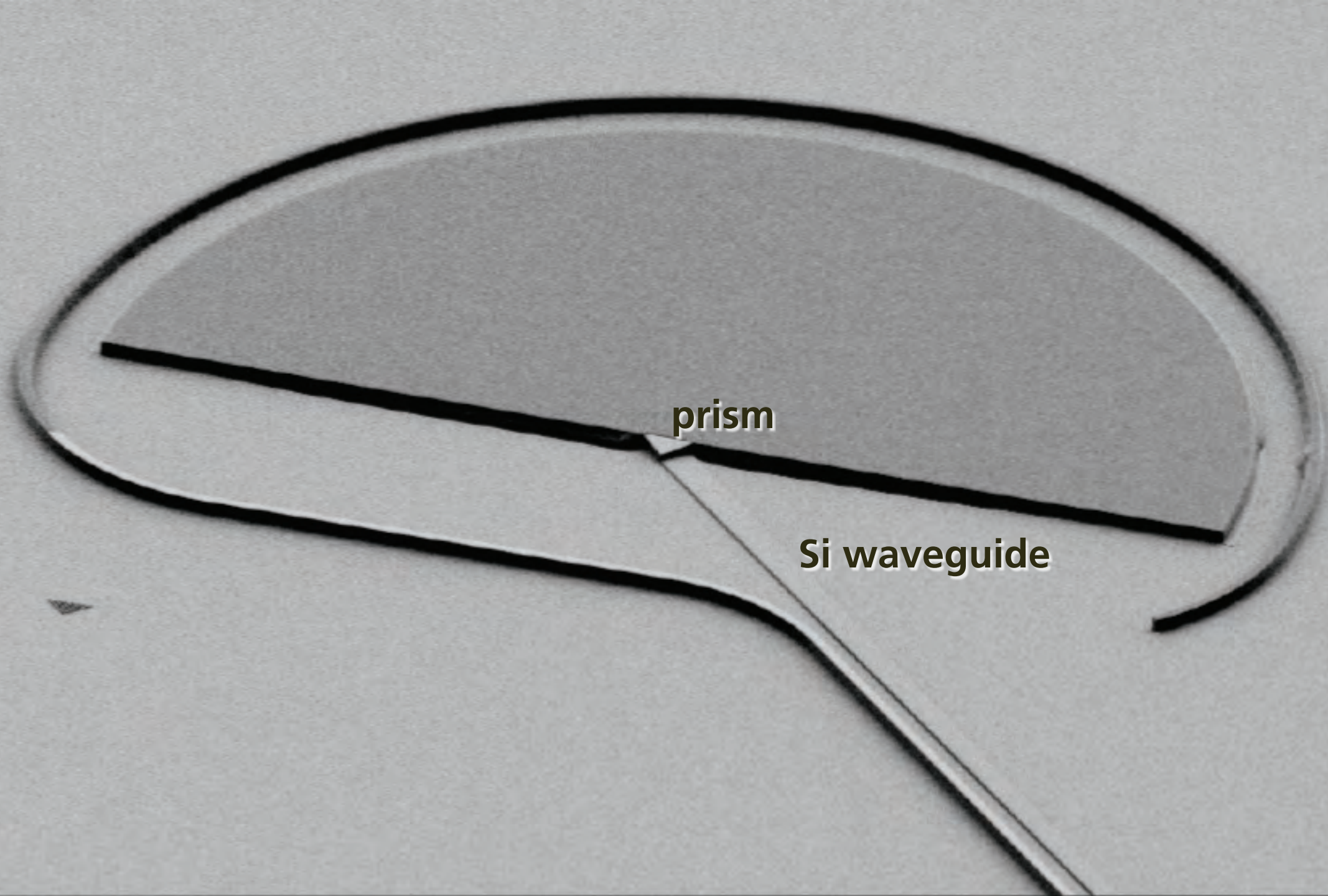


1 index

2 zero index

3 experiments





prism

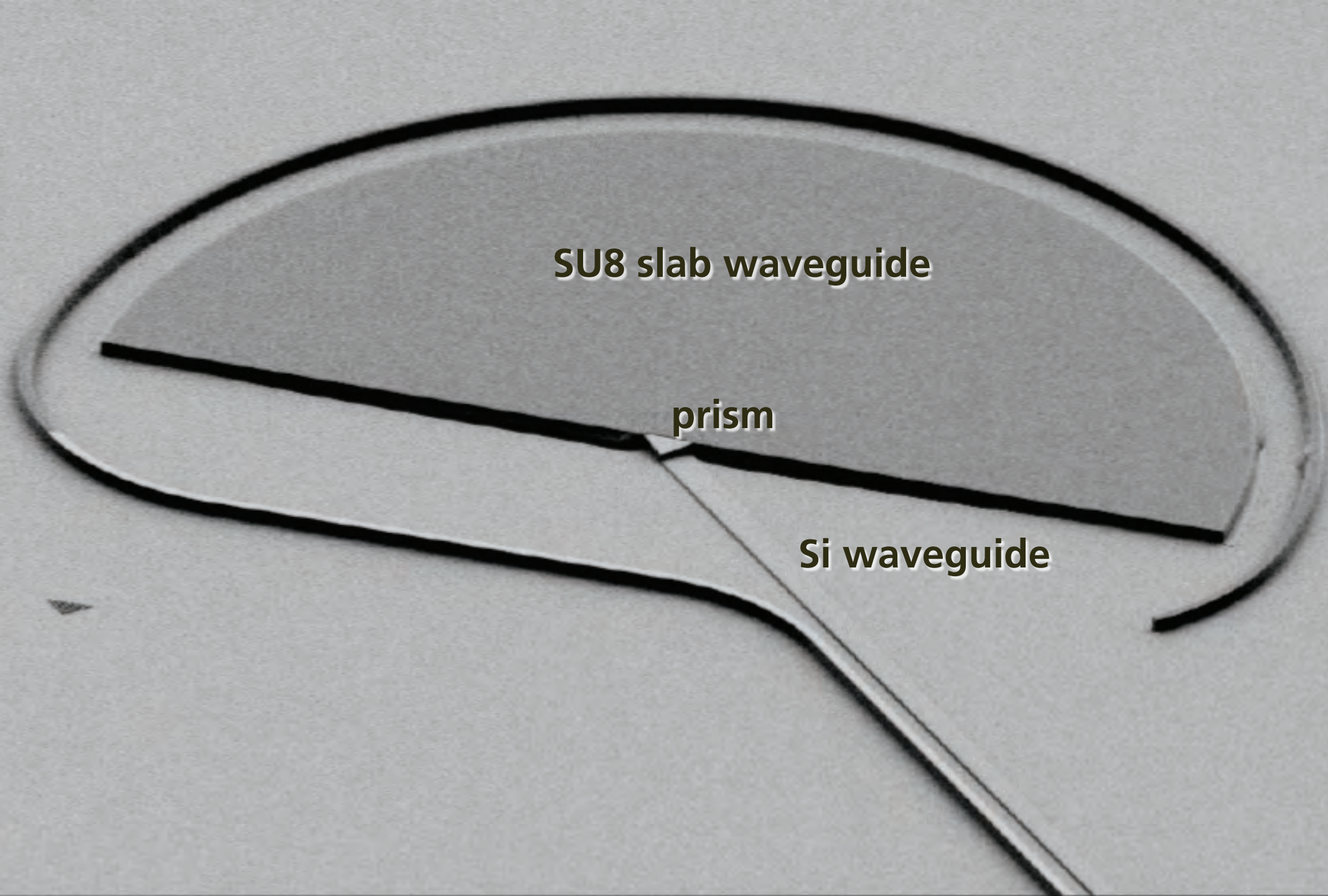
Si waveguide

1 index

2 zero index

3 experiments





SU8 slab waveguide

prism

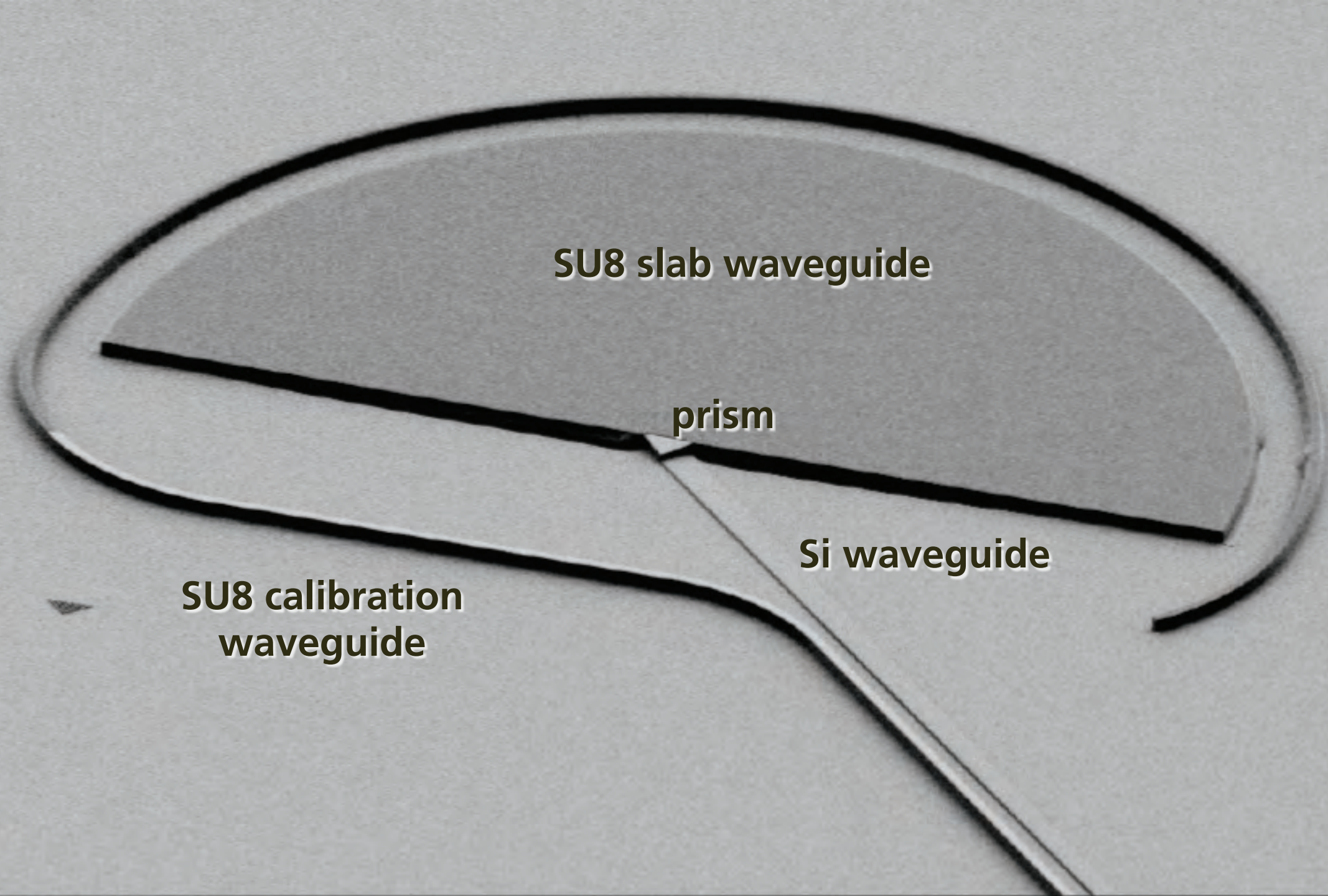
Si waveguide

1 index

2 zero index

3 experiments





SU8 slab waveguide

prism

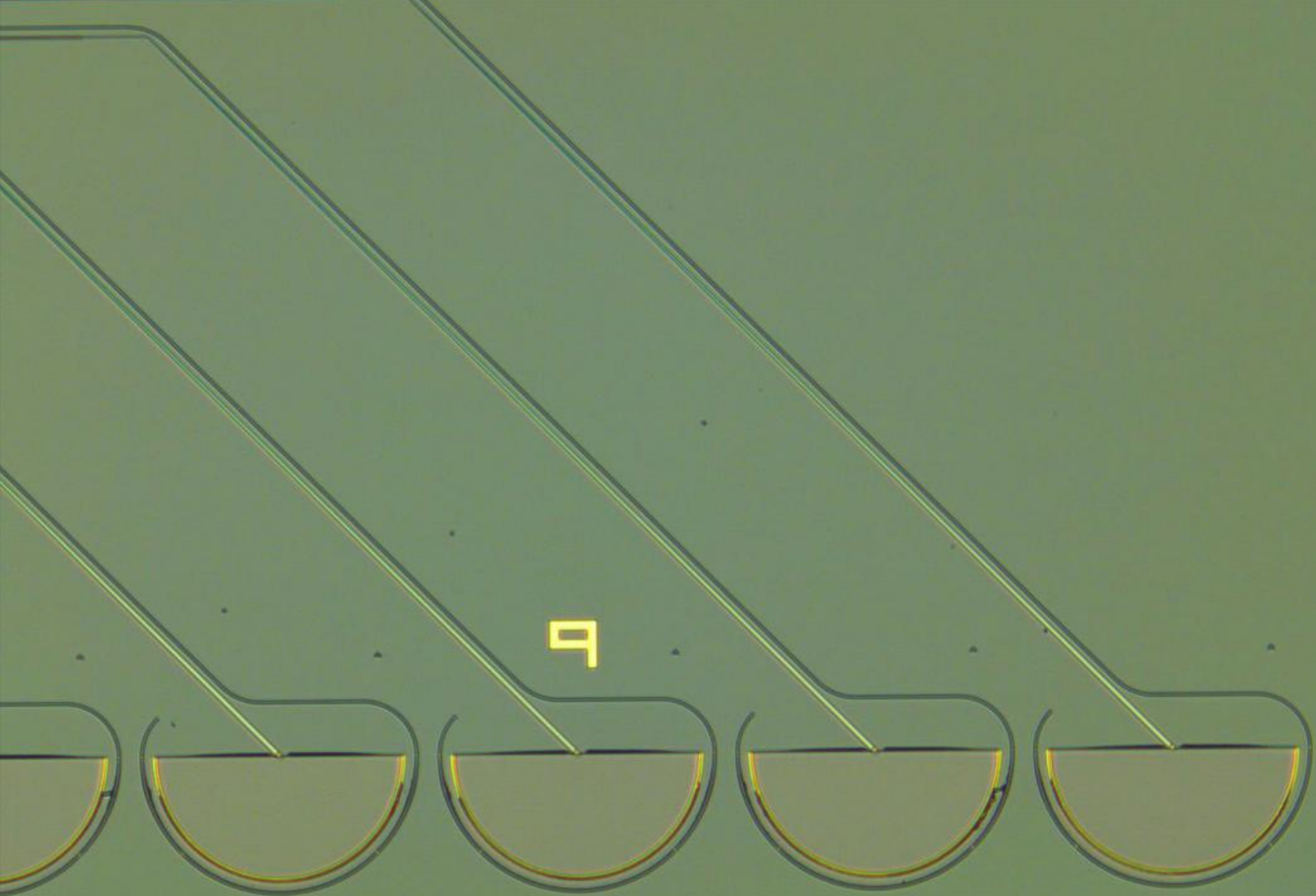
Si waveguide

SU8 calibration  
waveguide

1 index

2 zero index

3 experiments



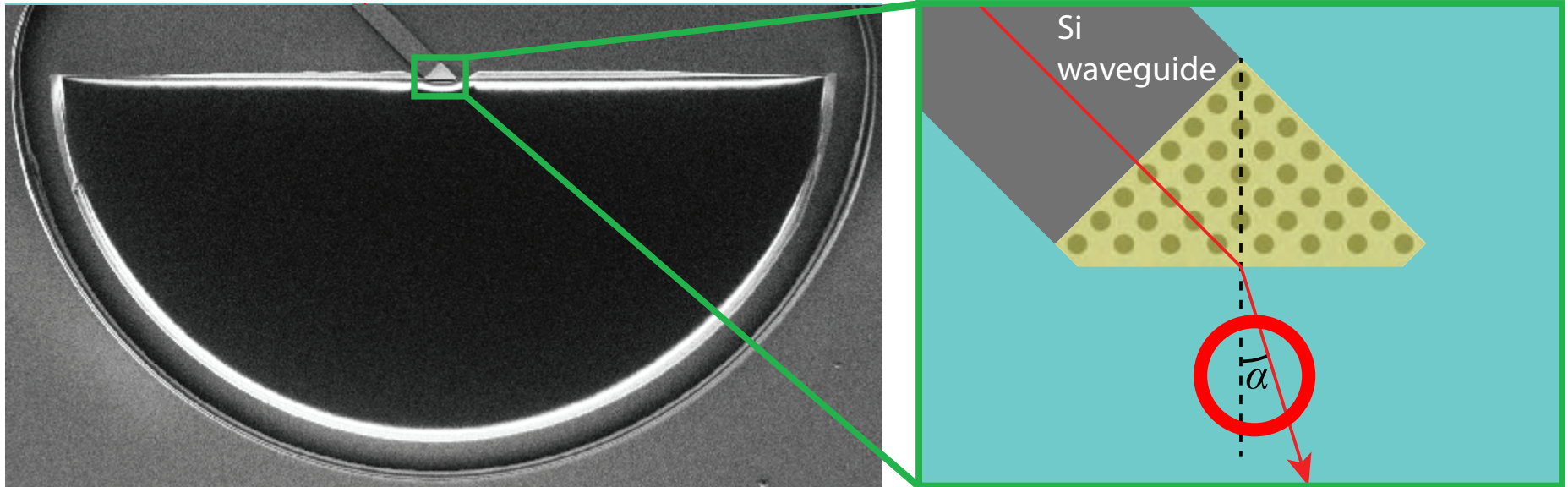
1 index

2 zero index

3 experiments



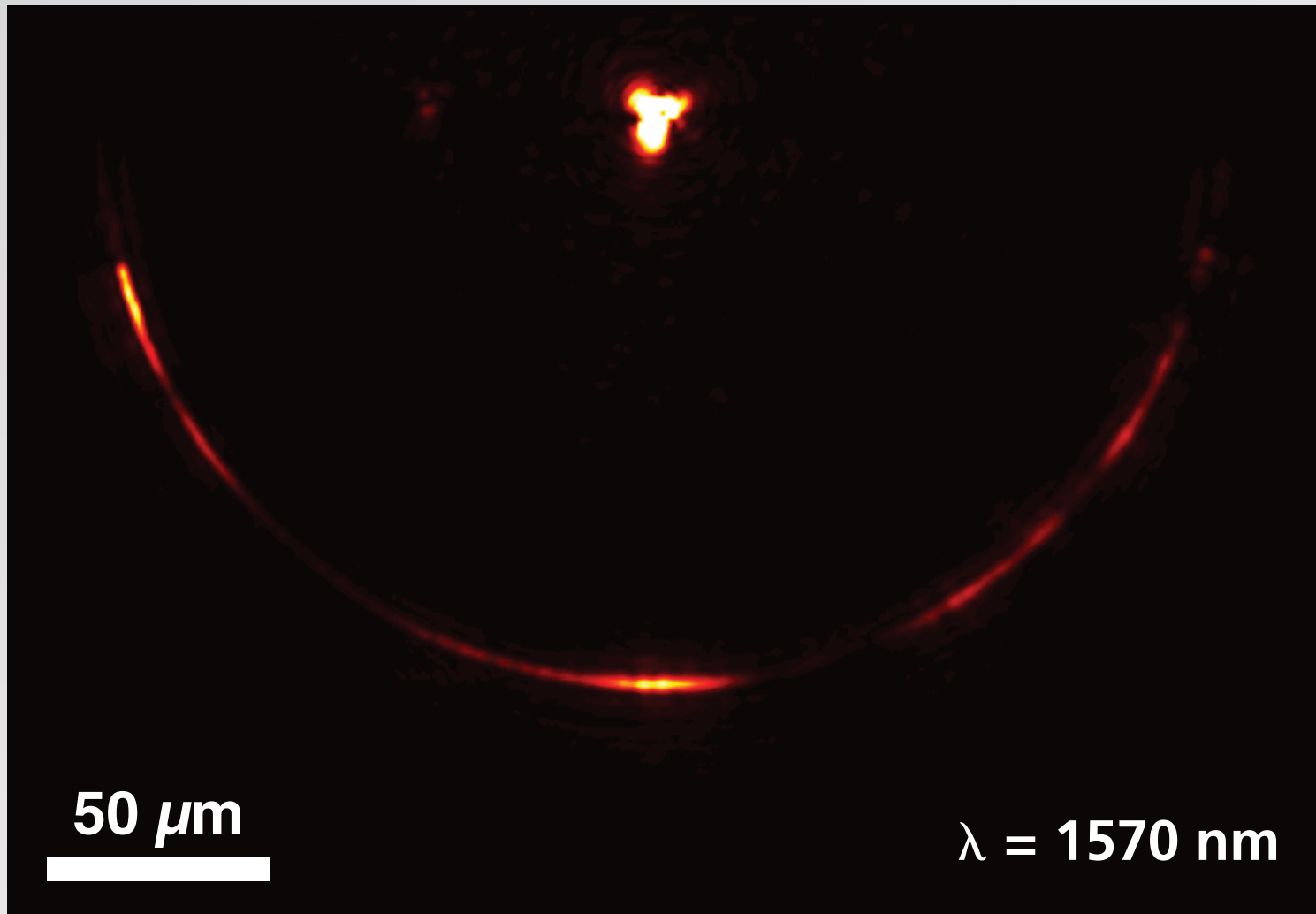
# On-chip zero-index prism



1 index

2 zero index

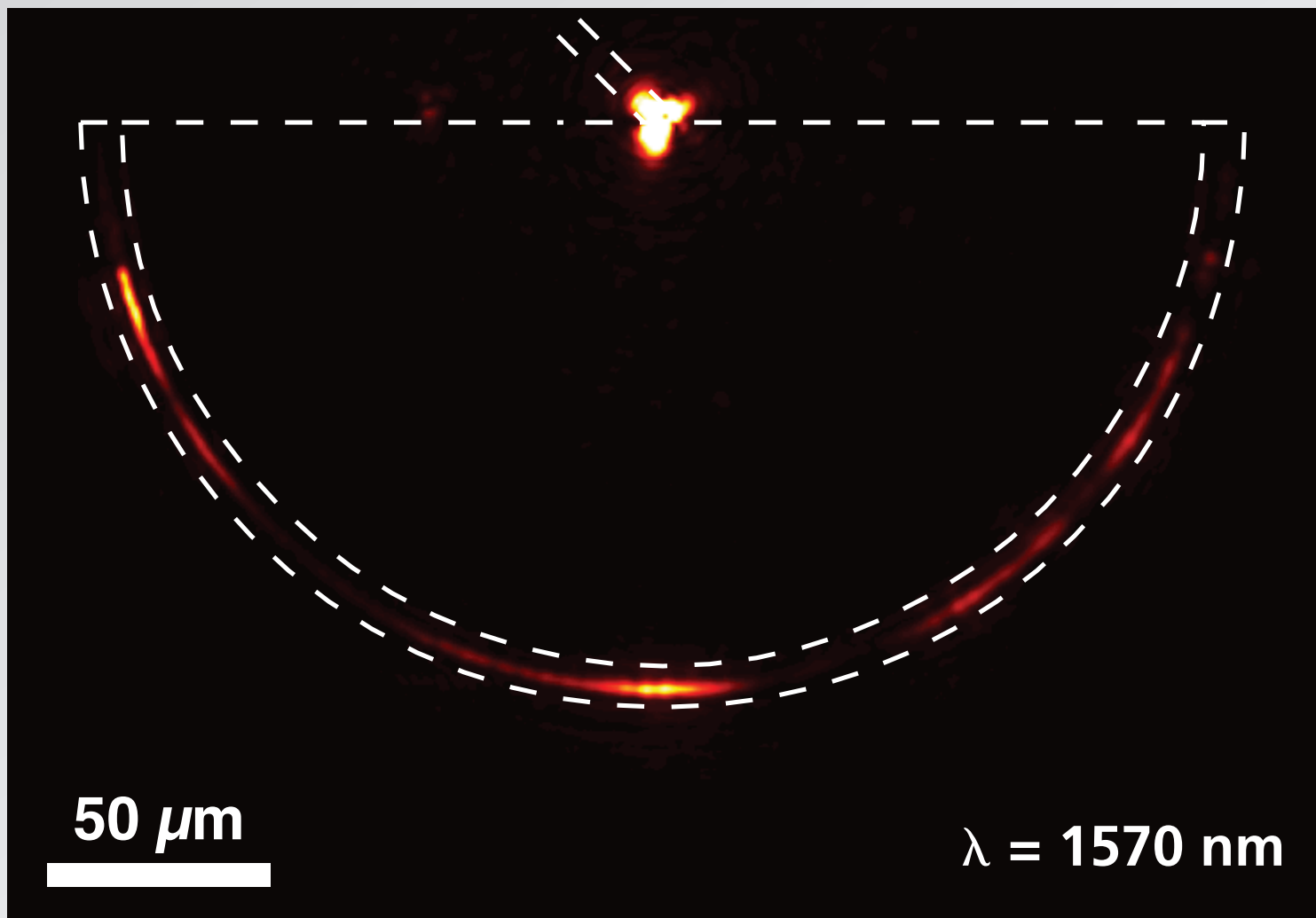
3 experiments



1 index

2 zero index

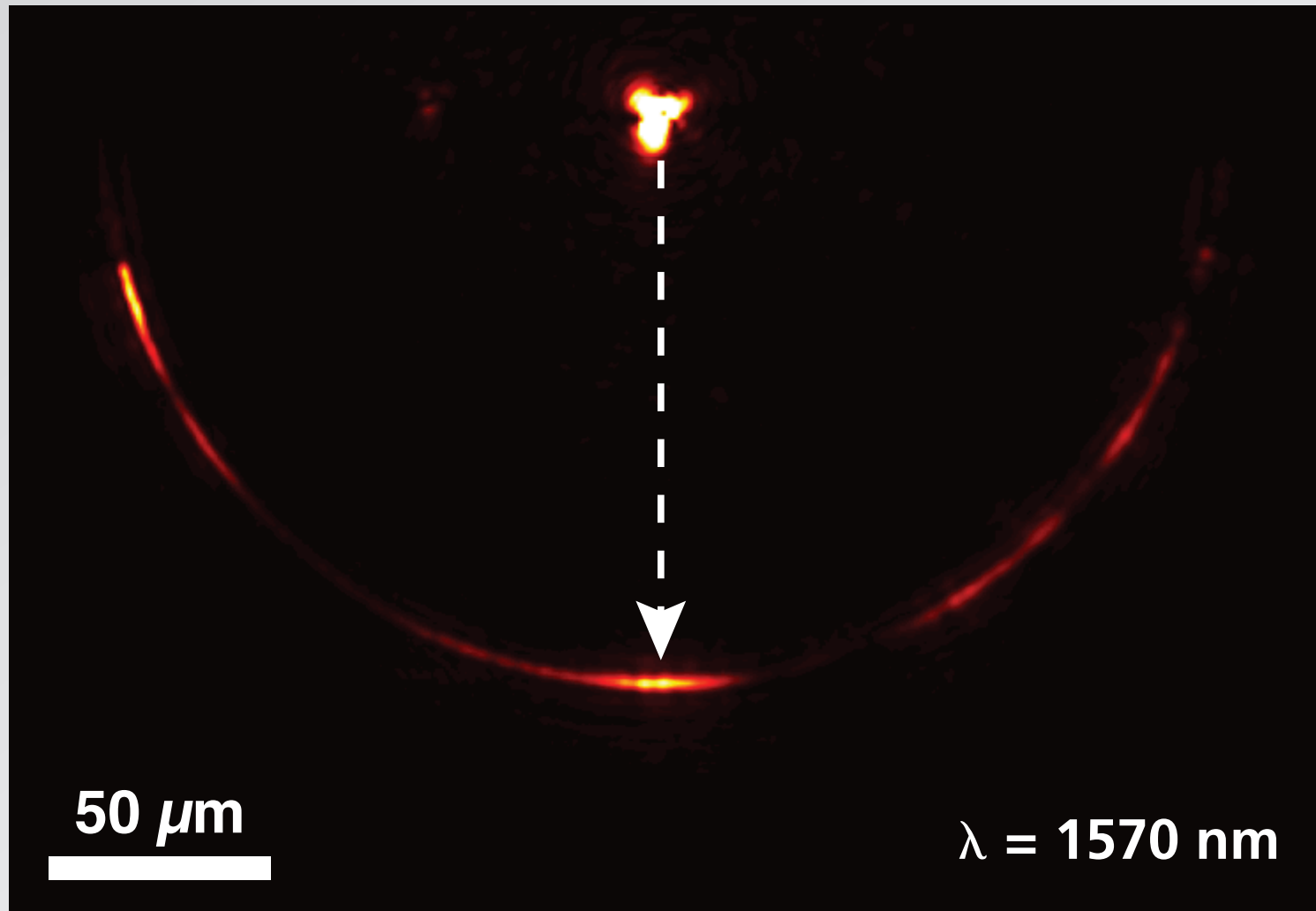
3 experiments



1 index

2 zero index

3 experiments

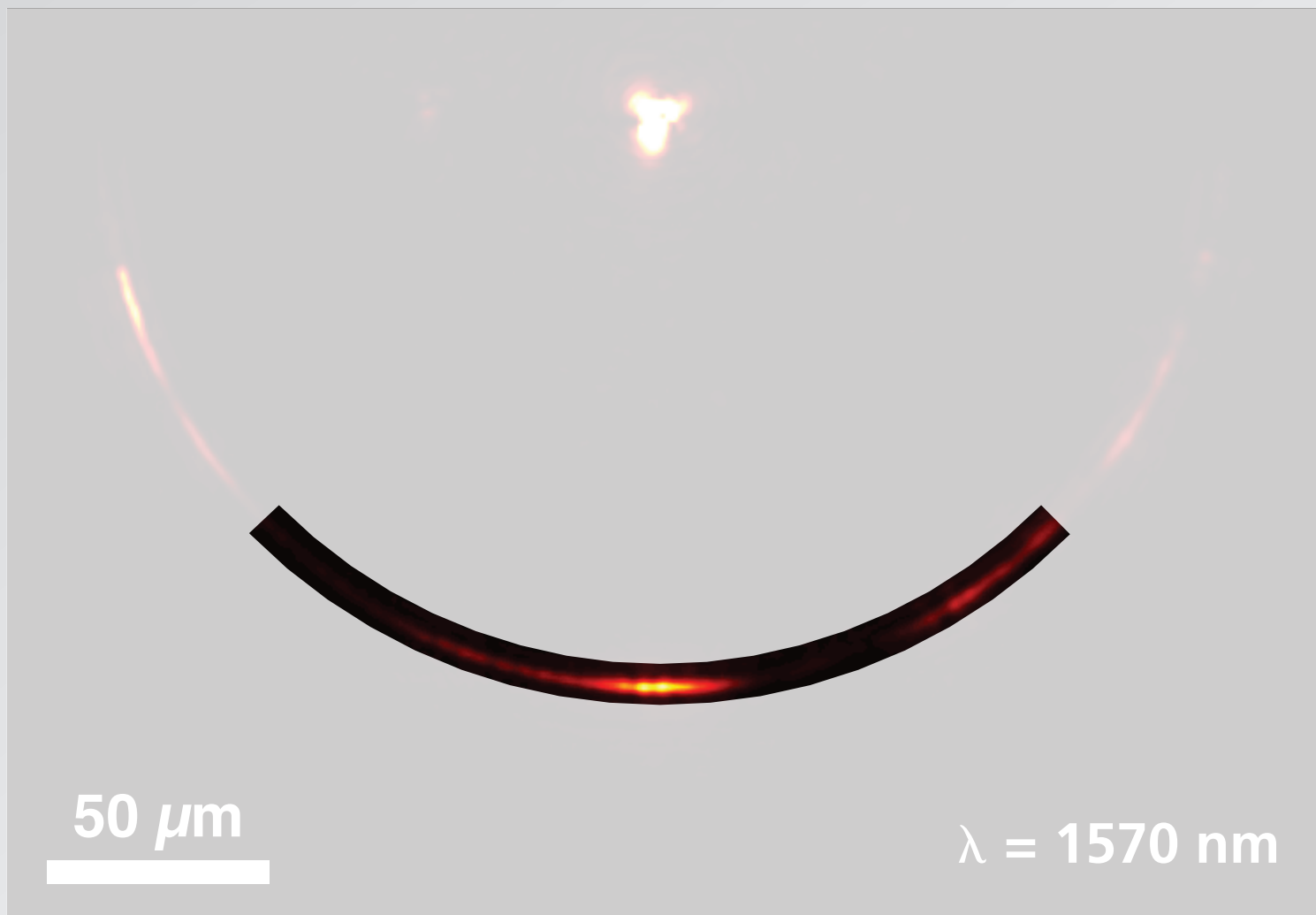


1 index

2 zero index

3 experiments



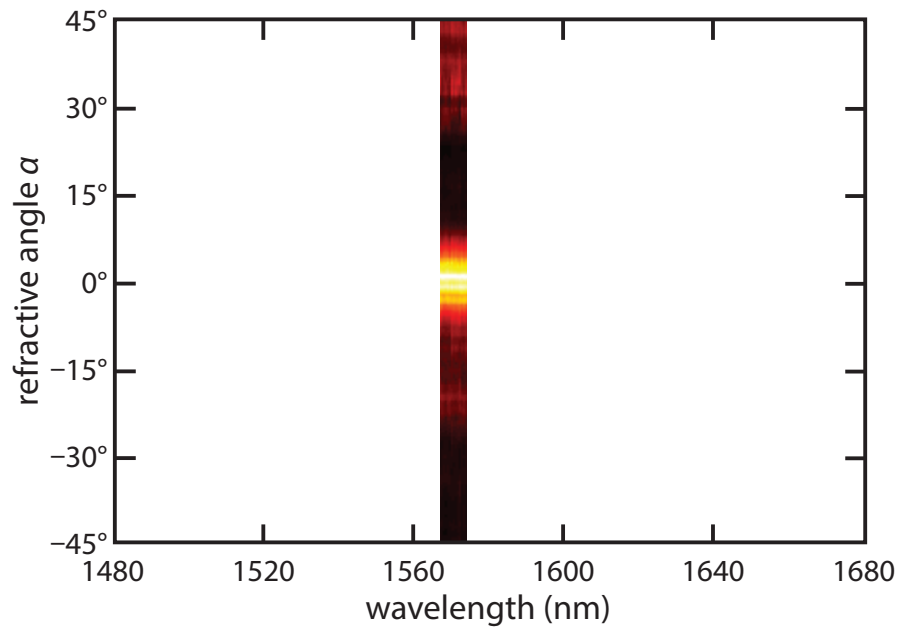


1 index

2 zero index

3 experiments

# Wavelength dependence of refraction angle

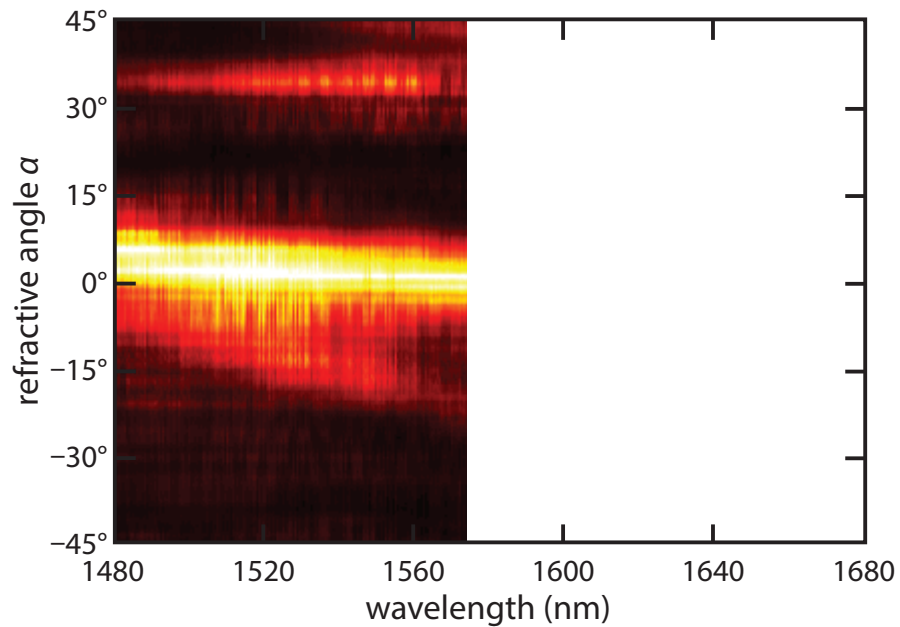


1 index

2 zero index

3 experiments

# Wavelength dependence of refraction angle

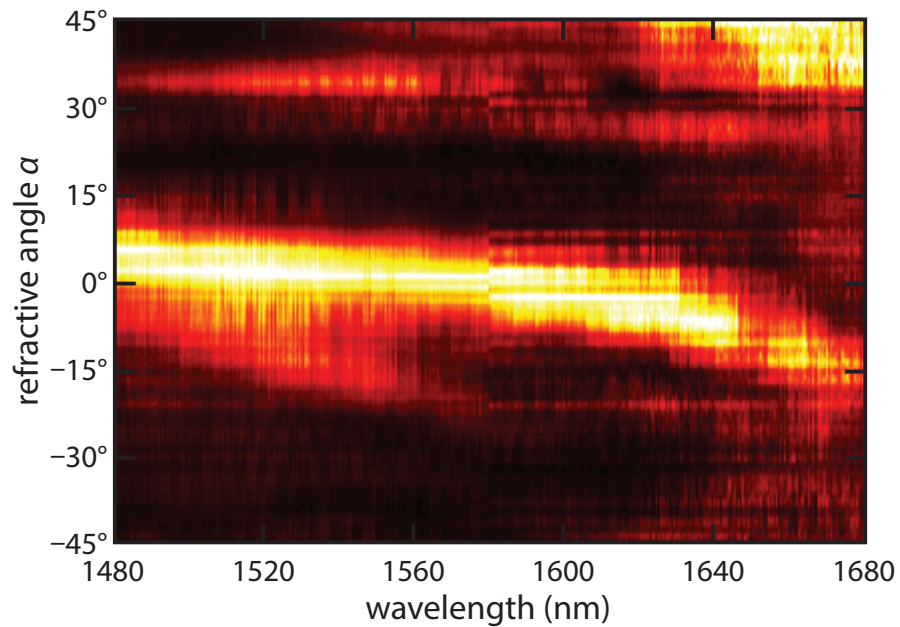


1 index

2 zero index

3 experiments

# Wavelength dependence of refraction angle

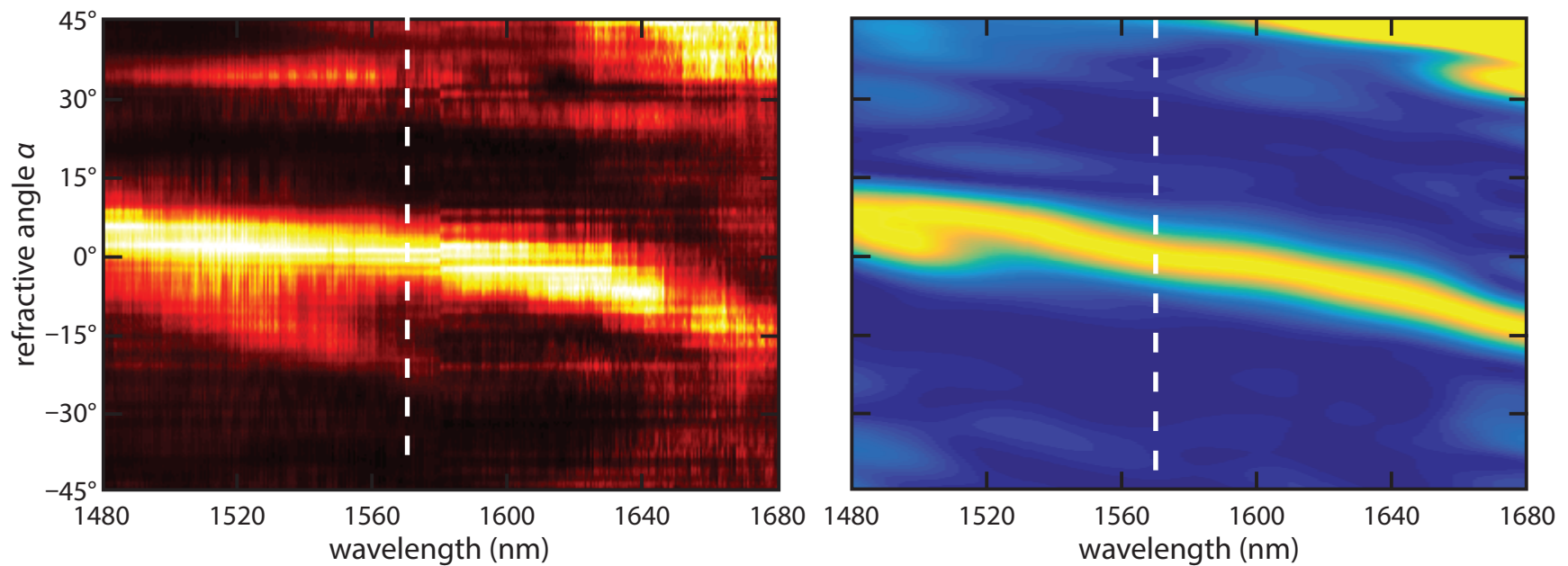


1 index

2 zero index

3 experiments

# Wavelength dependence of refraction angle

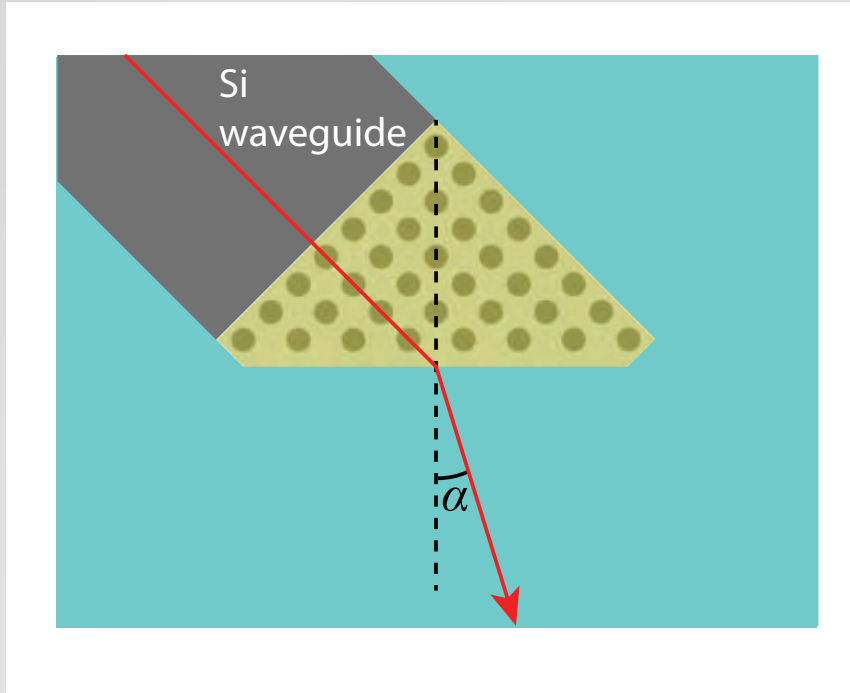


1 index

2 zero index

3 experiments

# Wavelength dependence of index



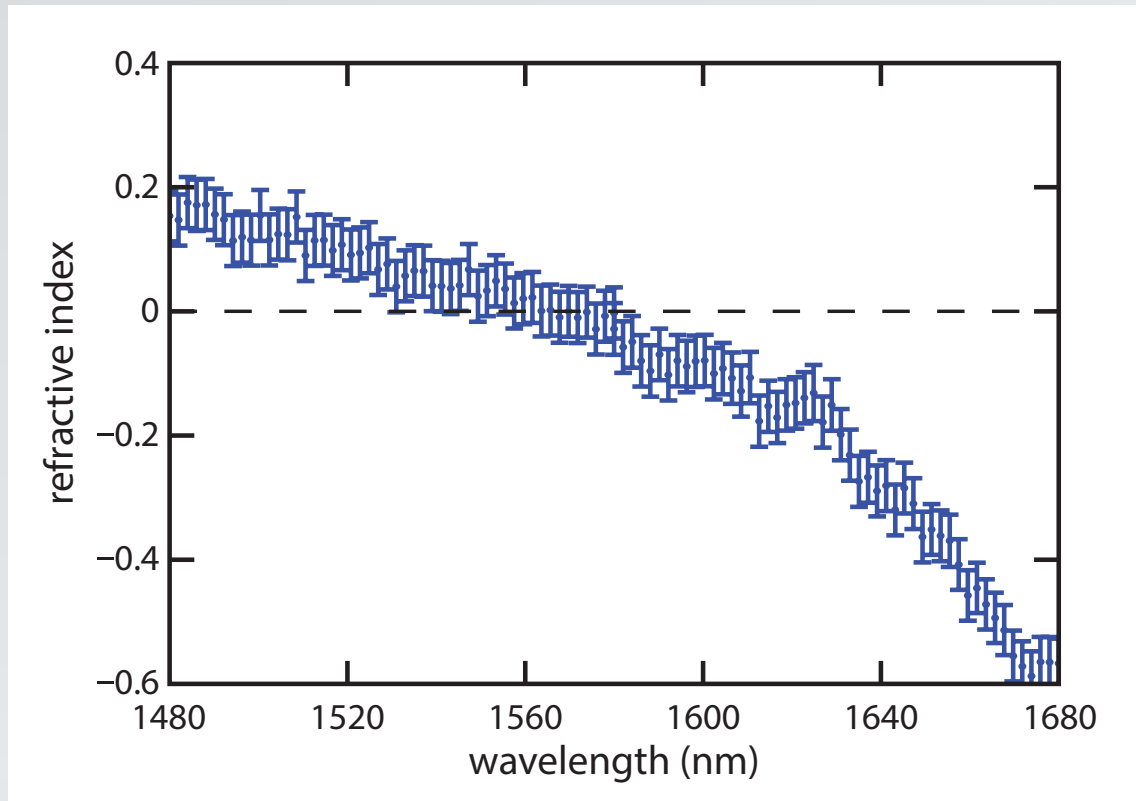
$$n_{\text{prism}} = n_{\text{slab}} \frac{\sin \alpha}{\sin 45^\circ}$$

1 index

2 zero index

3 experiments

# Wavelength dependence of index

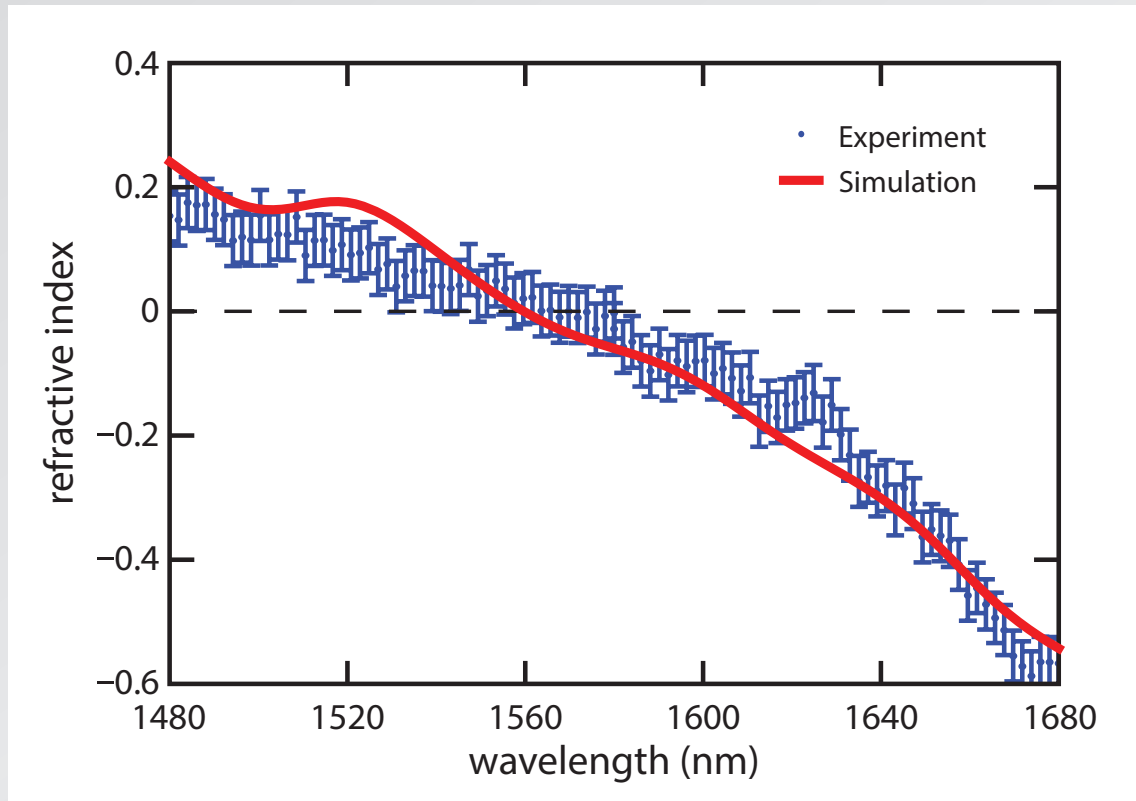


1 index

2 zero index

3 experiments

# Wavelength dependence of index



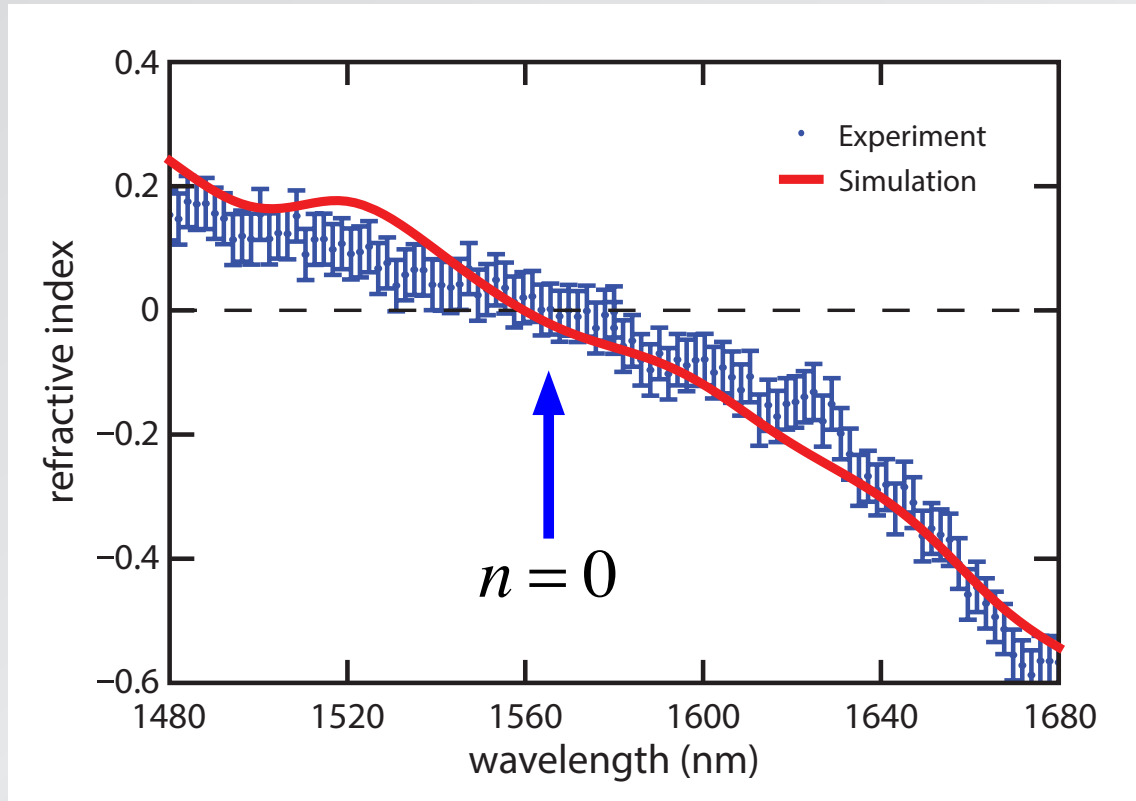
1 index

2 zero index

3 experiments



# Wavelength dependence of index

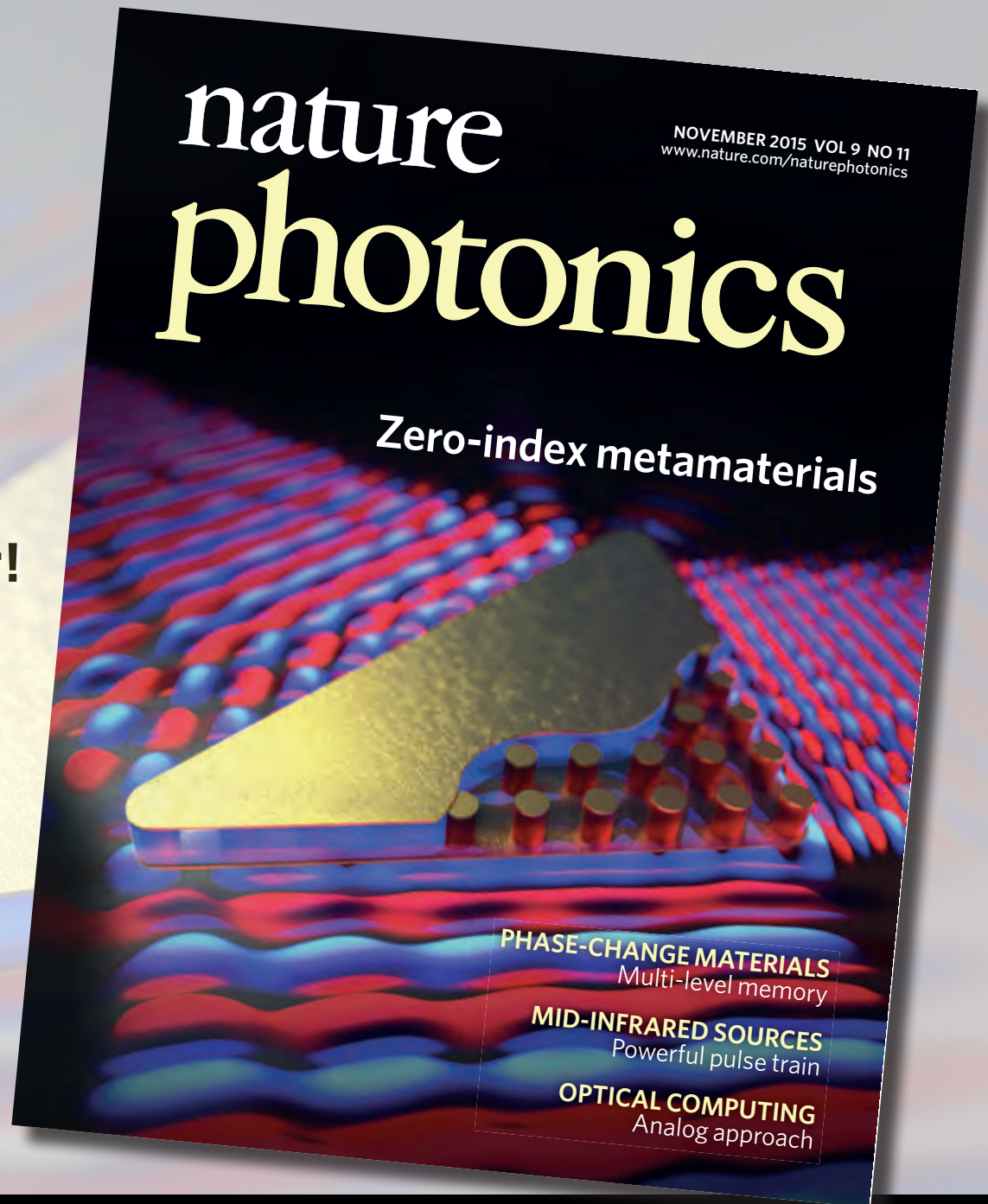


1 index

2 zero index

3 experiments

More info: download paper!

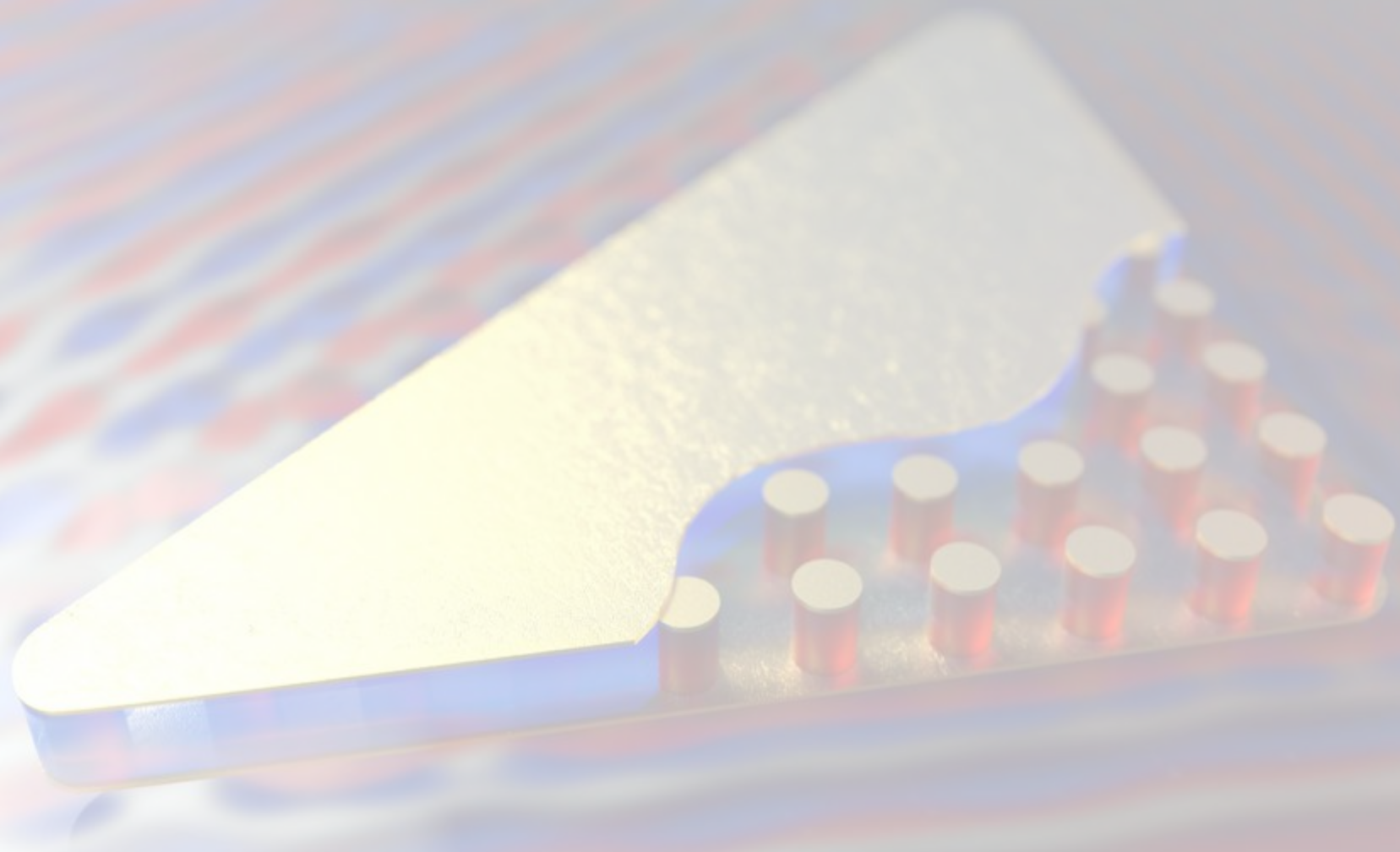


1 index

2 zero index

3 experiments

Where do we go from here?



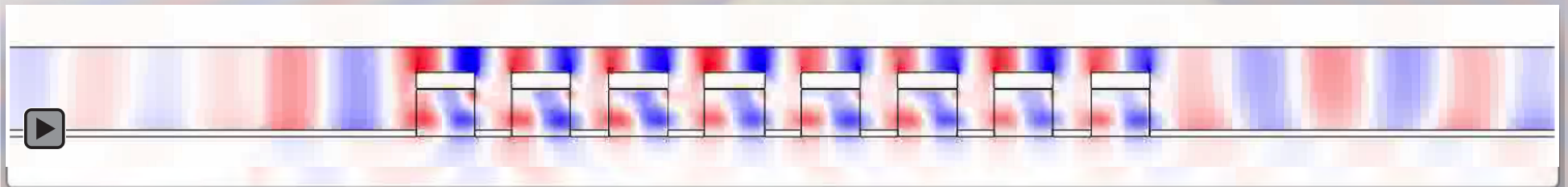
1 index

2 zero index

3 experiments



Where do we go from here?



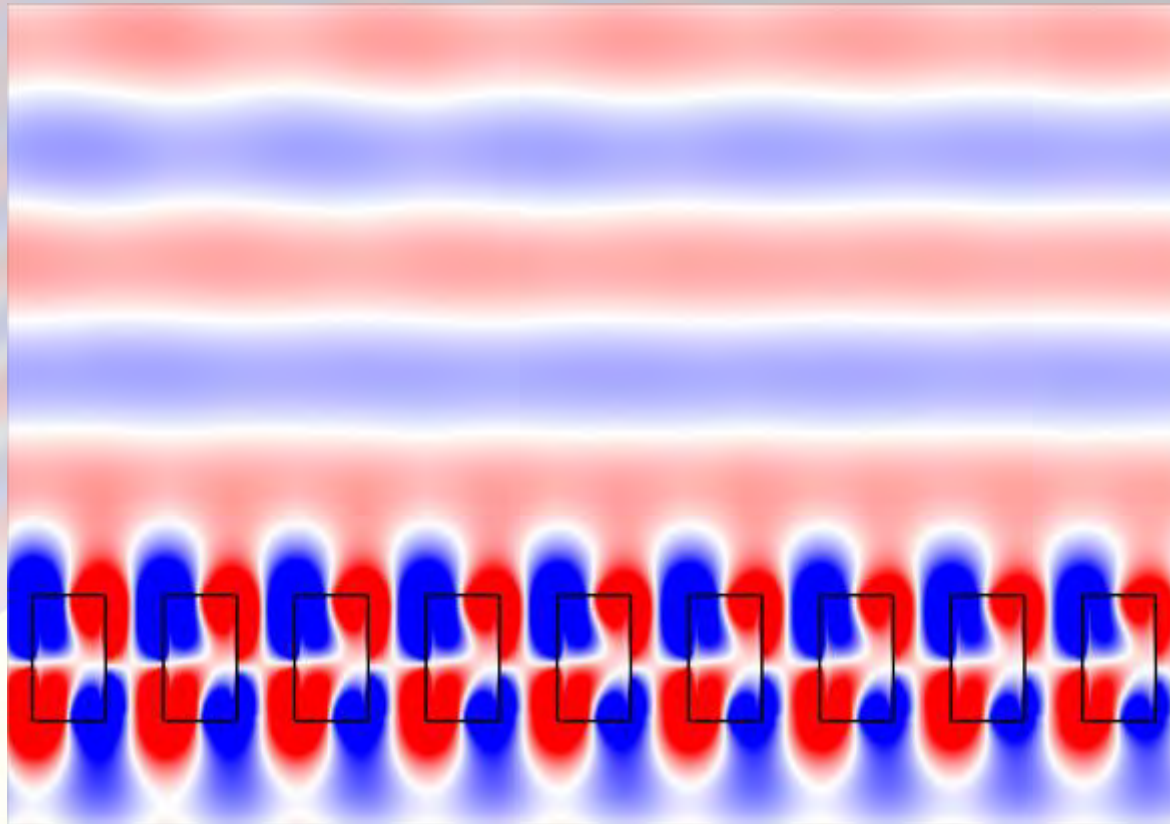
Need to eliminate losses in metal mirrors

1 index

2 zero index

3 experiments

Where do we go from here?



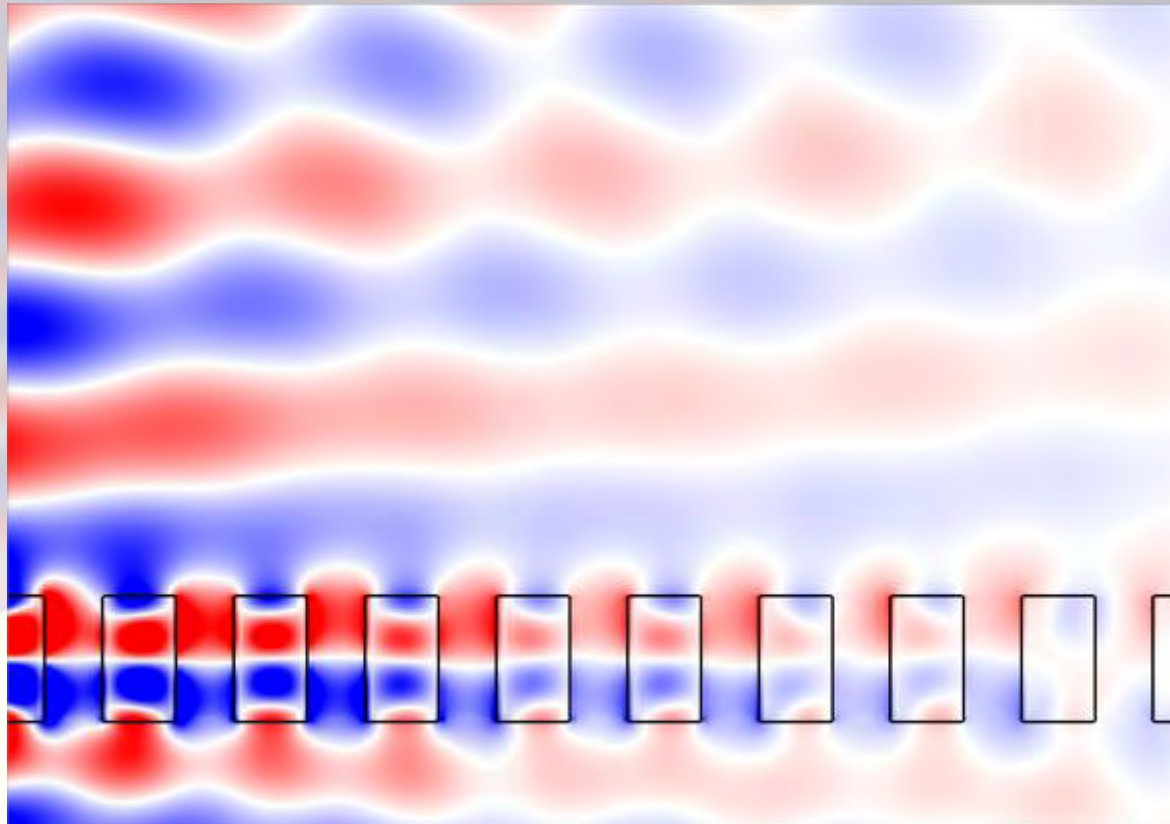
Removing mirrors causes radiative losses

1 index

2 zero index

3 experiments

Where do we go from here?



Radiative losses can be steered...

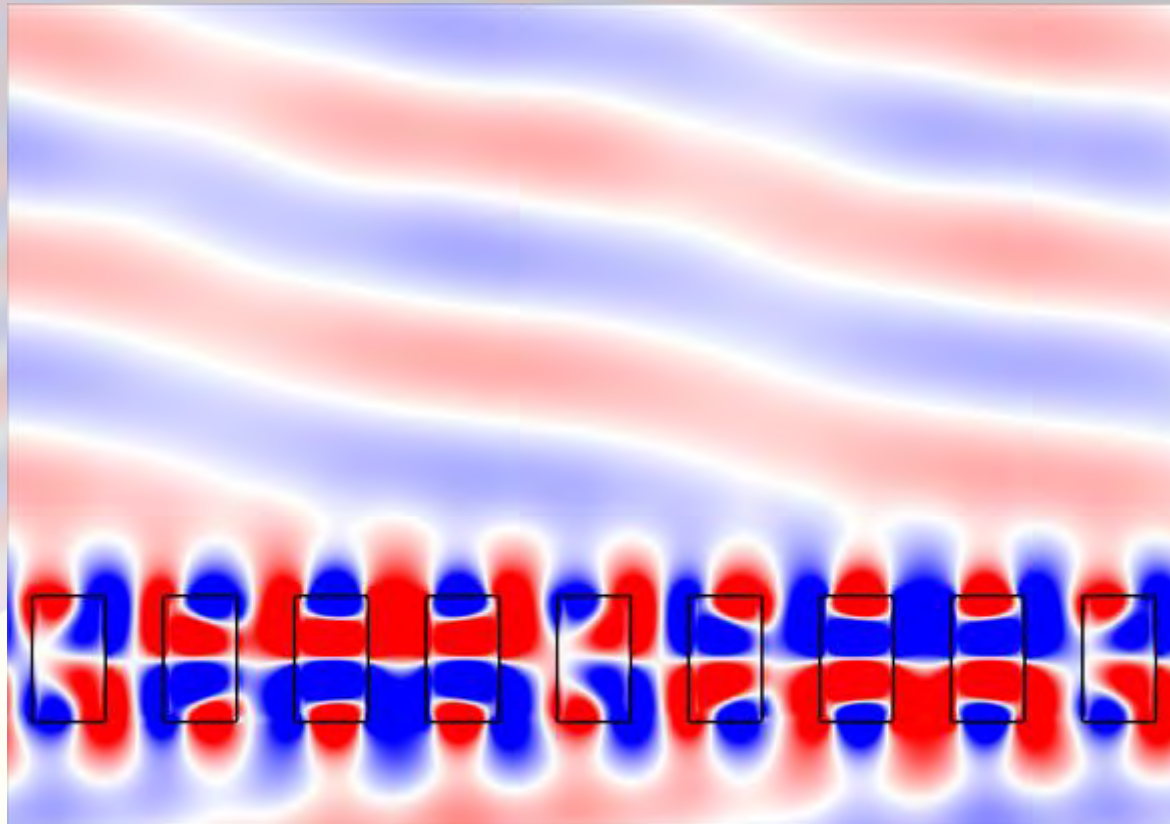
1 index

2 zero index

3 experiments



Where do we go from here?



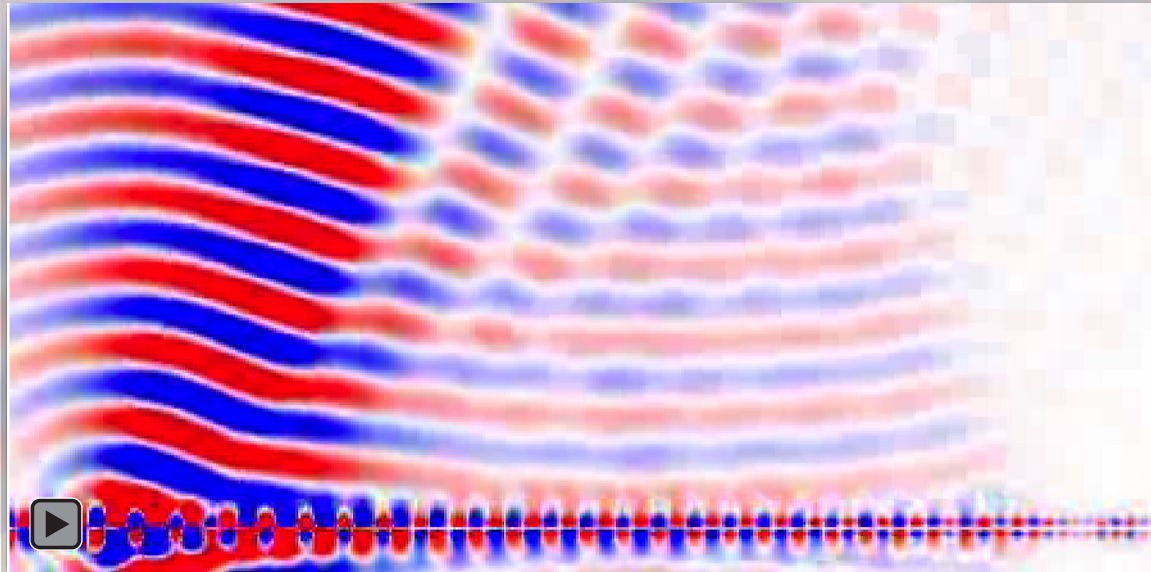
Radiative losses can be steered...

1 index

2 zero index

3 experiments

Where do we go from here?



...or arranged to cause focusing...

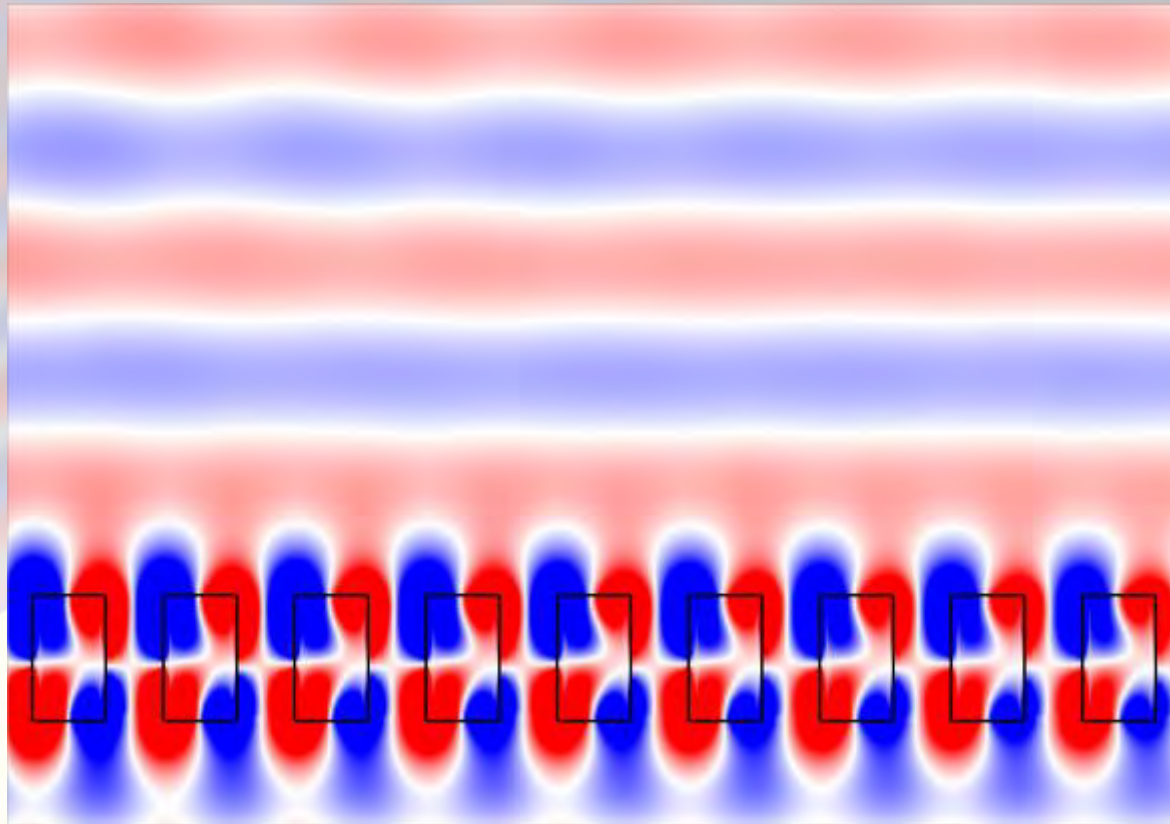
1 index

2 zero index

3 experiments



Where do we go from here?



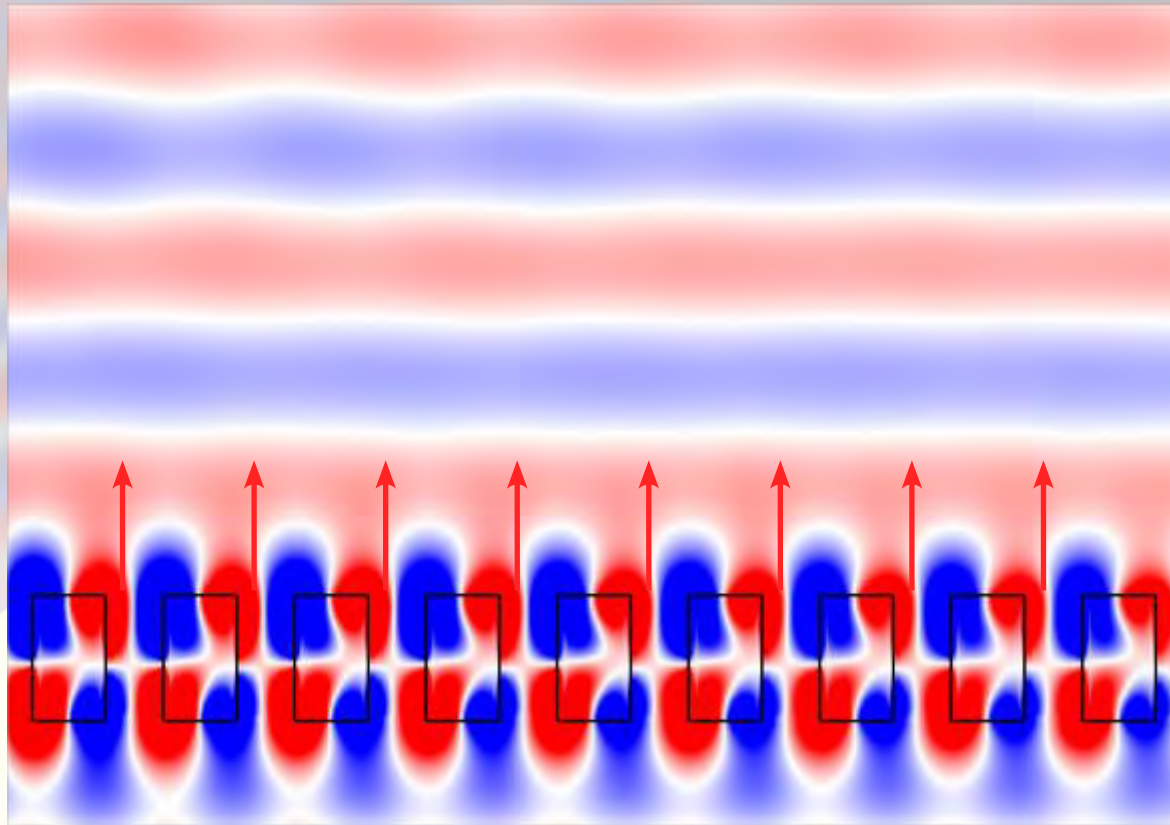
...or eliminated causing "bound in continuum" state

1 index

2 zero index

3 experiments

Where do we go from here?



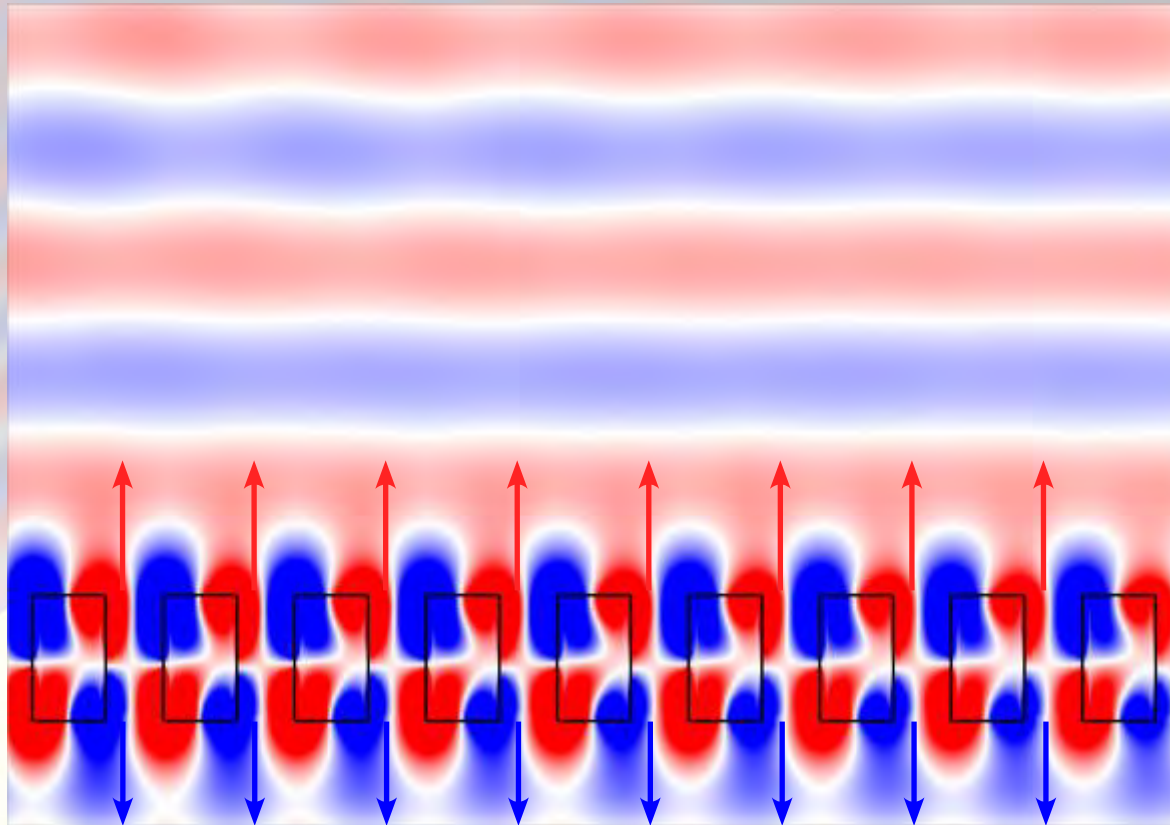
...or eliminated causing "bound in continuum" state

1 index

2 zero index

3 experiments

Where do we go from here?



...or eliminated causing "bound in continuum" state

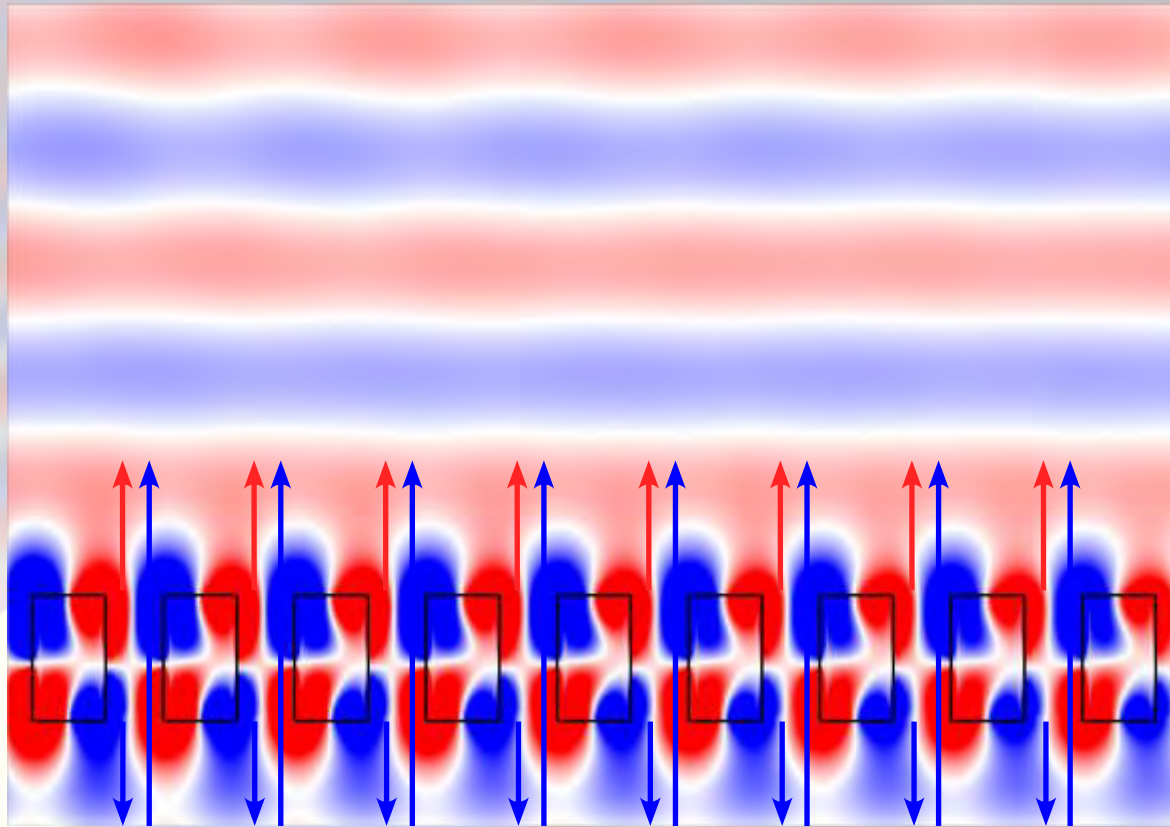
1 index

2 zero index

3 experiments



Where do we go from here?



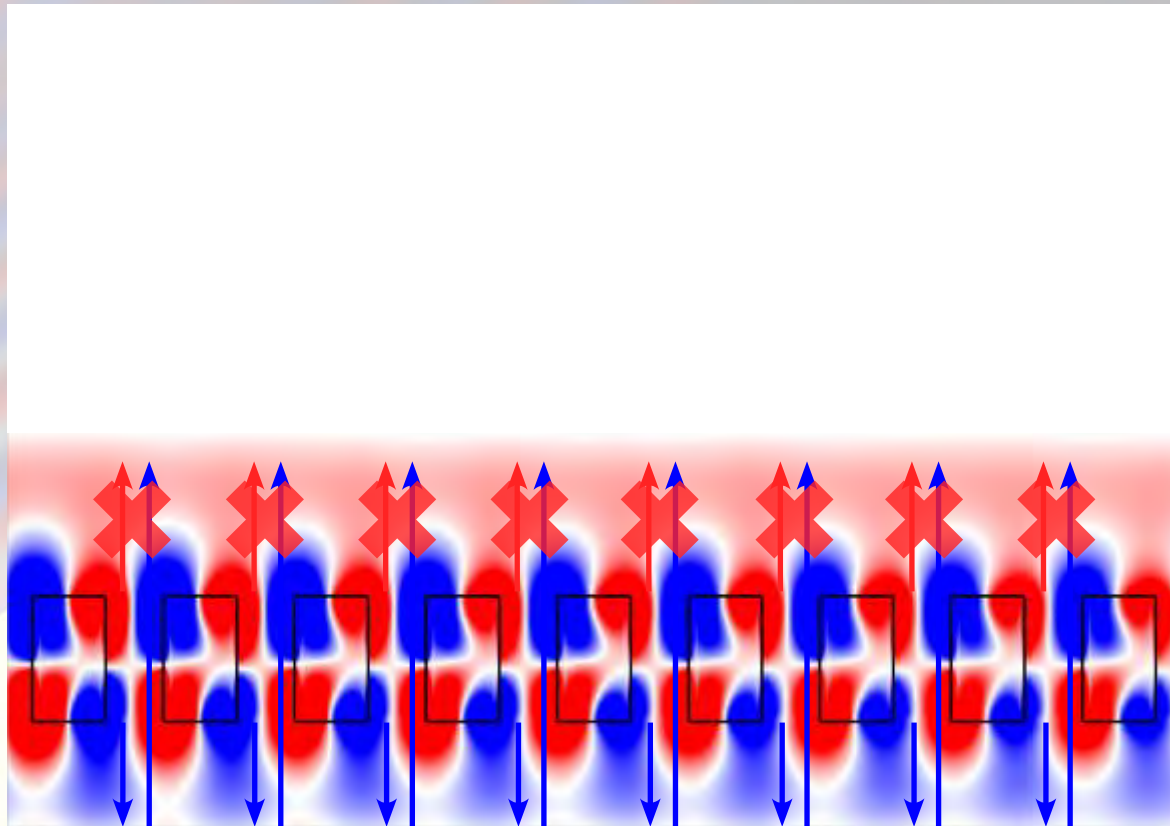
...or eliminated causing "bound in continuum" state

1 index

2 zero index

3 experiments

Where do we go from here?



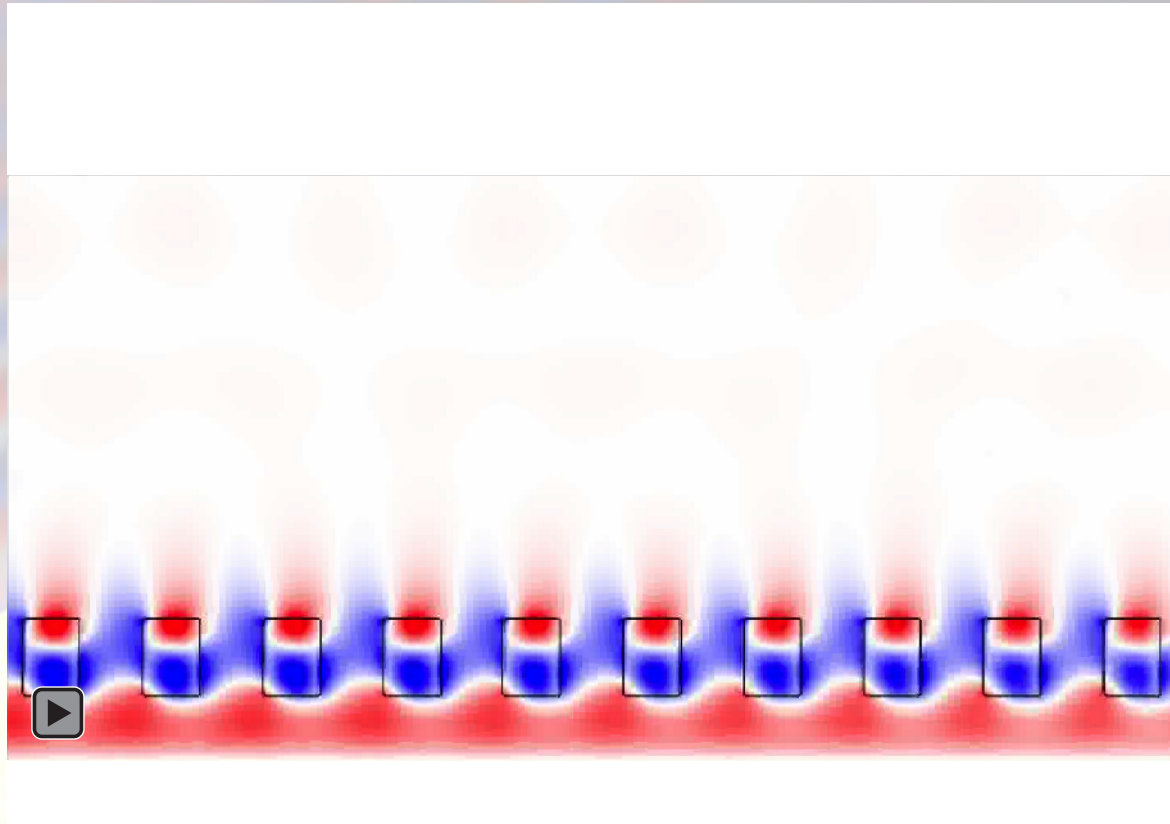
...or eliminated causing "bound in continuum" state

1 index

2 zero index

3 experiments

Where do we go from here?



...or eliminated causing "bound in continuum" state

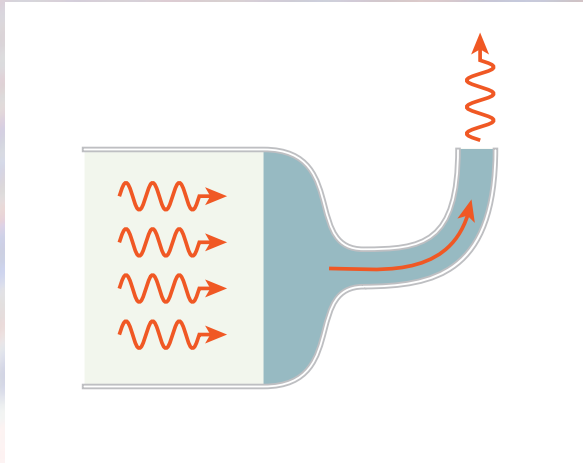
1 index

2 zero index

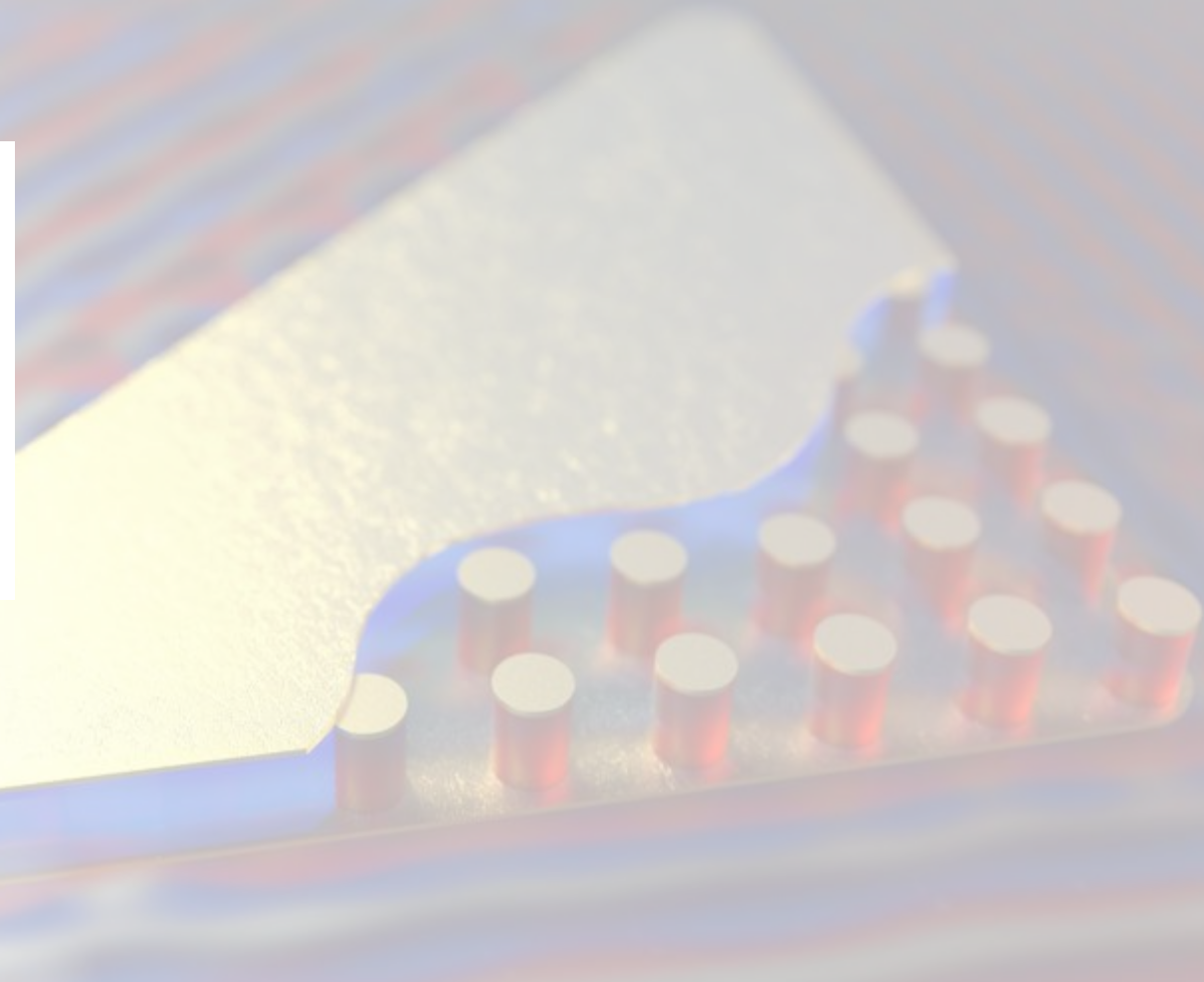
3 experiments



# Exciting applications ahead



**supercoupling**

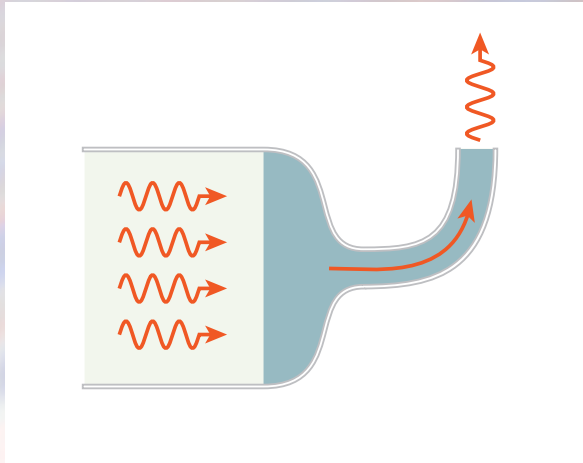


**1 index**

**2 zero index**

**3 experiments**

# Exciting applications ahead



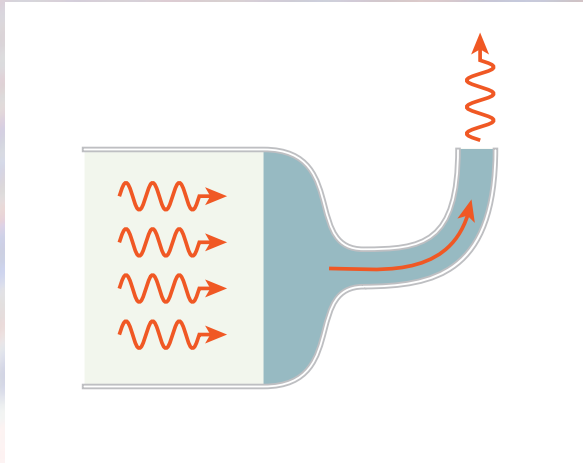
**supercoupling**



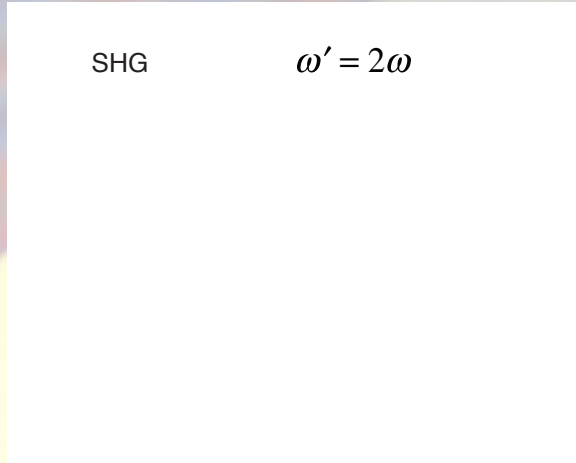
**NLO**



# Exciting applications ahead



**supercoupling**



SHG

$$\omega' = 2\omega$$

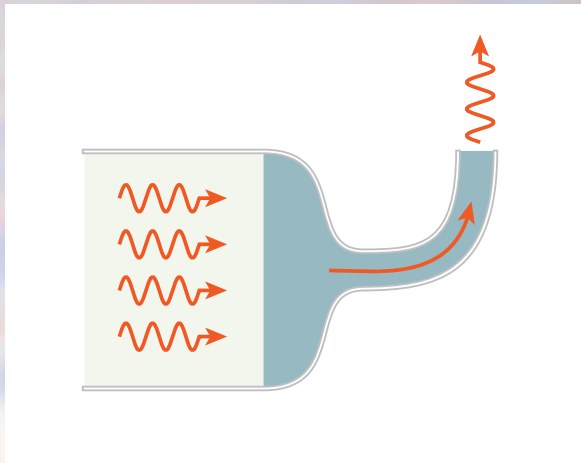
**NLO**

**1** index

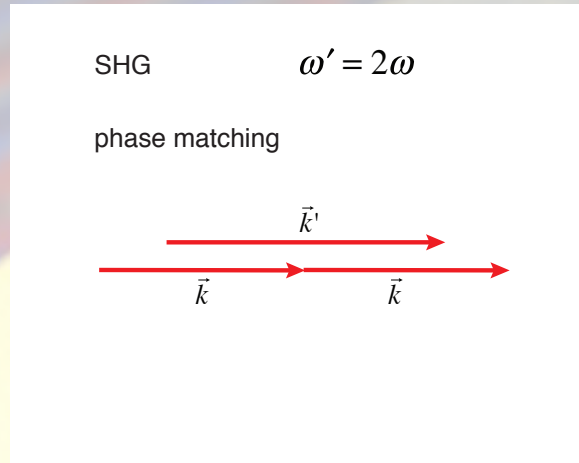
**2** zero index

**3** experiments

# Exciting applications ahead

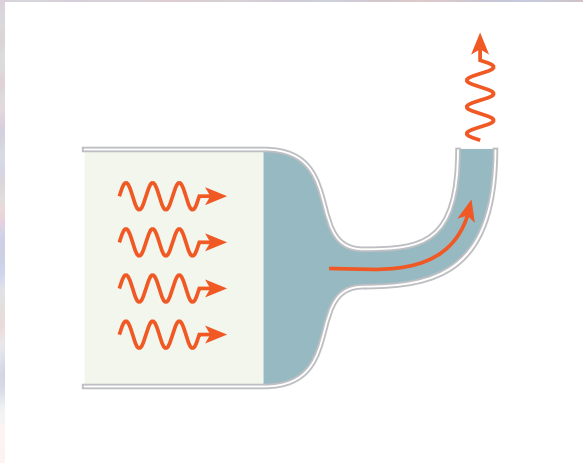


**supercoupling**

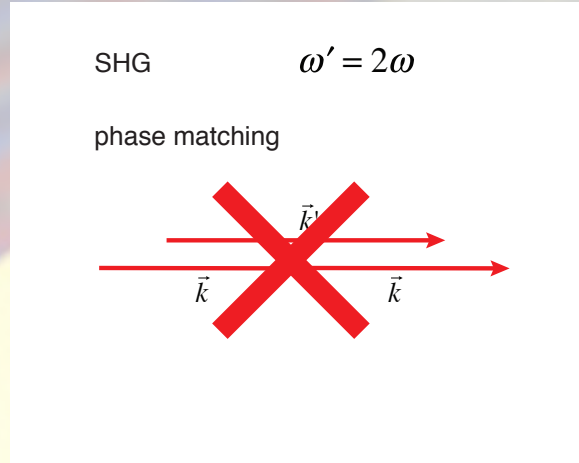


**NLO**

# Exciting applications ahead

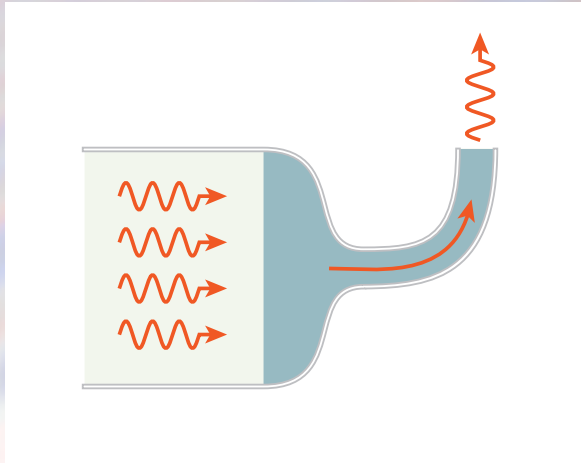


**supercoupling**

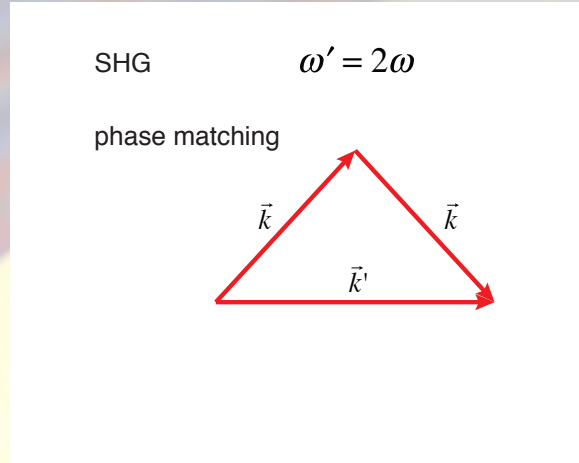


**NLO**

# Exciting applications ahead



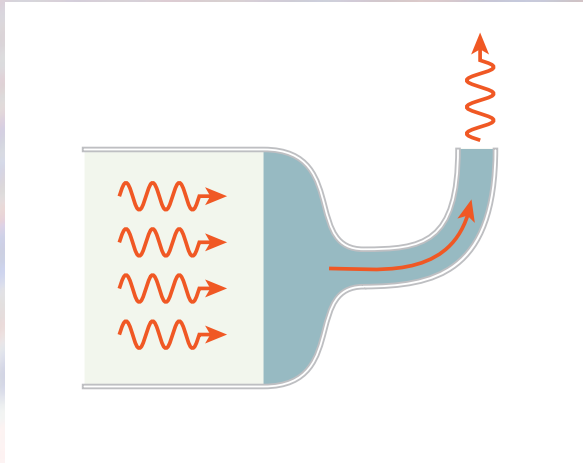
**supercoupling**



**NLO**



# Exciting applications ahead



SHG

$$\omega' = 2\omega$$

at zero index

$$\vec{k} = 0$$

**supercoupling**

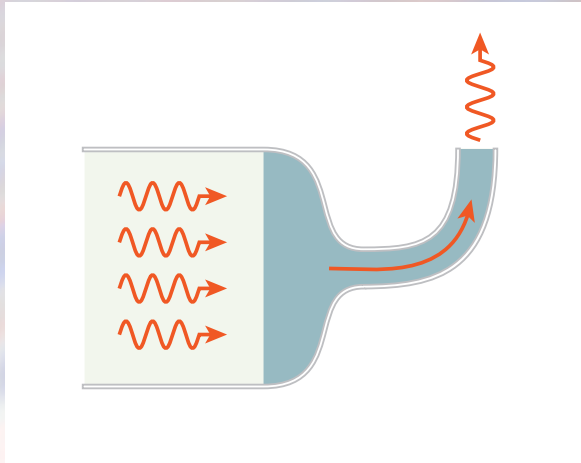
**NLO**

**1** index

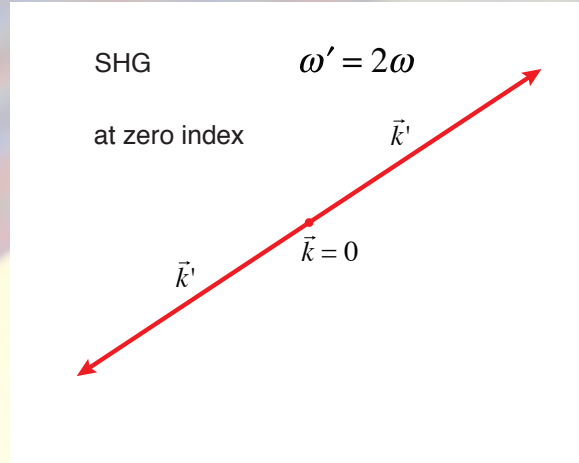
**2** zero index

**3** experiments

# Exciting applications ahead

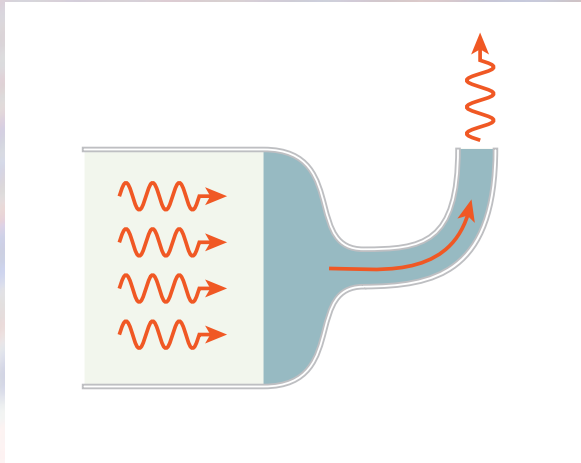


**supercoupling**

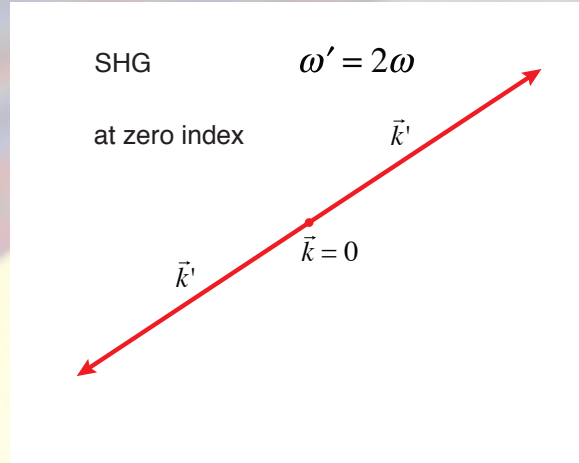


**NLO**

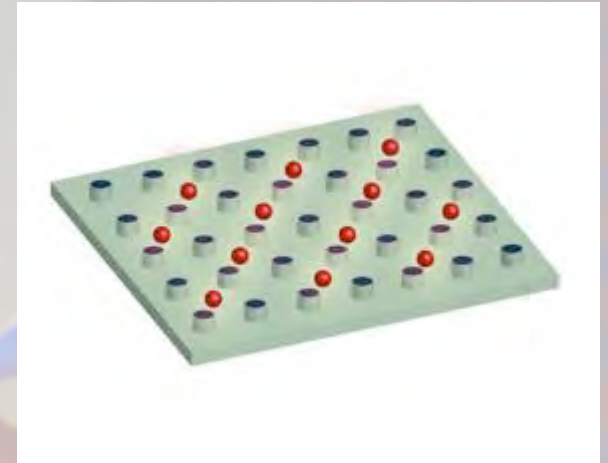
# Exciting applications ahead



supercoupling



NLO



quantum optics



**Yang Li, Shota Kita, Phil Muñoz, Orad Reshef,  
Daryl Vulis, Mei Yin, Lysander Christakis, Zin Lin,  
Cleaven Chia, Olivia Mello, Haoning Tang, Marko Lončar**

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