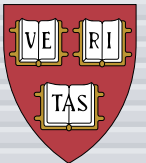


**Oscillating between semiconductor and metal:  
moving ions faster than electron  
wave functions can spread**

**Chris Roeser  
Maria Kandyla  
Albert Kim  
Arantza Mendioroz**



# Introduction

## The Theory of Impurity Conduction†

By N. F. MOTT and W. D. TWOSE‡  
Department of Physics, University of Cambridge

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N. Mott and W.D. Twose, *Adv. Phys.* 10, 107 (1961)

§ 1. INTRODUCTION  
The purpose of this article is to study one of the ways in which electric current is carried by electrons in a conductor containing impurities. The current in a conductor is carried by electrons, and the processes which are responsible for the current are the same as those which are responsible for the current in a metal. The current is carried by electrons, and the processes which are responsible for the current are the same as those which are responsible for the current in a metal.

# Introduction

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### CONTENTS

**structure determines electronic state**

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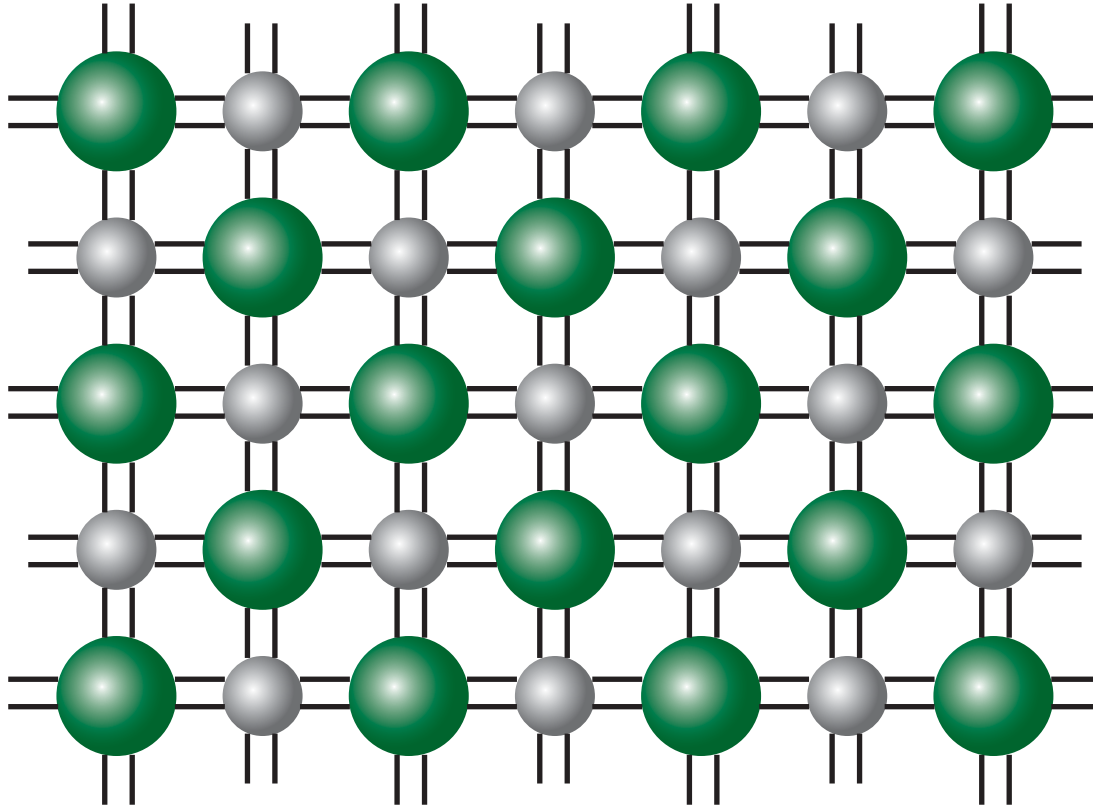
§ 1. INTRODUCTION  
The purpose of this article is to study one of the ways in which electrical conduction is affected by the presence of impurities. The current in a conductor containing impurities is carried by electrons and holes. There are competing conduction processes which are possible for the current to be carried by electrons or holes. The current is carried by electrons or holes on

# *Introduction*

**short laser pulses can drive structural transitions**

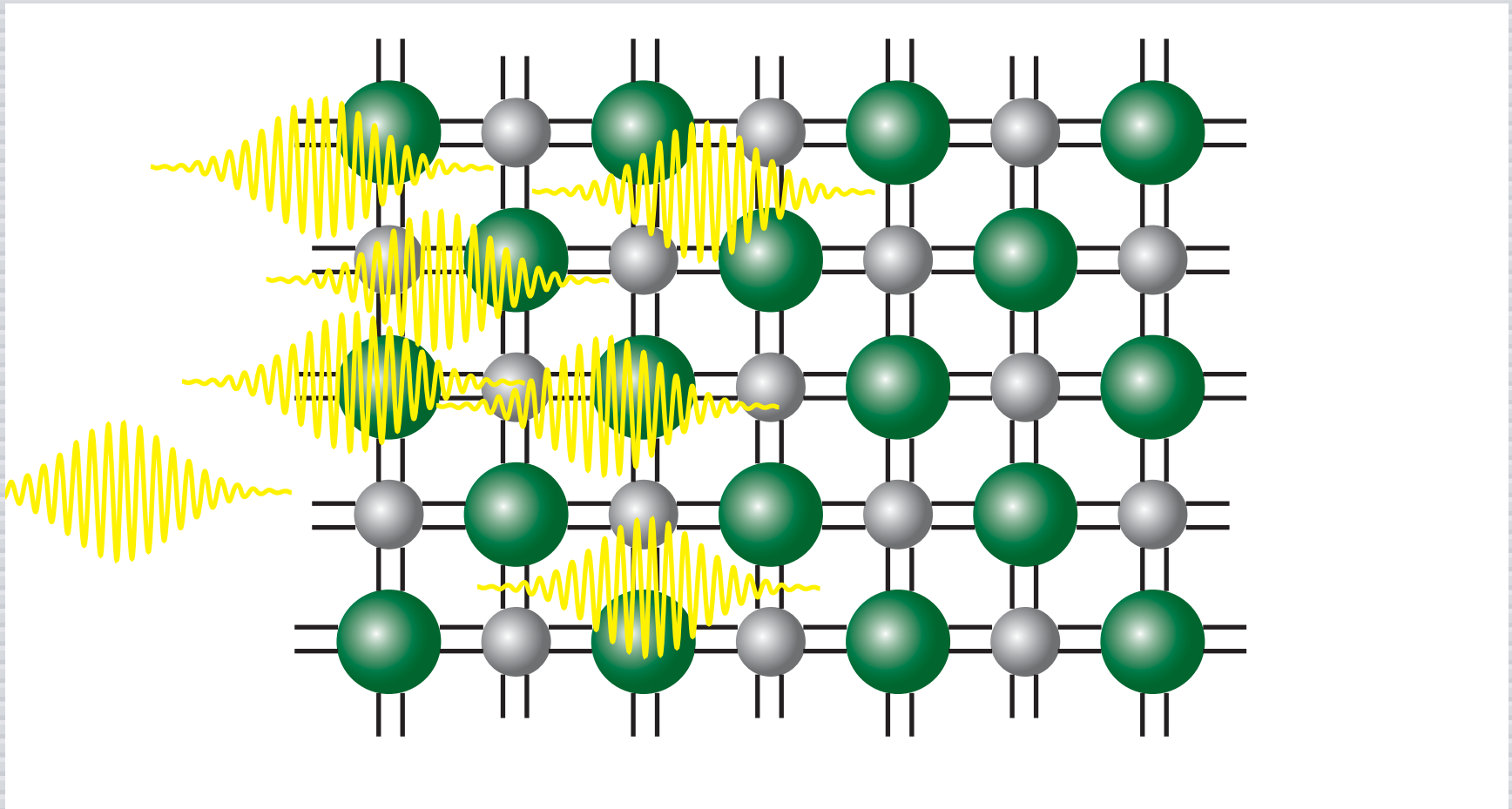
# *Introduction*

how do femtosecond laser pulses alter a solid?



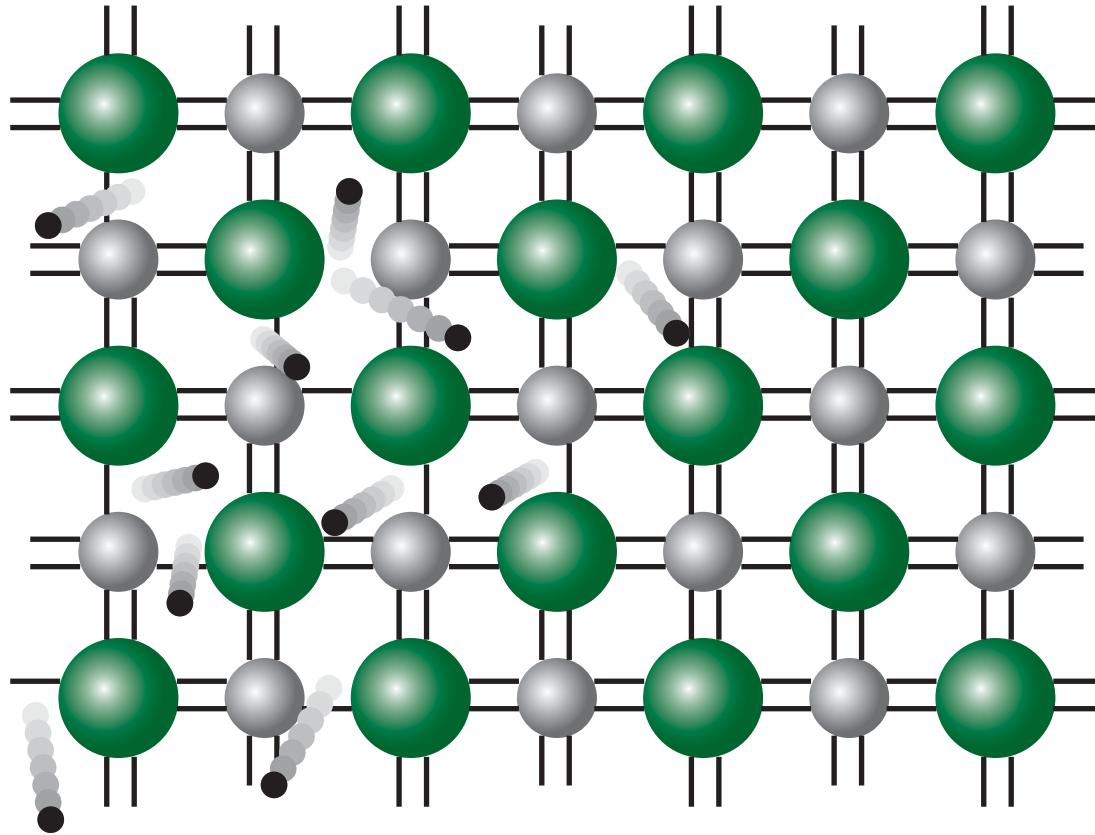
# *Introduction*

**photons excite valence electrons...**



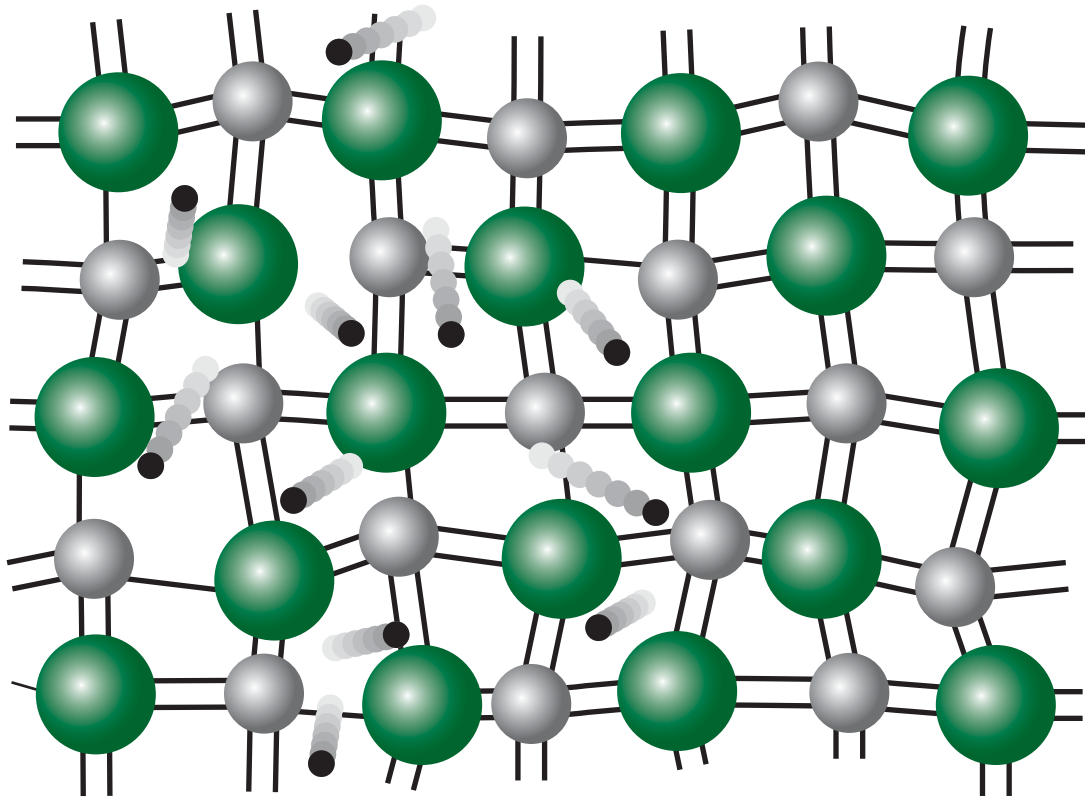
# *Introduction*

... and create free electrons...



# *Introduction*

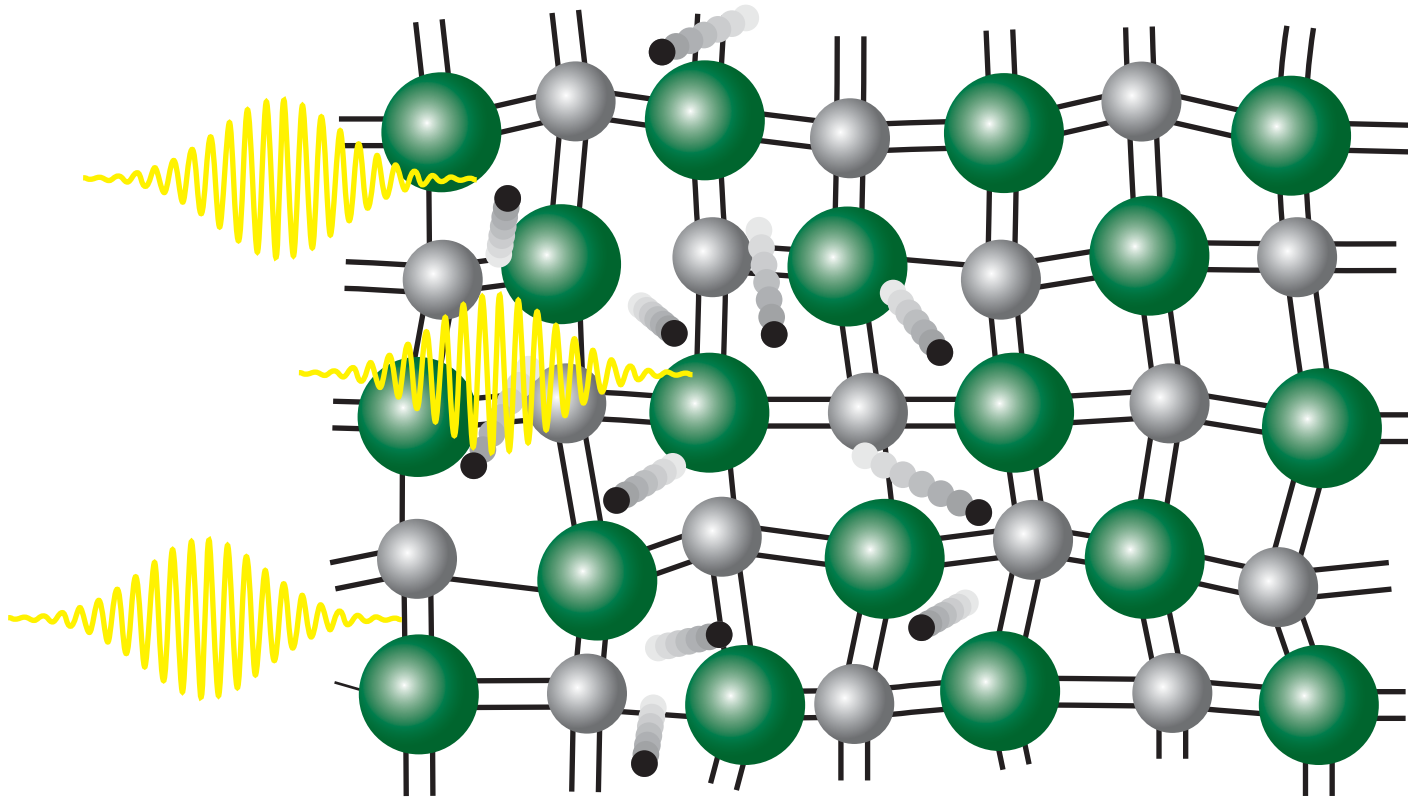
**... causing electronic and structural changes...**





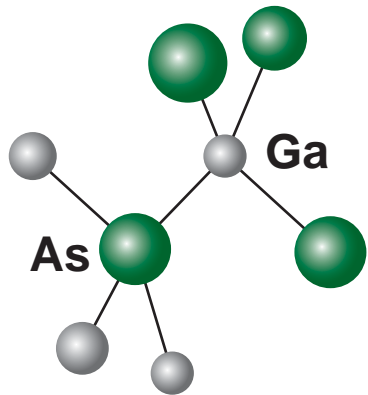
# Introduction

... which we detect with a second laser pulse



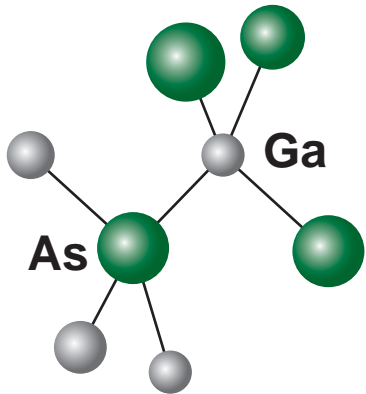
# Introduction

structure

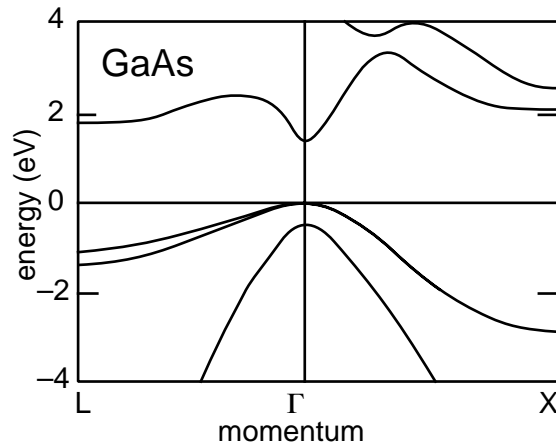


# Introduction

structure

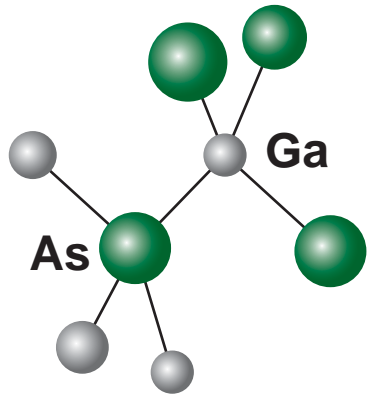


band structure

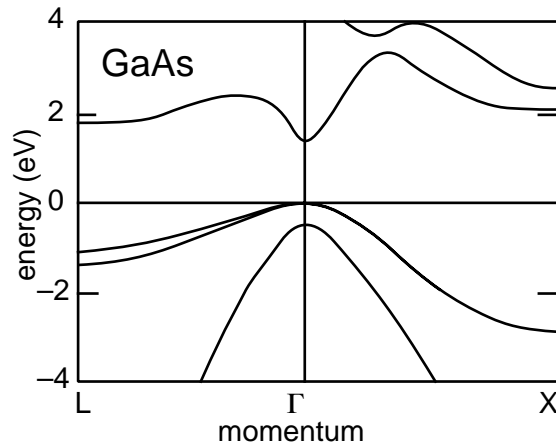


# Introduction

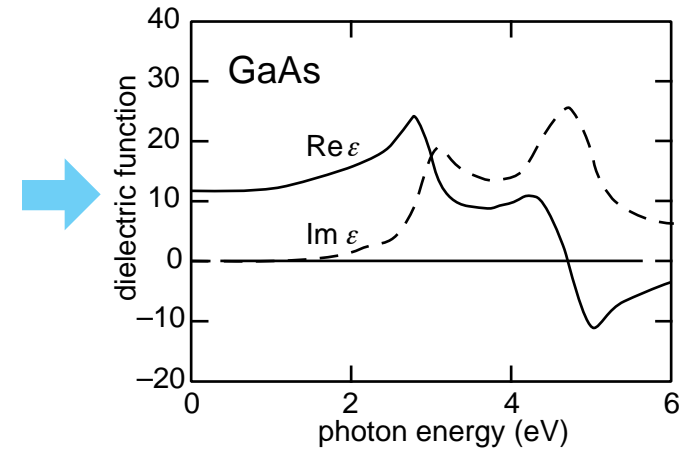
structure



band structure

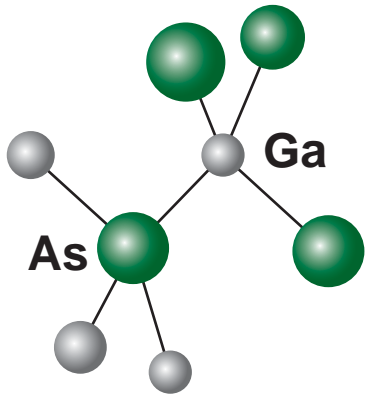


dielectric function

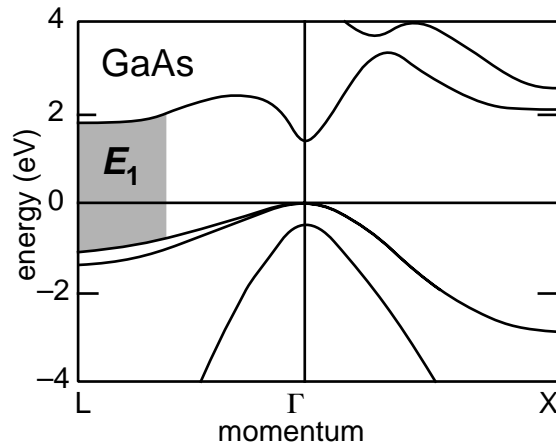


# Introduction

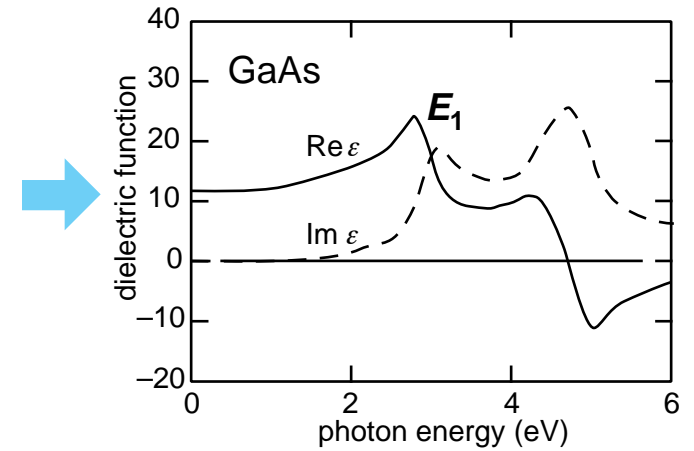
structure



band structure

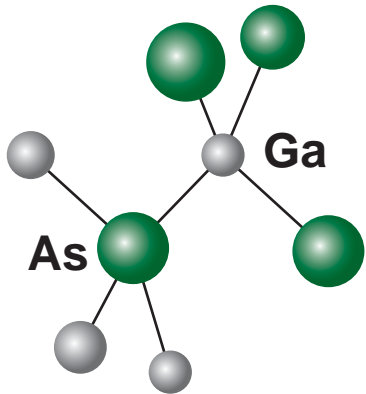


dielectric function

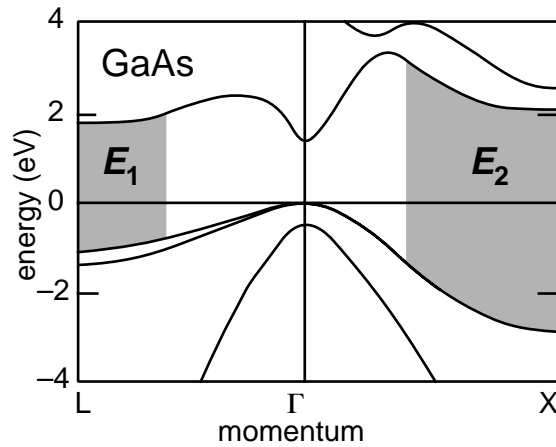


# Introduction

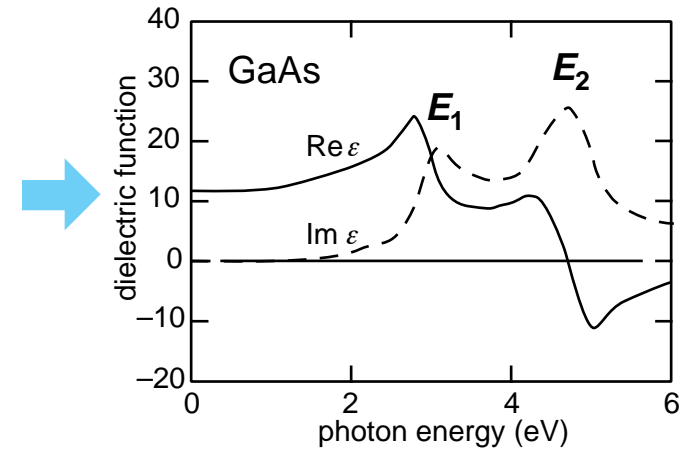
structure



band structure

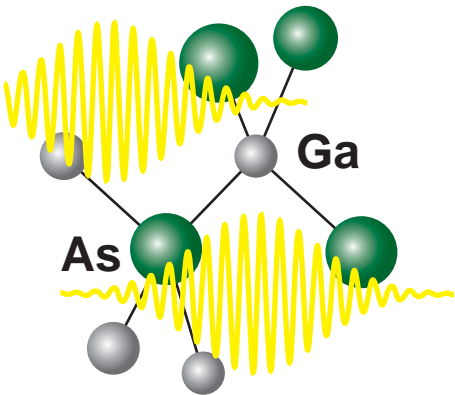


dielectric function

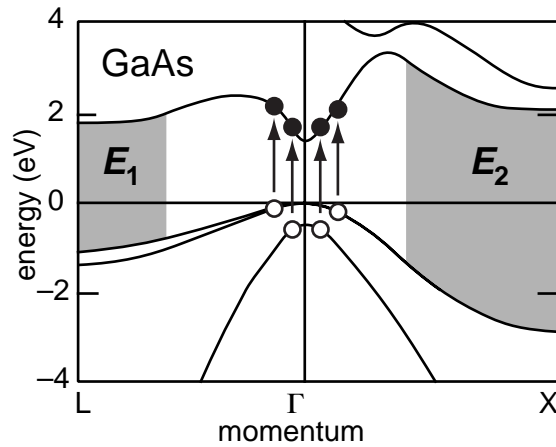


# Introduction

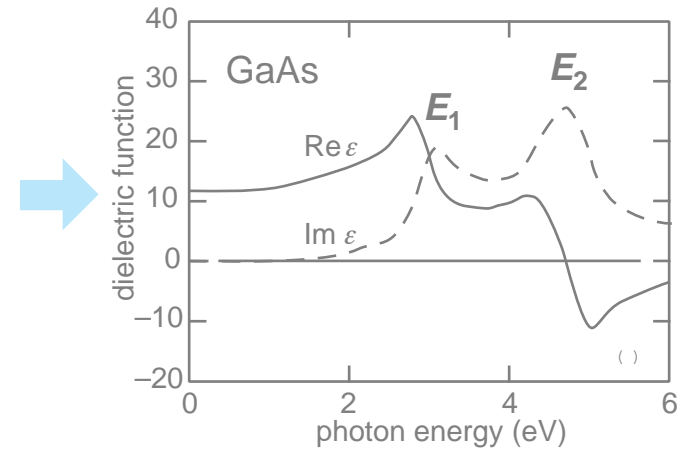
structure



band structure

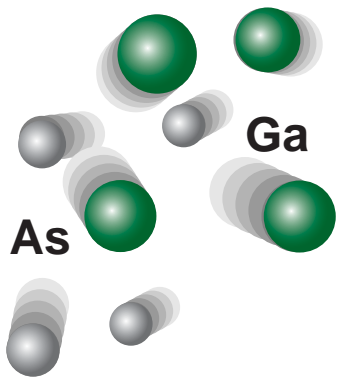


dielectric function

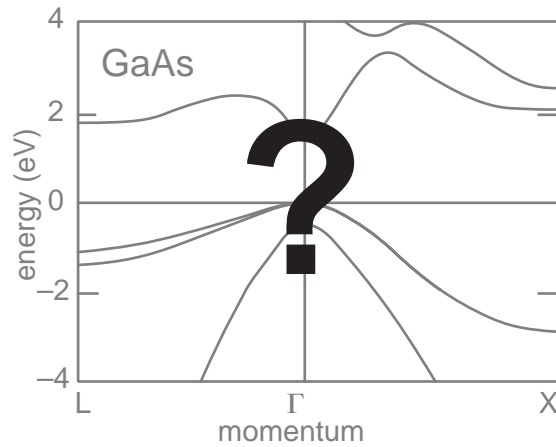


# Introduction

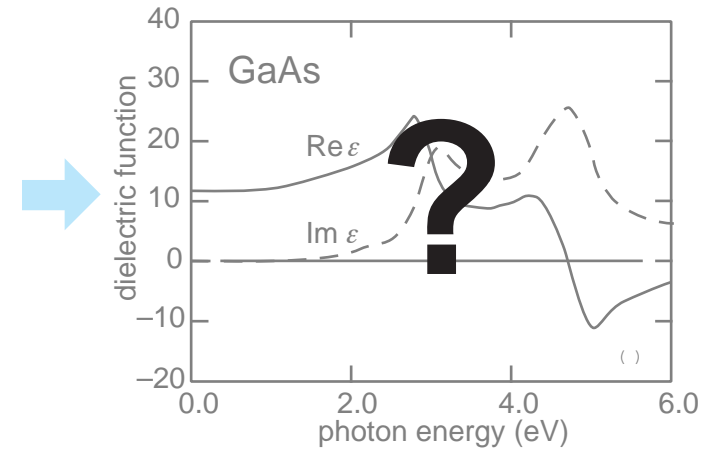
structure



band structure



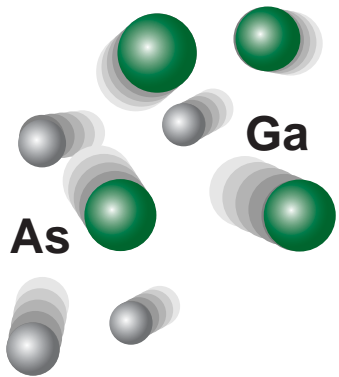
dielectric function



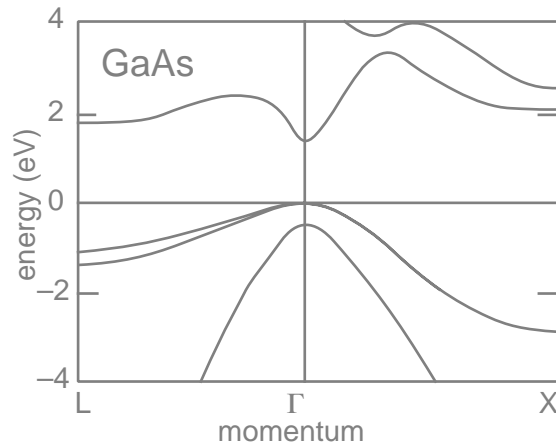


# Introduction

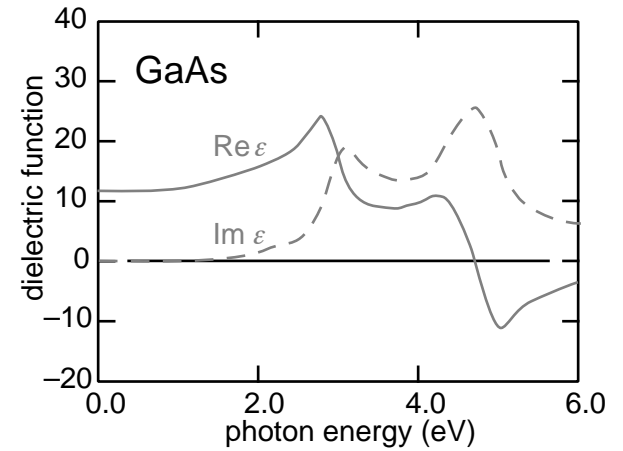
structure



band structure

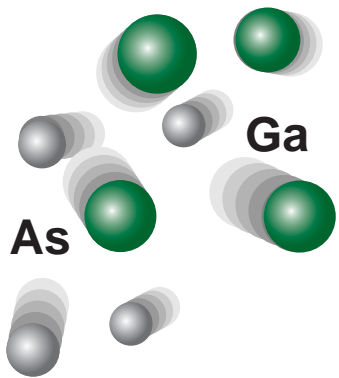


dielectric function

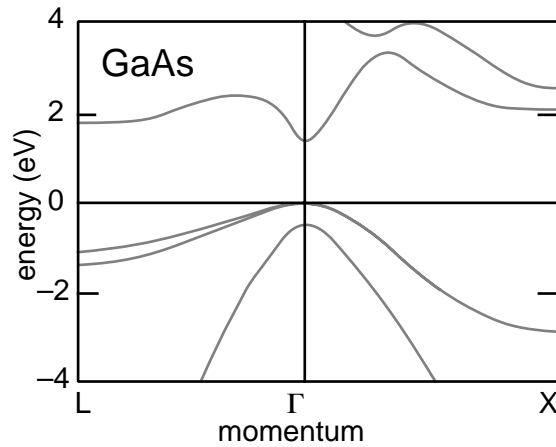


# Introduction

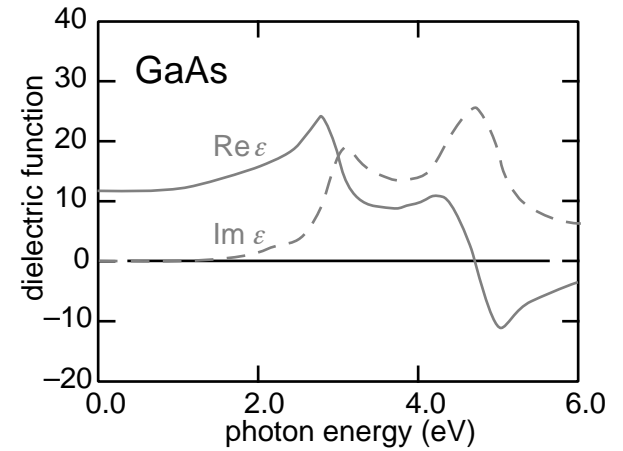
structure



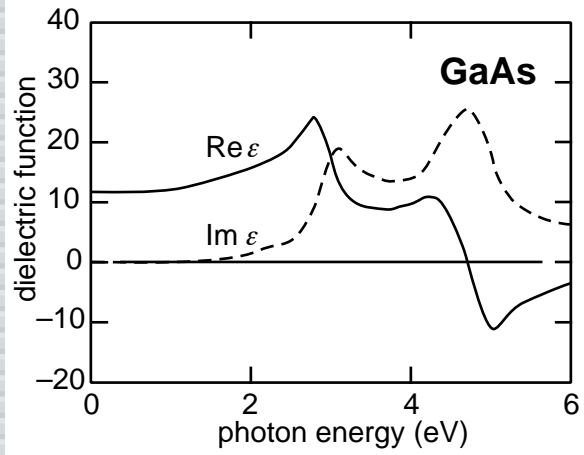
band structure



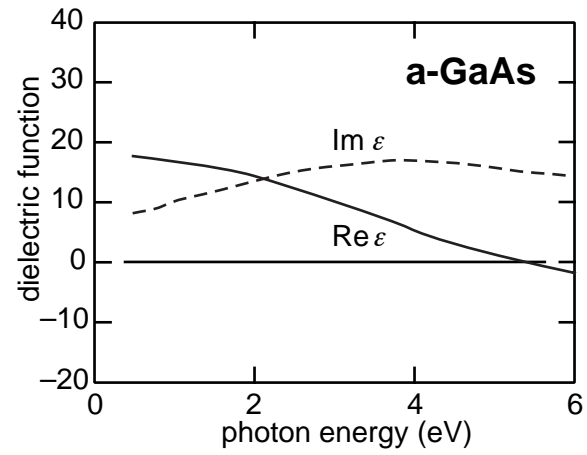
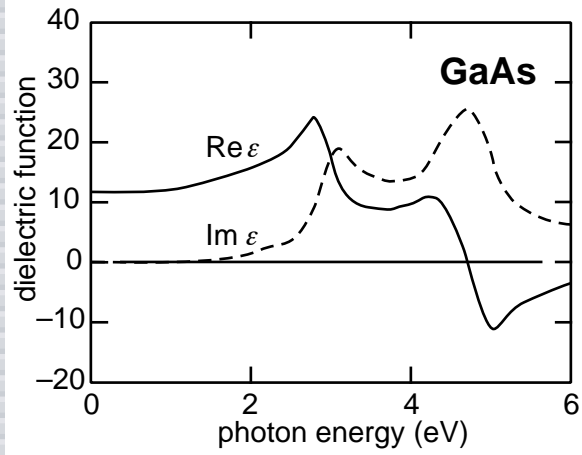
dielectric function



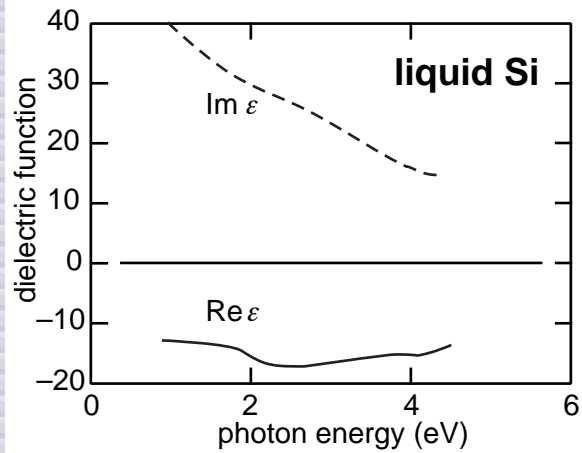
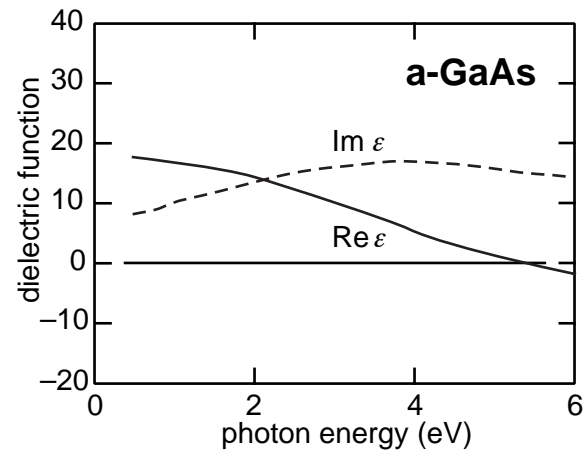
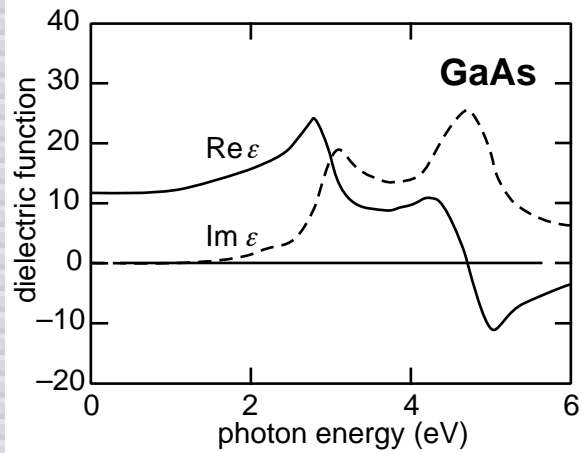
# Introduction



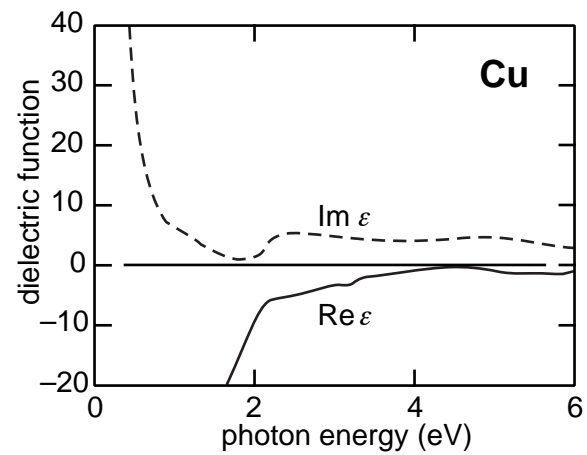
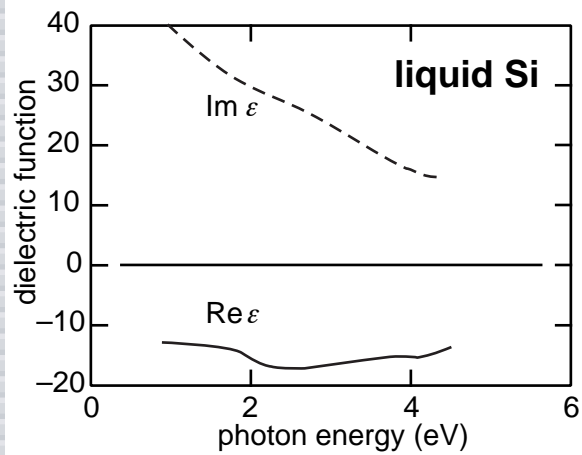
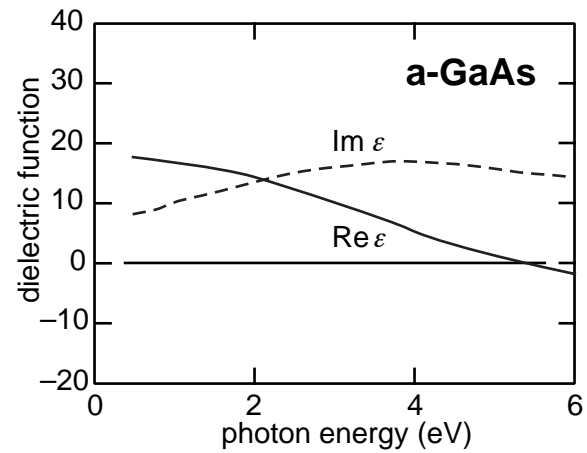
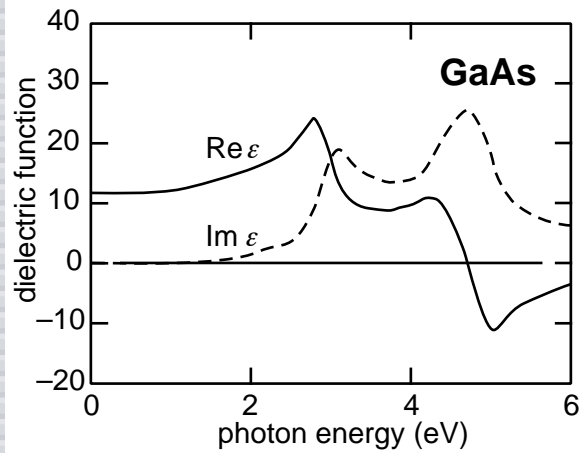
# Introduction



# Introduction



# Introduction



# *Introduction*

- ▶ **dielectric function: 'fingerprint' of state**
- ▶ **light can induce structural transitions**

# *Introduction*

- ▶ **optically induce electronic transitions *without* disordering lattice?**
- ▶ **(coherently) control state of solid?**



# Introduction

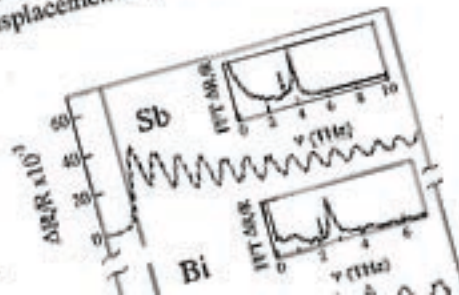
## Mechanism for displacive excitation of coherent phonons in Sb, Bi, Te, and $Ti_2O_3$

T. K. Cheng, J. Vidal, H. J. Zeiger, G. Dresselhaus, M. S. Dresselhaus, and E. P. Ippen  
*Massachusetts Institute of Technology, Cambridge, Massachusetts 02139*  
(Received 1 July 1991; accepted for publication 9 August 1991)

Coherent phonons in Sb, Bi, Te, and  $Ti_2O_3$  can be generated impulsively, and detected in the time domain through reflectivity modulation using 60 fs pulses of laser light at 2 eV. Experimental data for these opaque solids suggest that a direct Raman excitation mechanism is not responsible for coherent phonon generation. Rather, the excitation is attributed to an electronically induced displacement of the ion equilibrium coordinates.

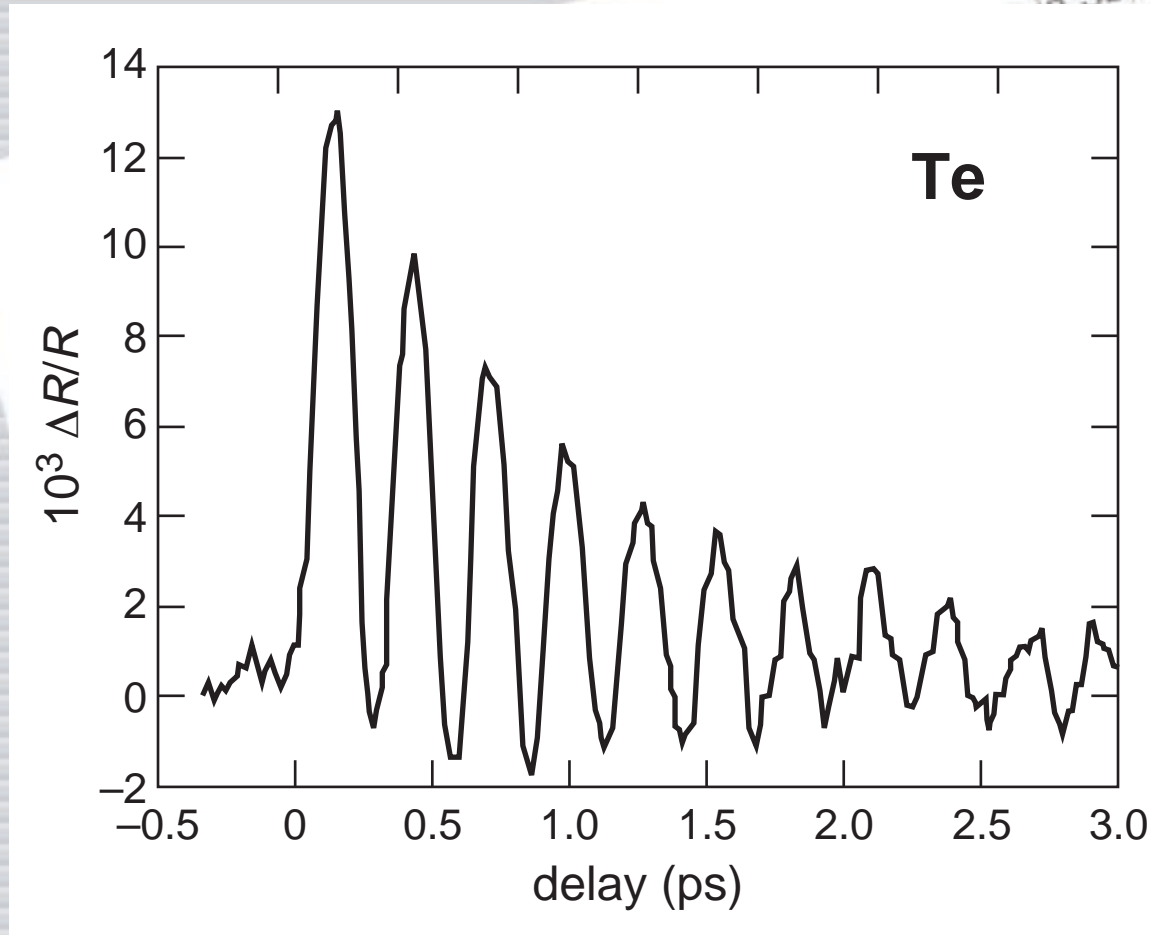
In recent years, there have been numerous reports of coherent molecular<sup>1-3</sup> and lattice<sup>4-9</sup> vibrations in time-resolved optical pump-probe measurements. In this letter, we propose a model to explain our observations of the excitation of very large coherent phonon amplitudes with only  $A_1$  symmetry in opaque single-crystal samples of Sb, Bi, Te, and  $Ti_2O_3$ . The experimental data for these opaque solids suggest that the coherent phonon excitation involves an electronic resonance but is not directly driven by an impulsive stimulated Raman scattering mechanism (ISRS),<sup>2-5</sup> as is often the case in the experiments for large coherent phonon mode selectivity and careful measurement of the coherent pump pulse in each material. Our conclusion follows from observation of the excitation and detection of coherent phonons were the output of a dispersion-compensated laser<sup>10</sup> (producing 60 fs, 2 eV pulses at a repetition rate of 100 MHz) and a pump-

2 to 1 ratio for  $A_{1g}$  to  $E_g$  mode intensities in Sb and Bi). Rather, we believe the coherent phonon generation is due to a displacement of the ion quasi-equilibrium coordinates produced by electronic excitation, which we call displacive excitation of coherent phonons (DECP). The DECP mechanism is closely related to the displaced ion equilibrium model for molecular systems. The ions cannot respond on the time scale of the electronic quasi-equilibration time and are therefore set into oscillation in an  $A_1$  mode of vibration about the displaced quasi-equilibrium  $A_1$  ion coordinate  $Q_0$ . Any other quasi-equilibrium displacements (displacements of  $E_g$  symmetry, for exam-



# Introduction

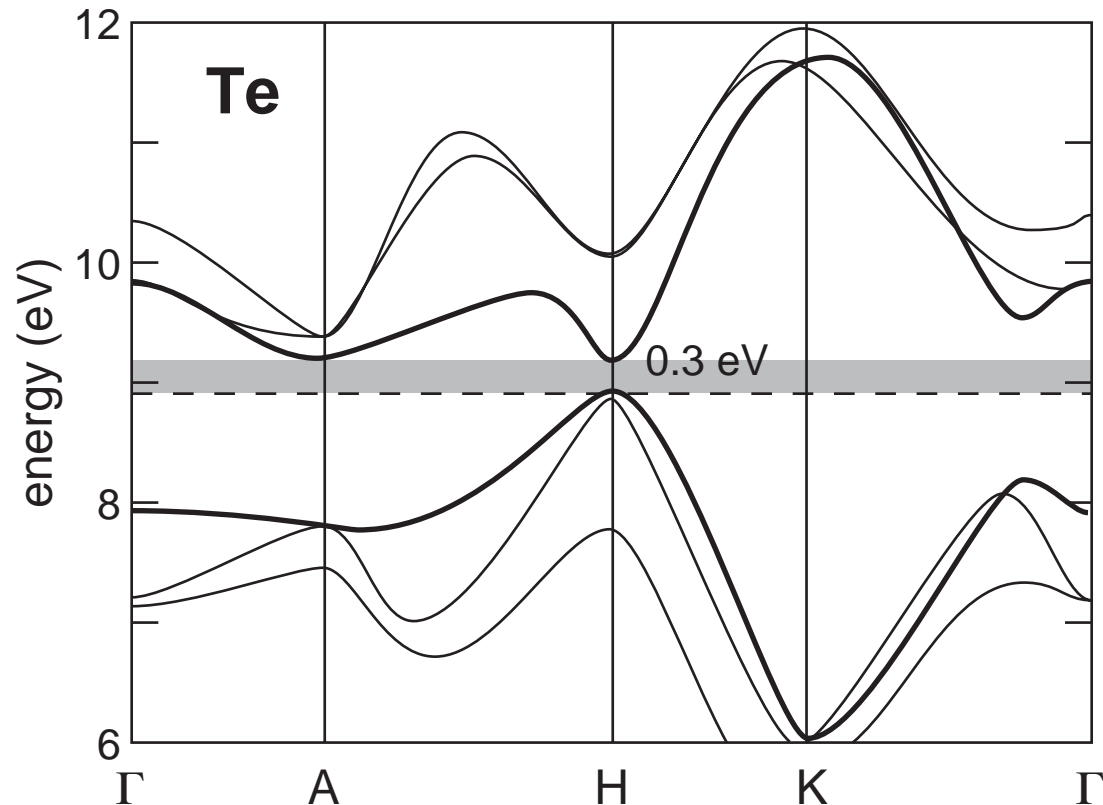
optically induce large amplitude phonons



Cheng *et al.*, *Appl. Phys. Lett.* 59, 1923 (1991)

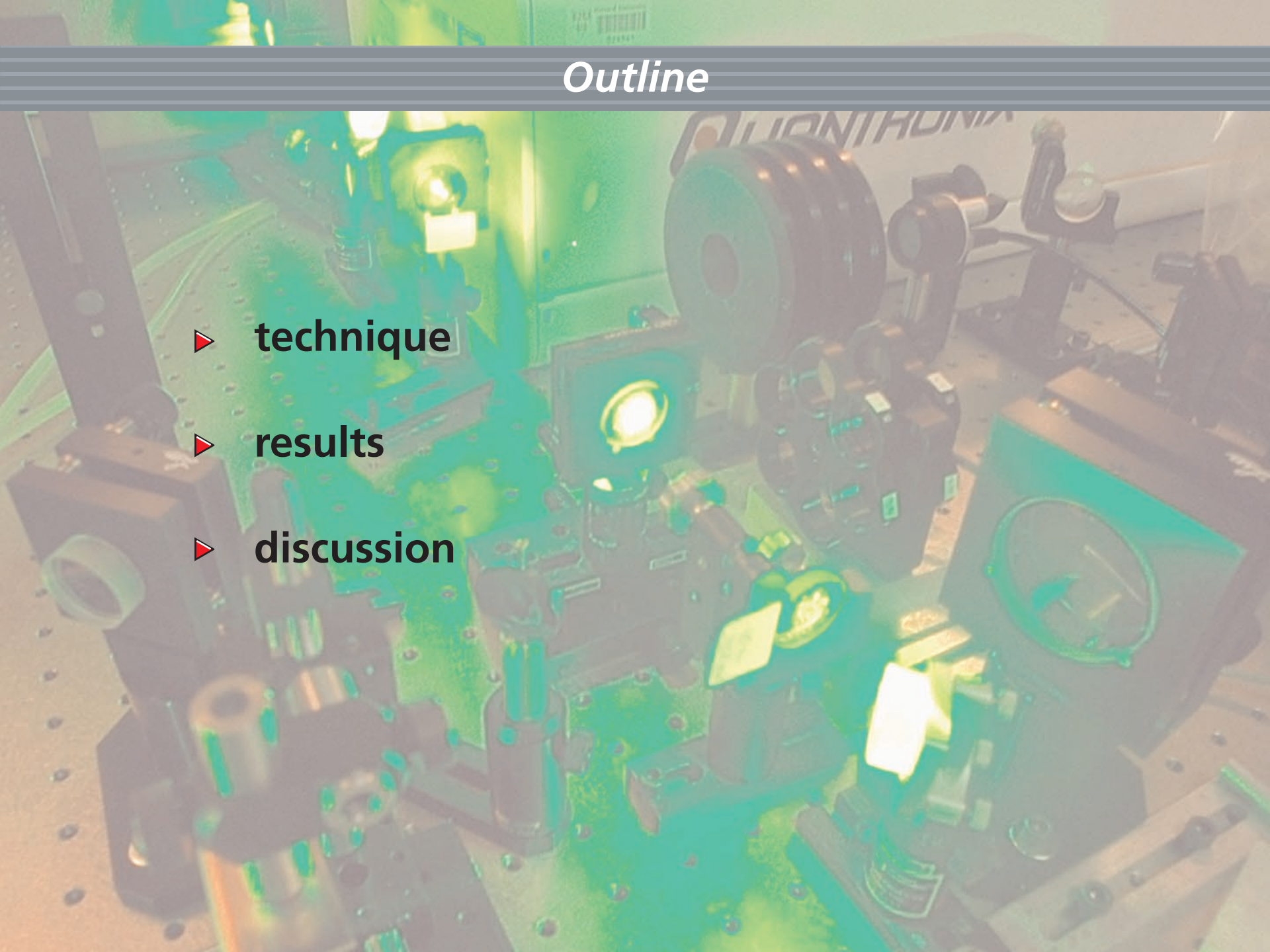
# Introduction

Tellurium: close to transition (0.3 eV gap)



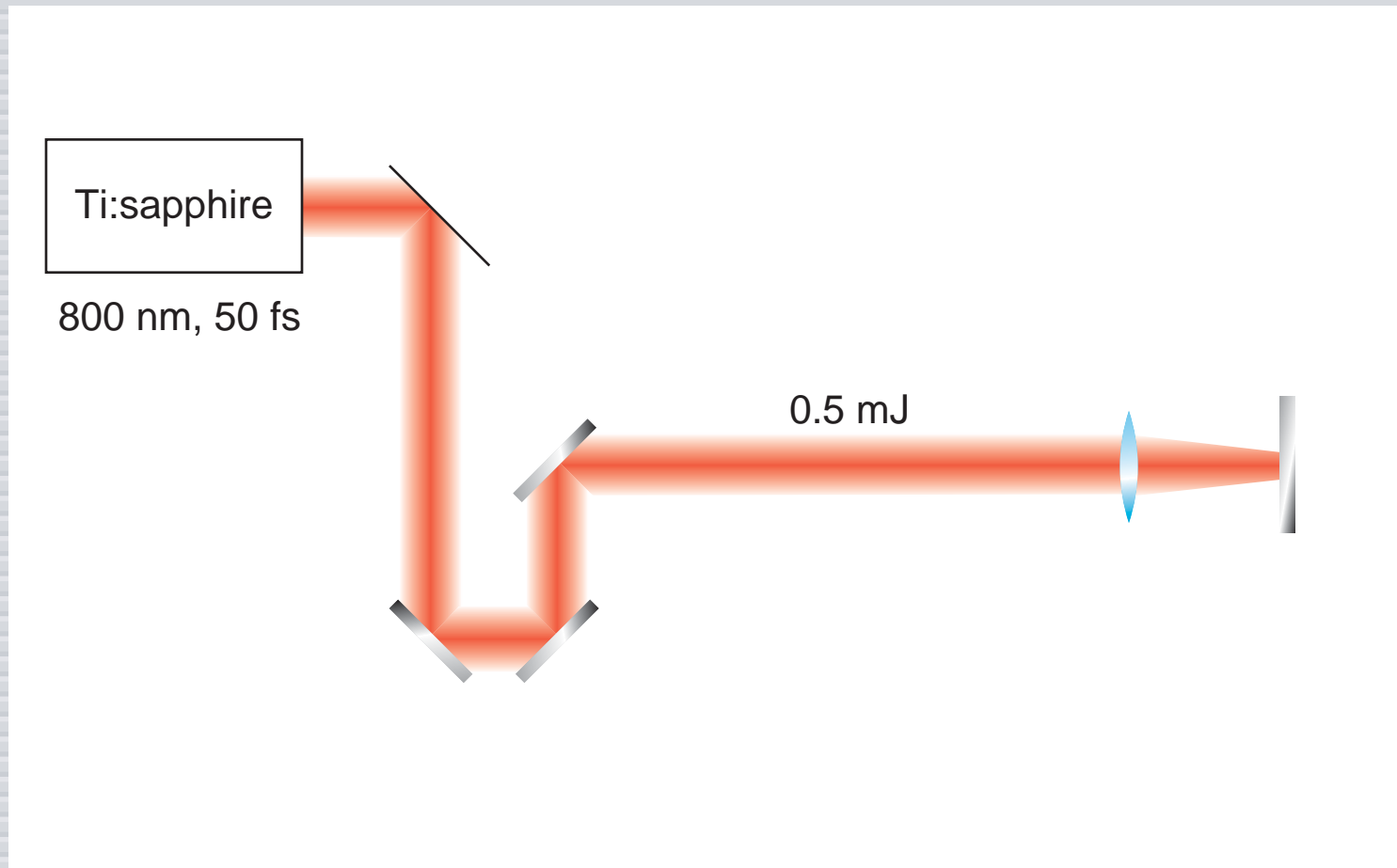
# Outline

- ▶ **technique**
- ▶ **results**
- ▶ **discussion**



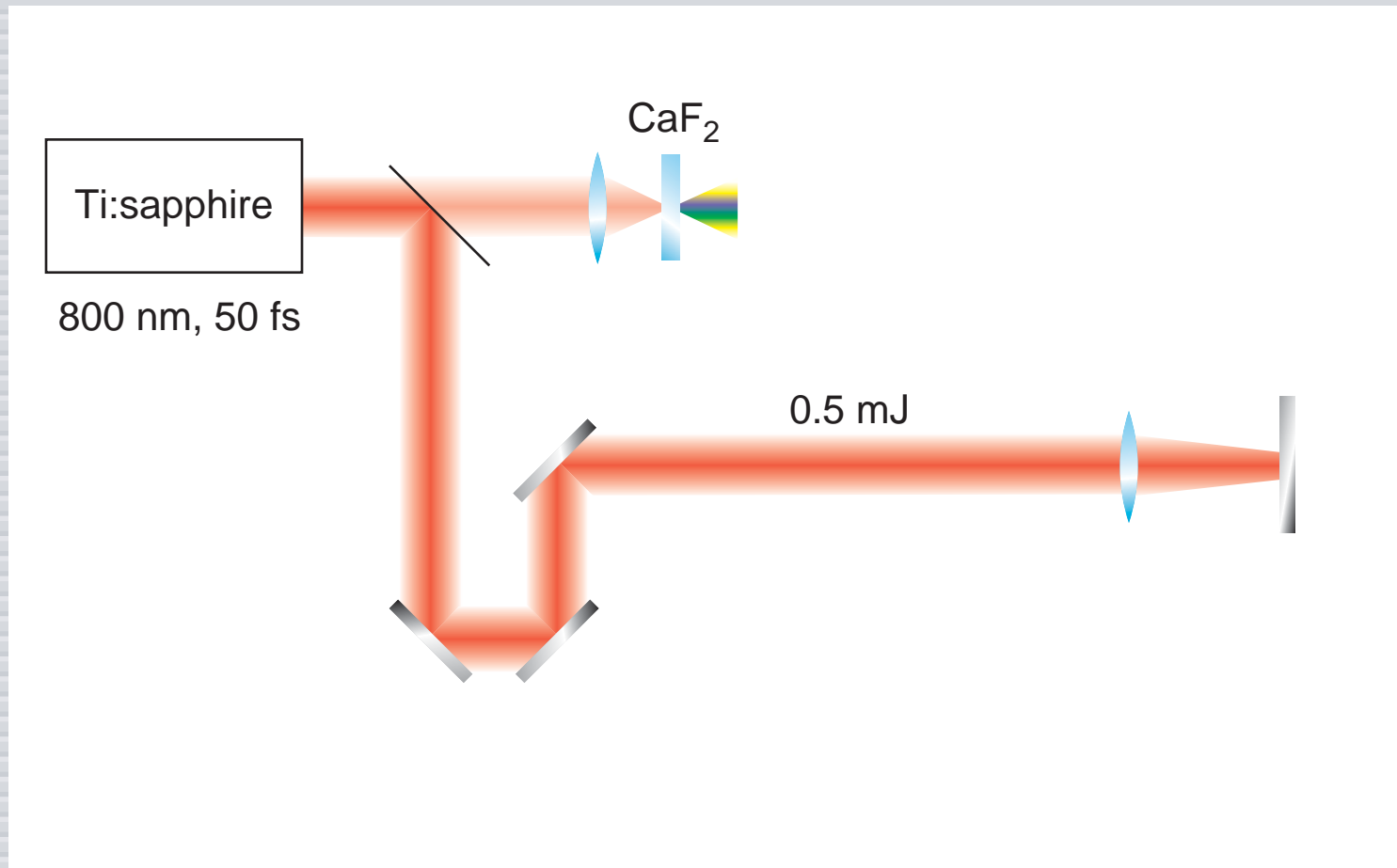
# Technique

## broadband time-resolved ellipsometry



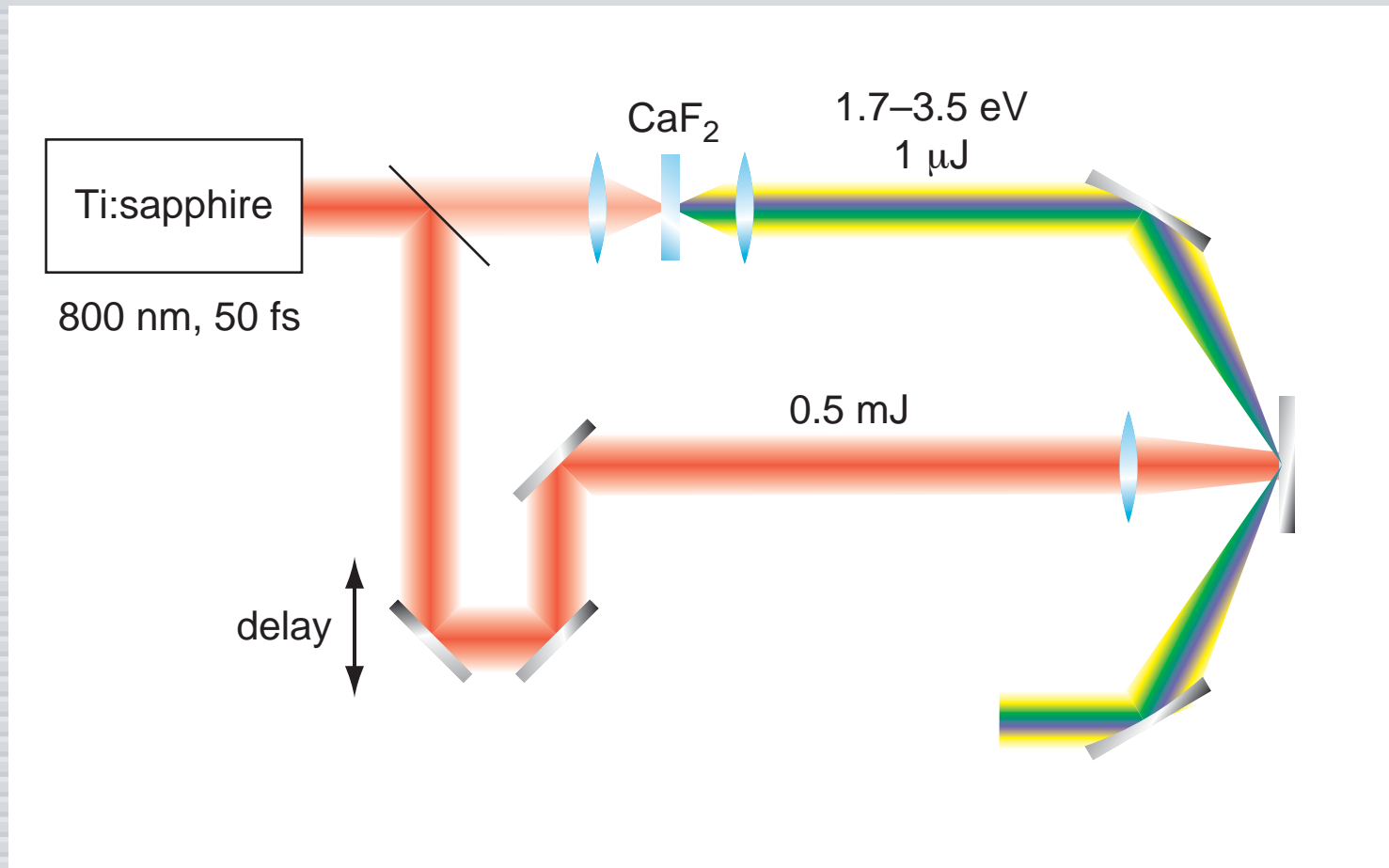
# Technique

## broadband time-resolved ellipsometry



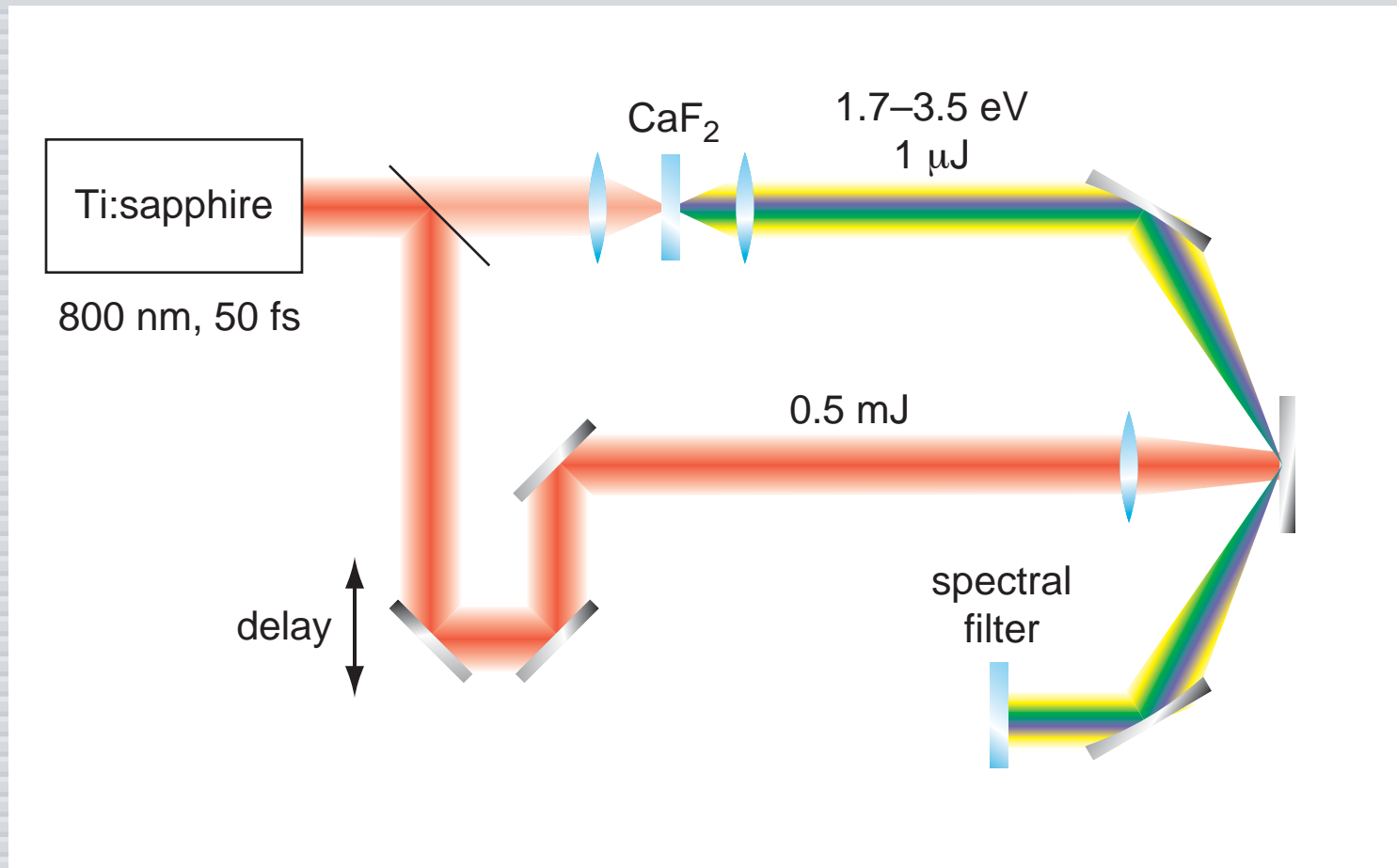
# Technique

## broadband time-resolved ellipsometry



# Technique

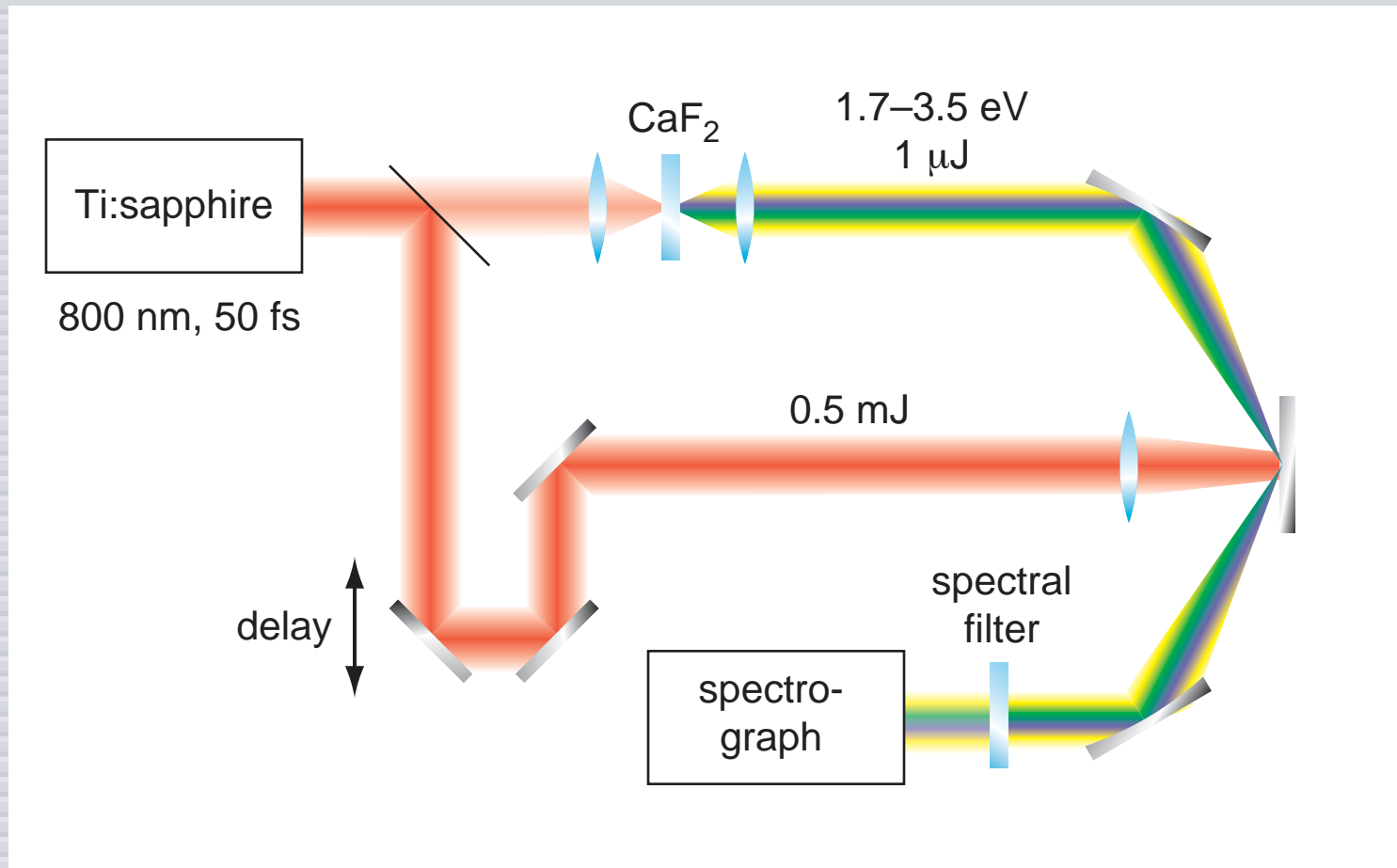
## broadband time-resolved ellipsometry





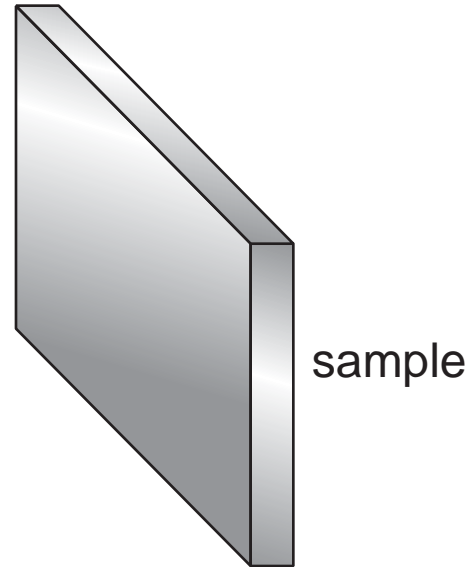
# Technique

## broadband time-resolved ellipsometry



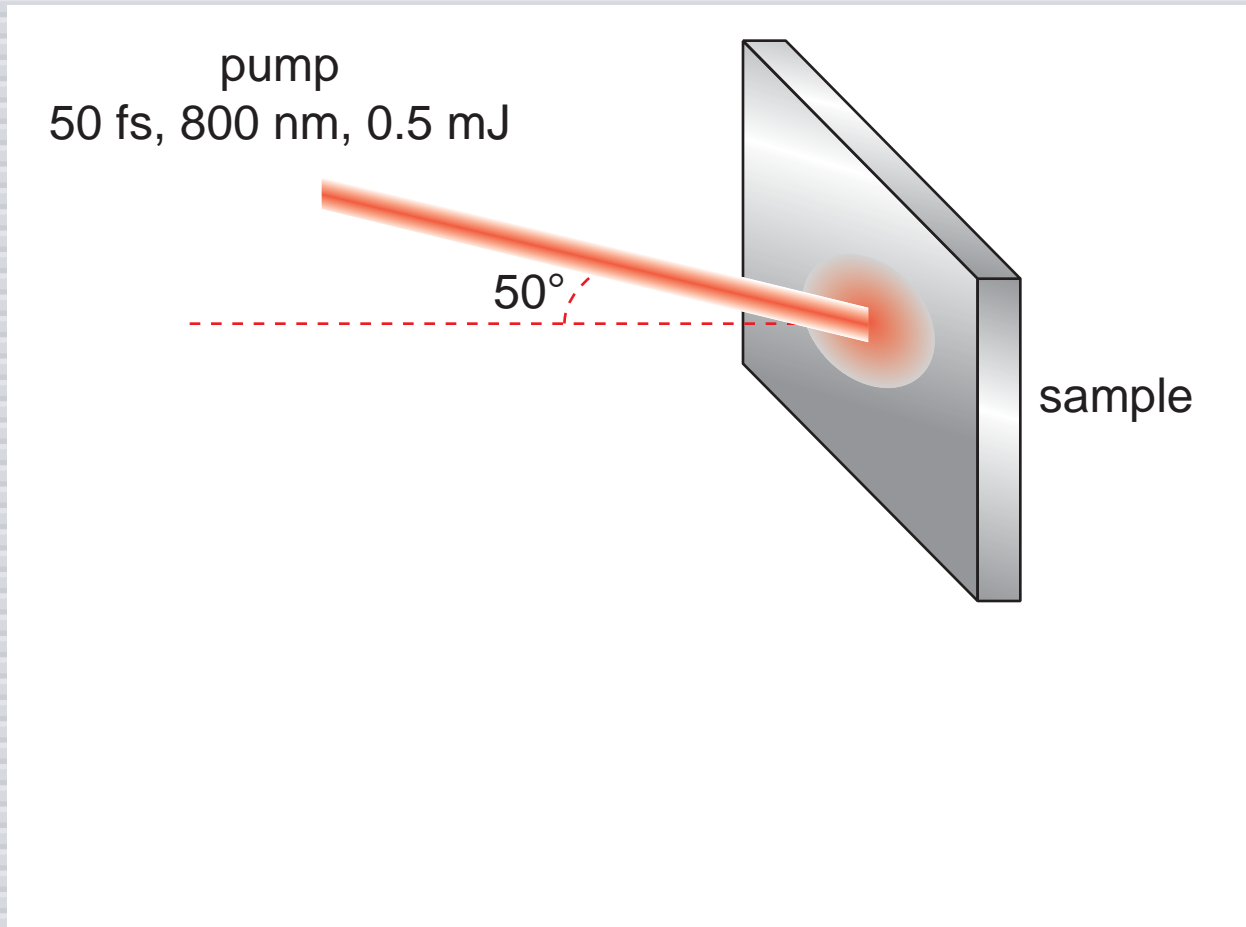
# *Technique*

## **broadband time-resolved ellipsometry**



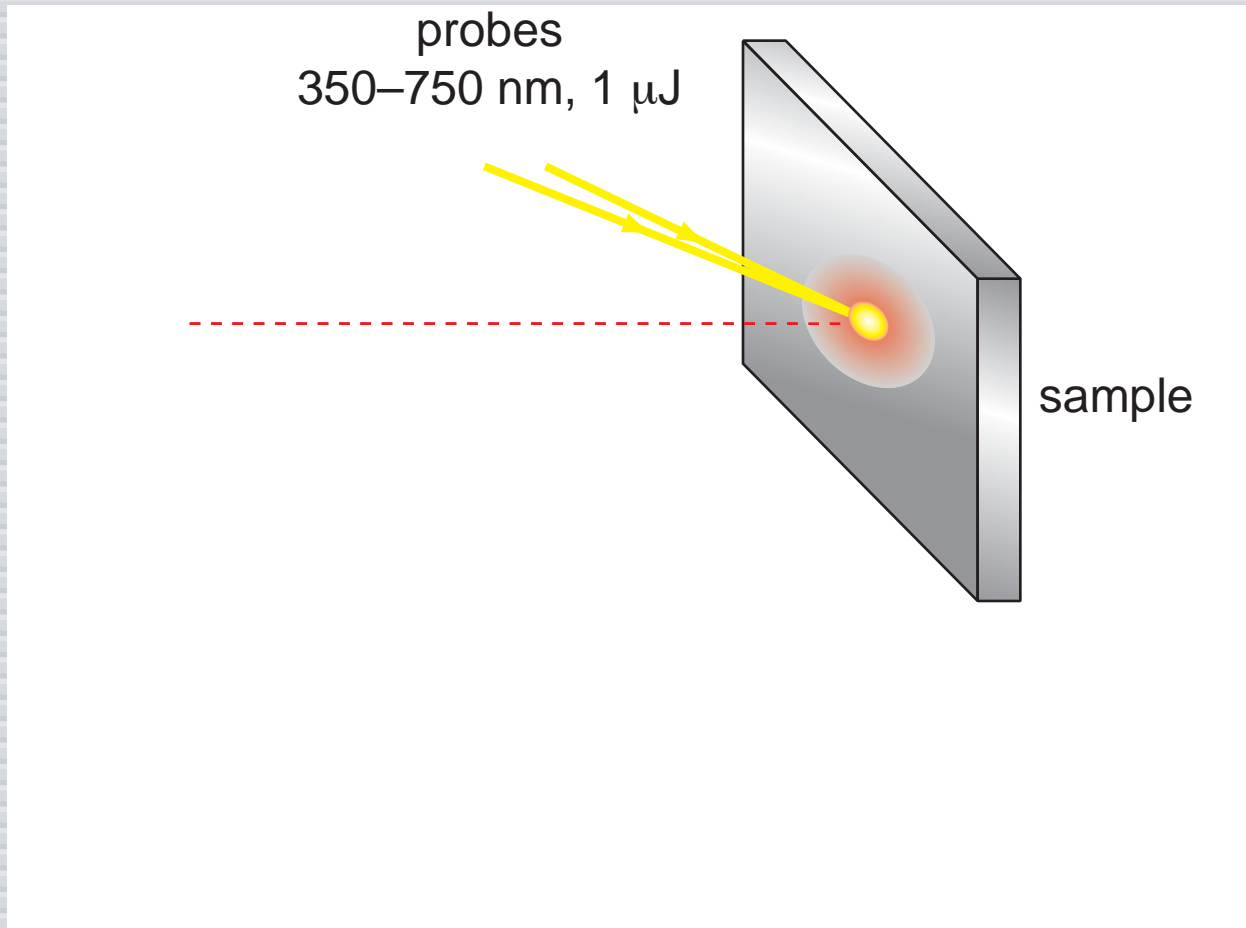
# Technique

## broadband time-resolved ellipsometry



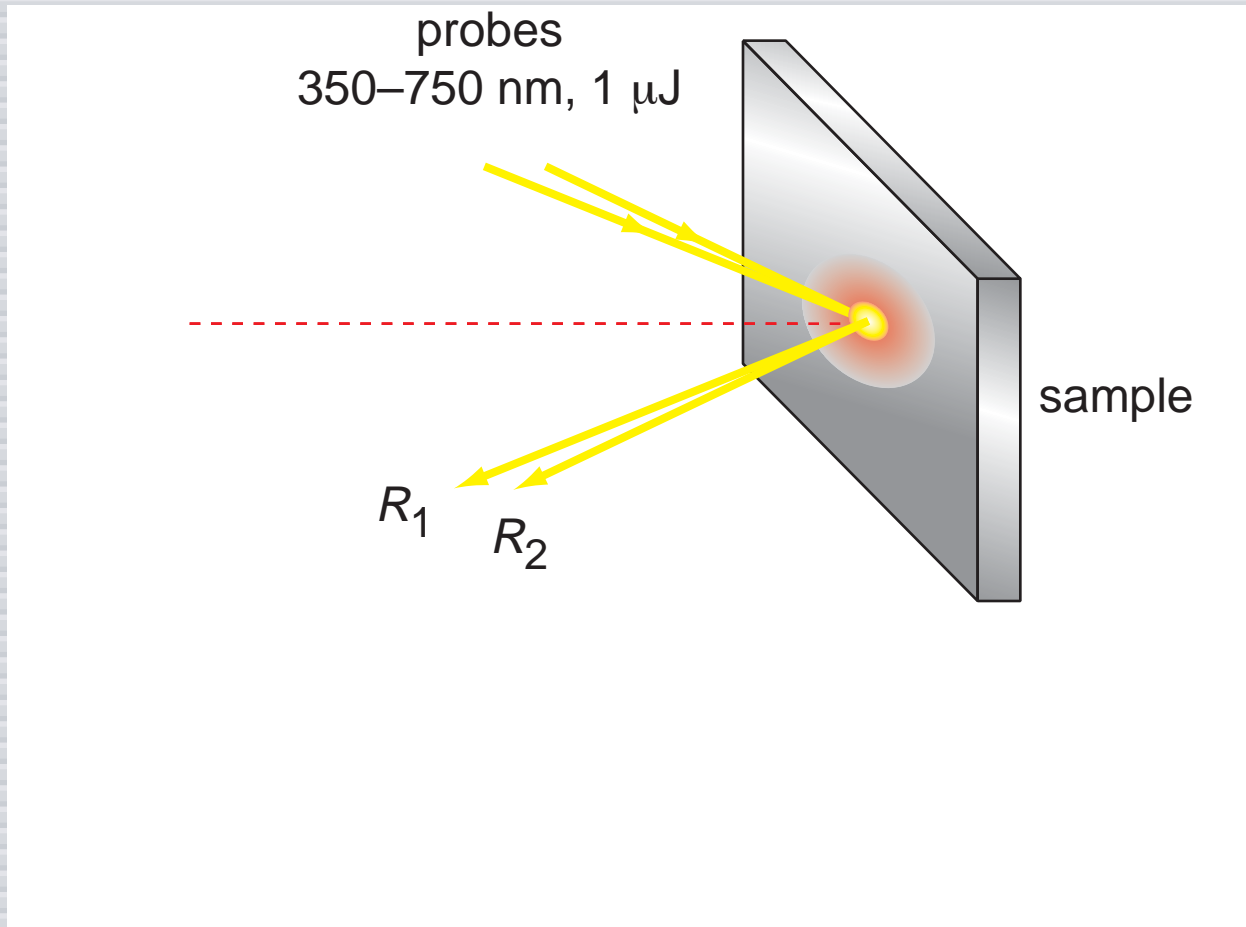
# Technique

## broadband time-resolved ellipsometry



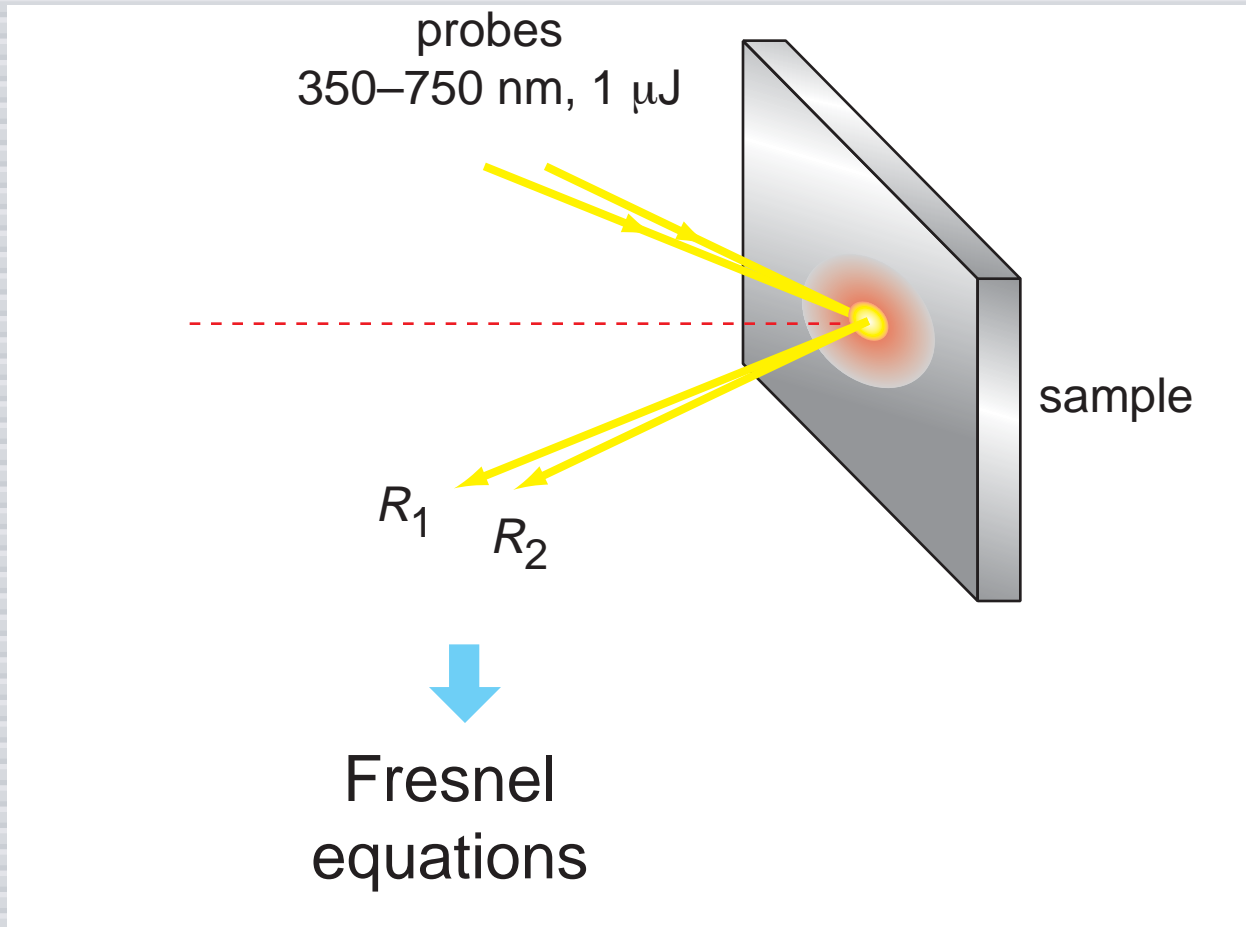
# Technique

## broadband time-resolved ellipsometry



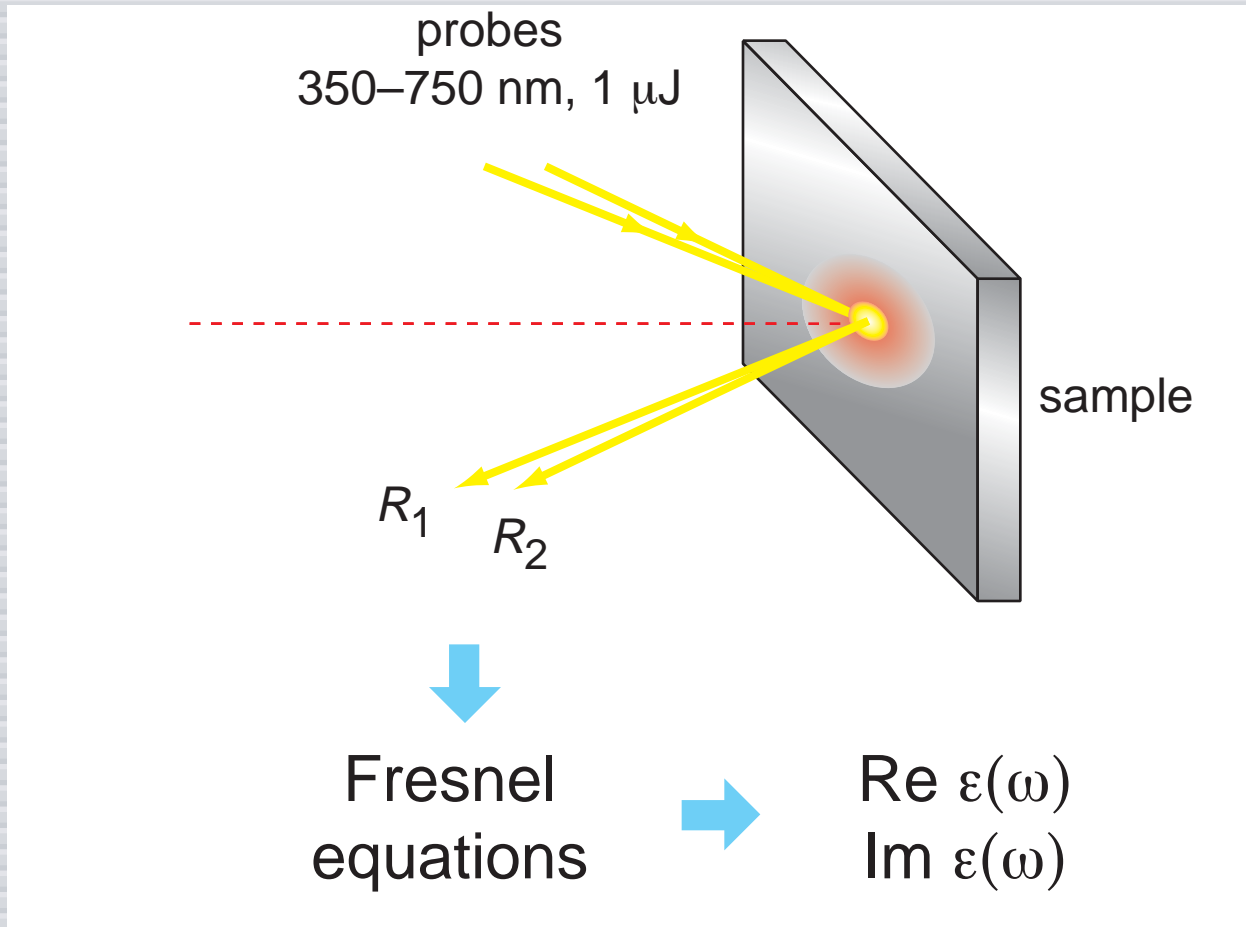
# Technique

## broadband time-resolved ellipsometry



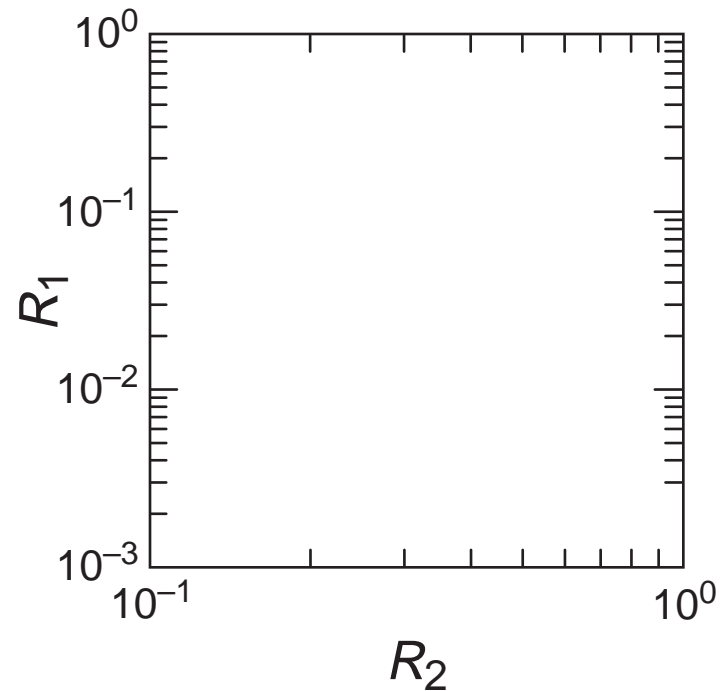
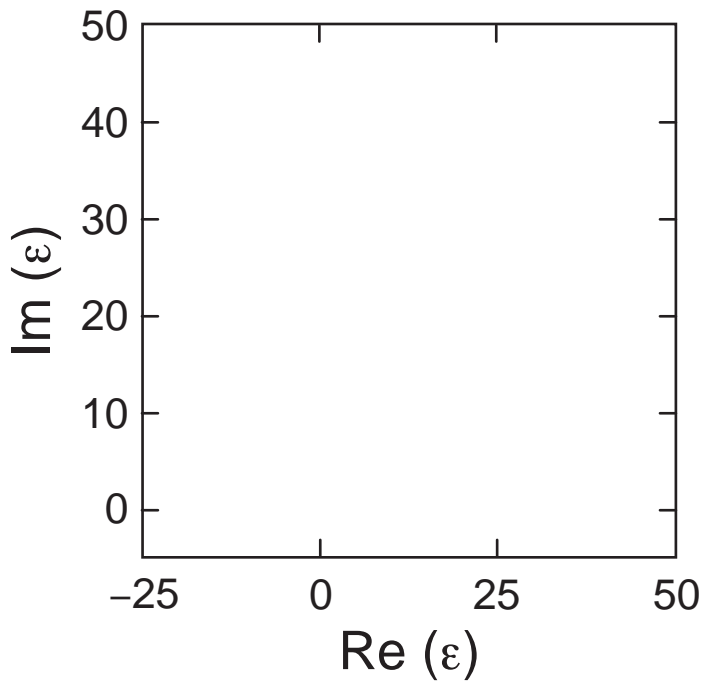
# Technique

## broadband time-resolved ellipsometry



# Technique

## choice of angles

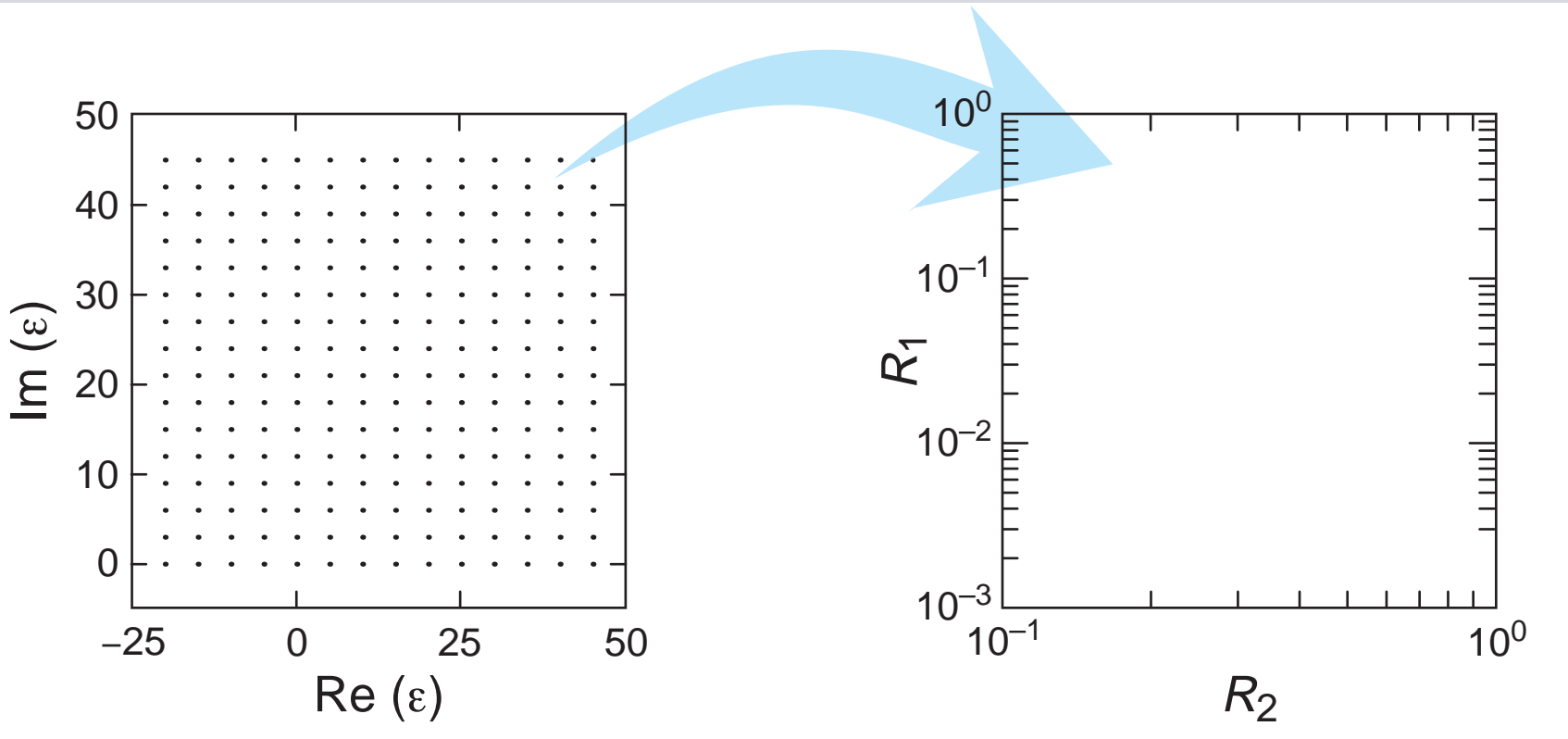


**Fresnel equations cannot be inverted analytically**



# Technique

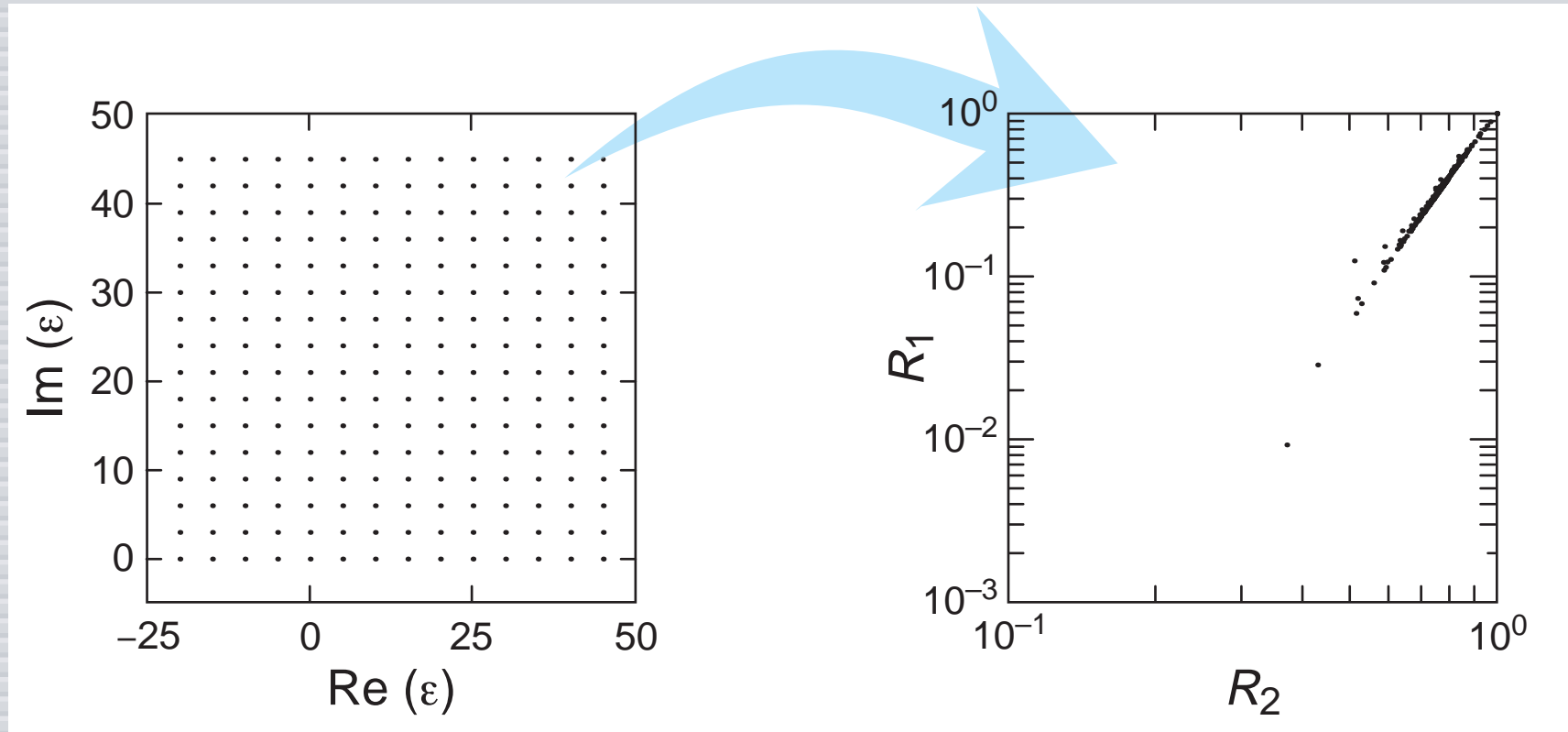
## choice of angles



**need numerical inversion**

# Technique

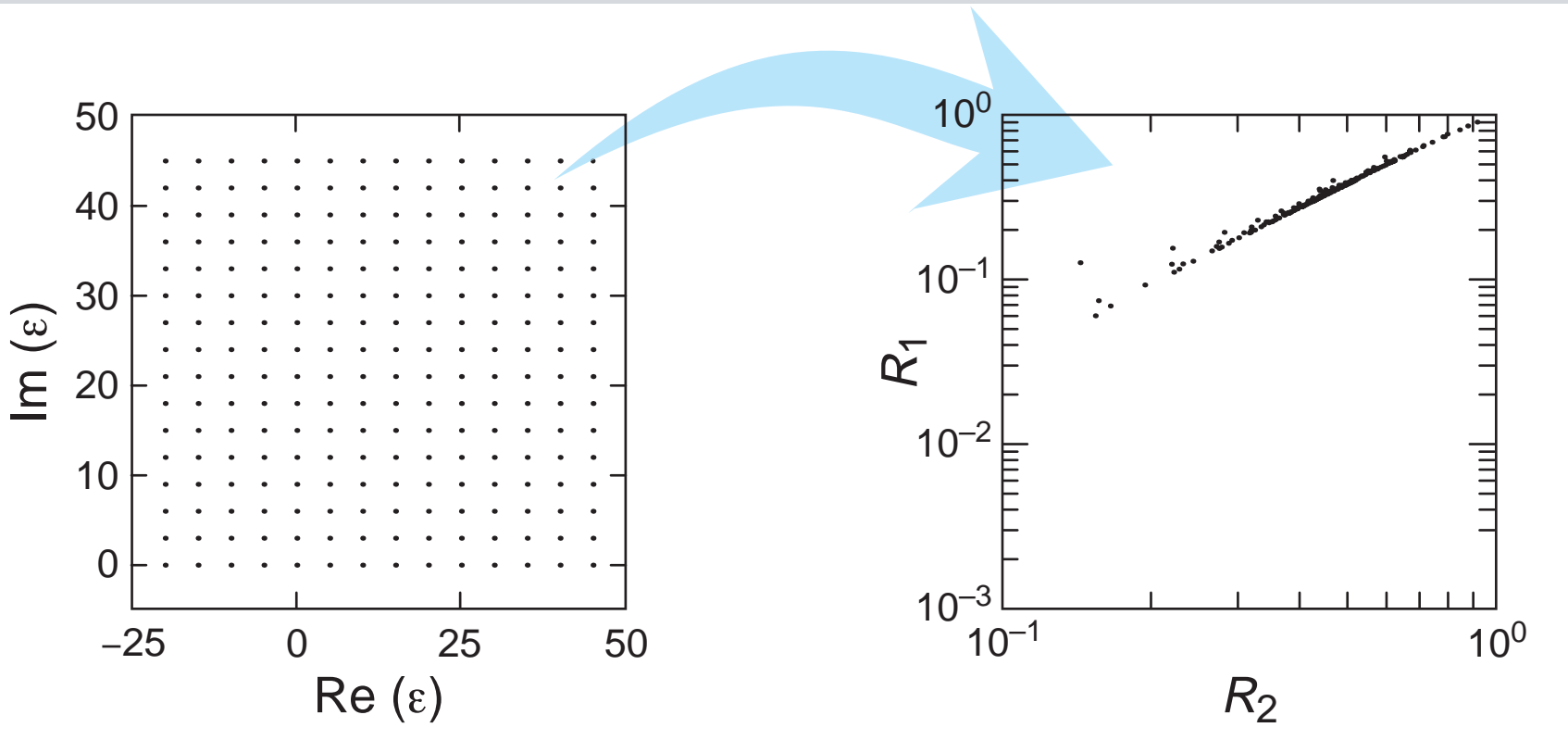
## choice of angles



$$R_1 = 45^\circ \text{ p-pol}, R_2 = 45^\circ \text{ s-pol}$$

# Technique

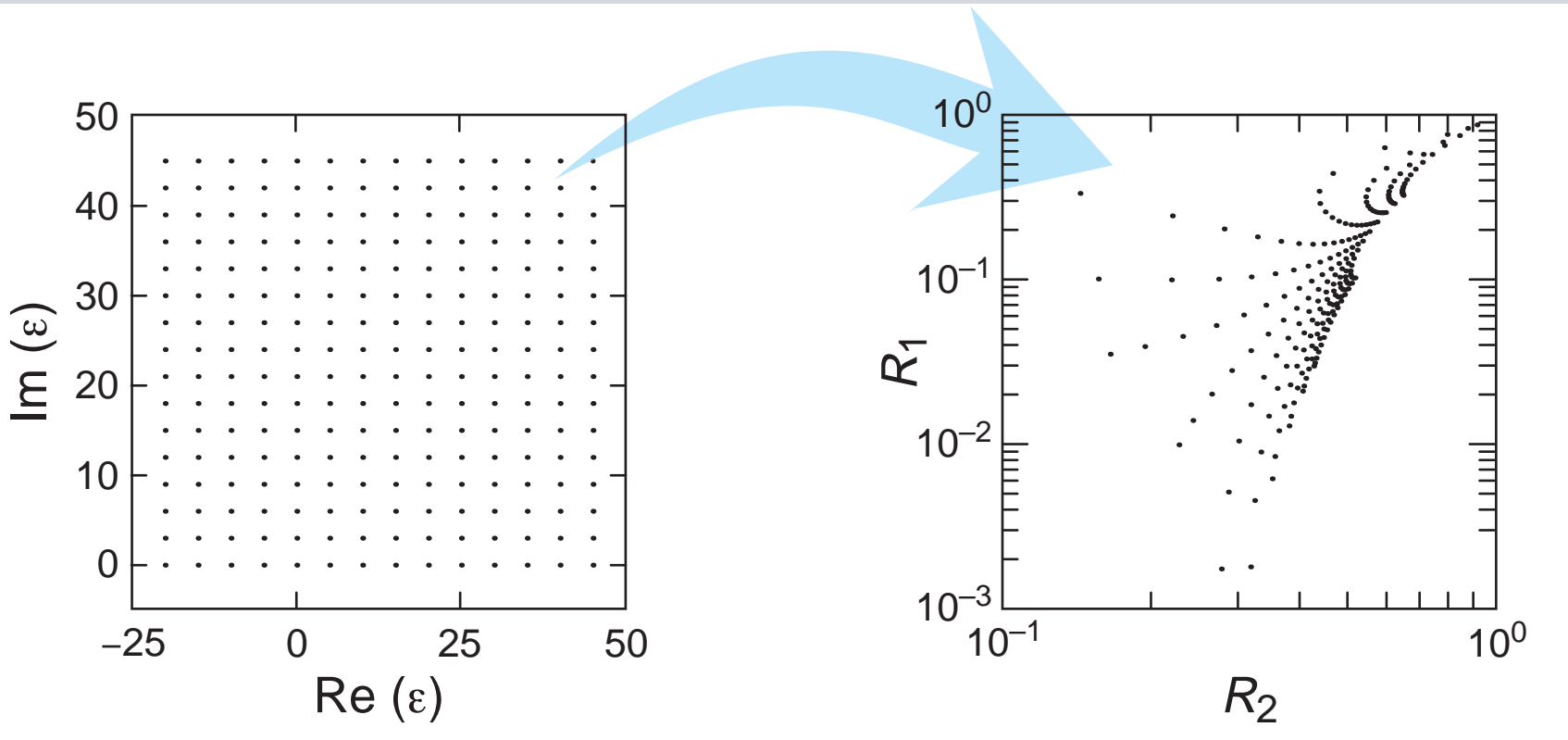
## choice of angles



$$R_1 = 60^\circ \text{ p-pol}, R_2 = 45^\circ \text{ p-pol}$$

# Technique

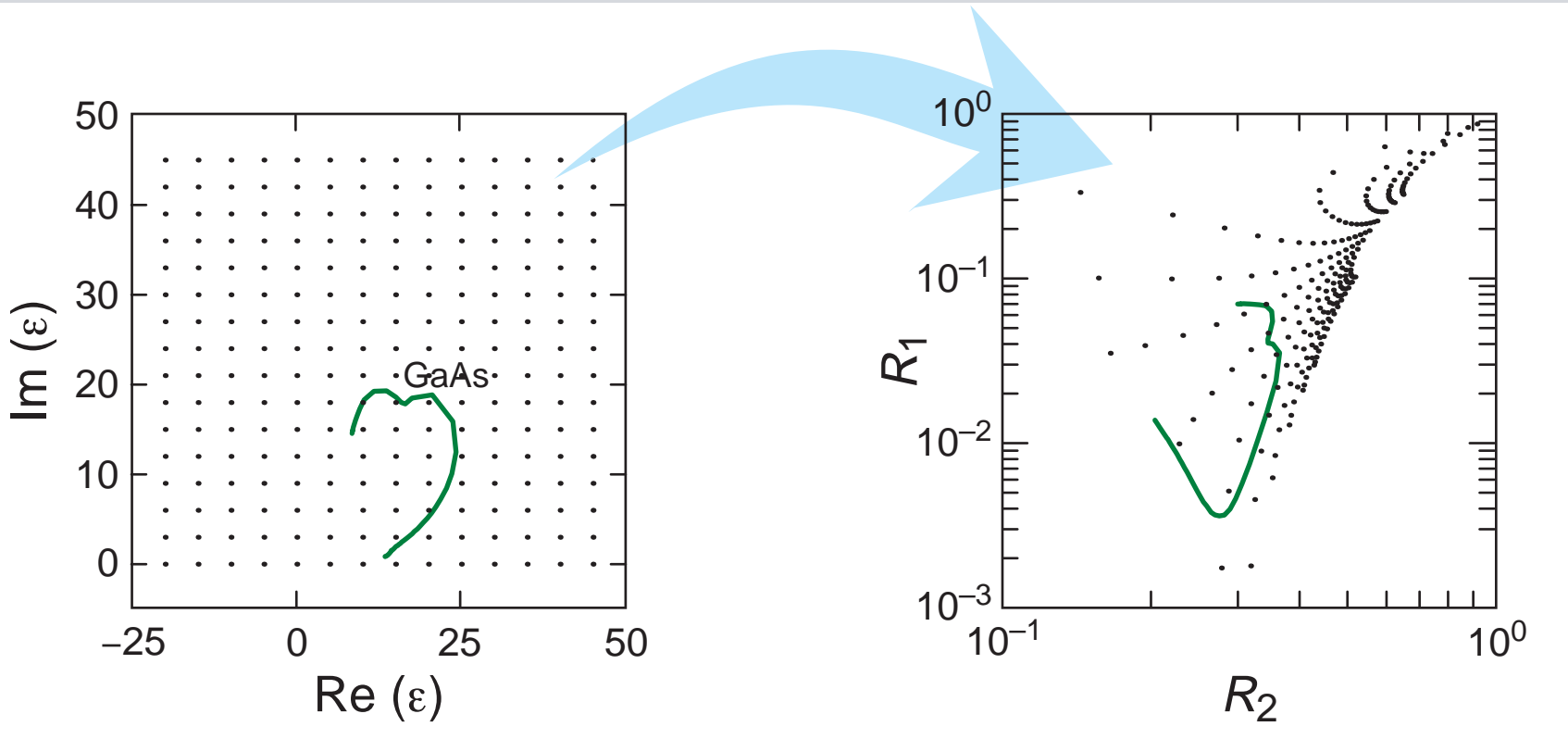
## choice of angles



$$R_1 = 78^\circ \text{ p-pol}, R_2 = 45^\circ \text{ p-pol}$$

# Technique

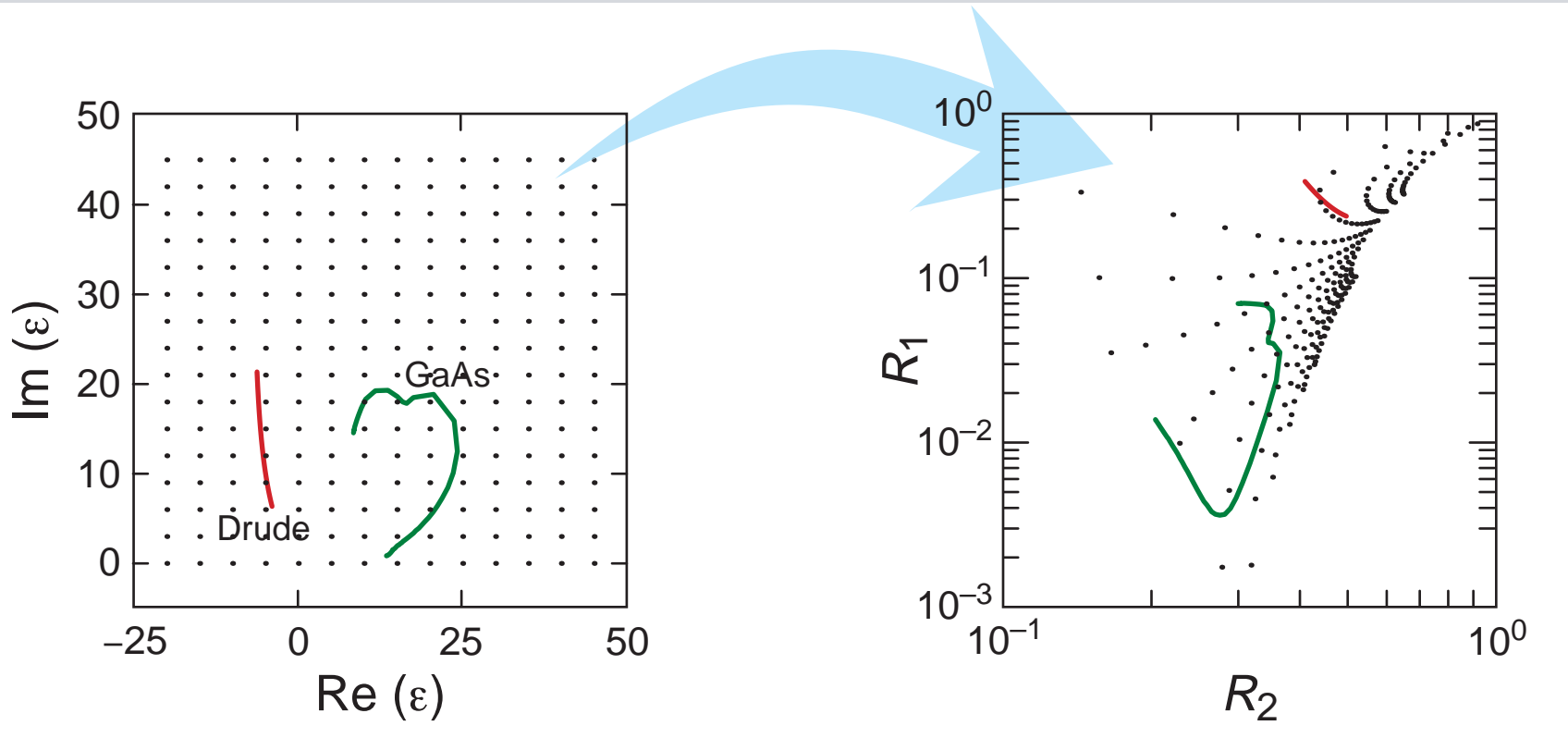
## choice of angles



$$R_1 = 78^\circ \text{ p-pol}, R_2 = 45^\circ \text{ p-pol}$$

# Technique

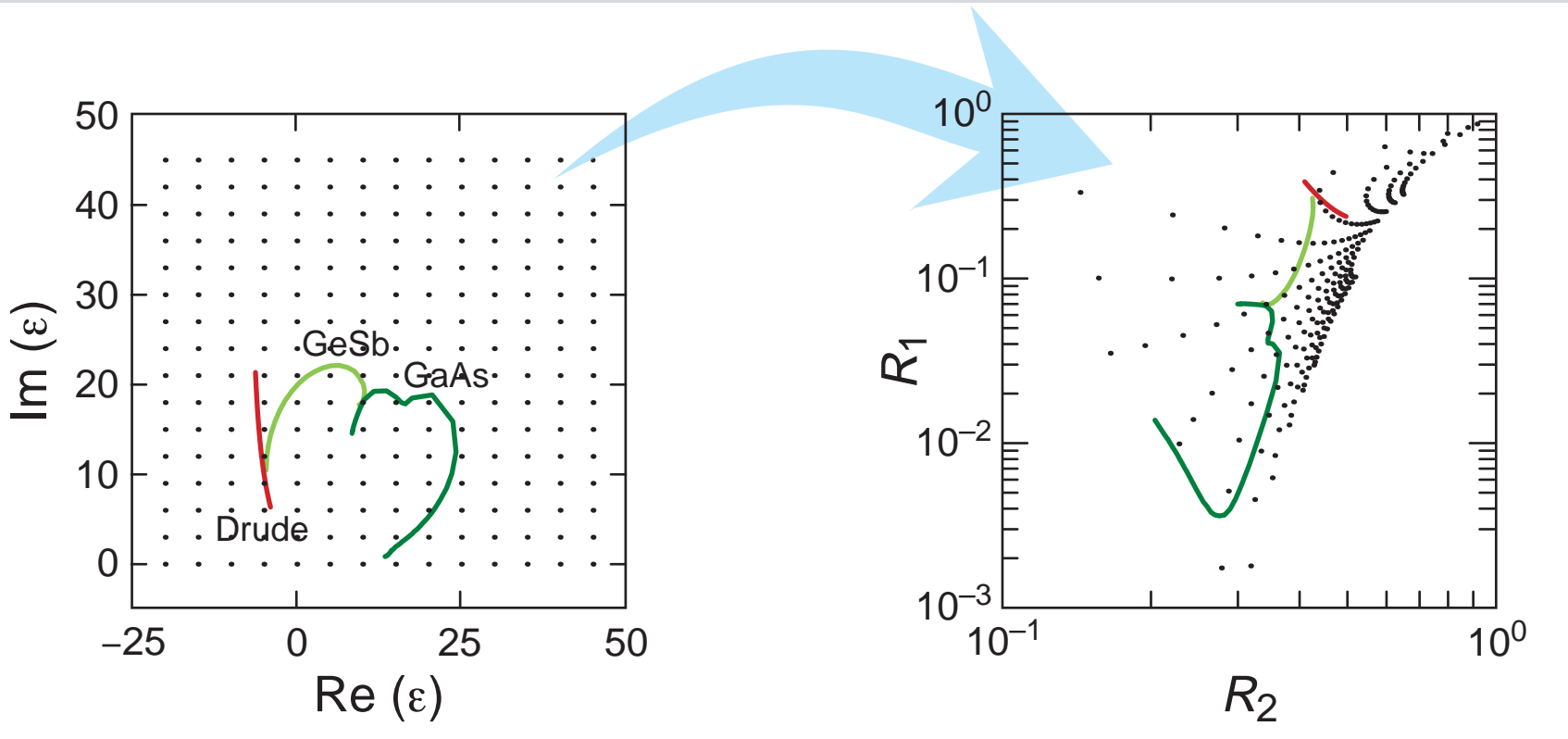
## choice of angles



$$R_1 = 78^\circ \text{ p-pol}, R_2 = 45^\circ \text{ p-pol}$$

# Technique

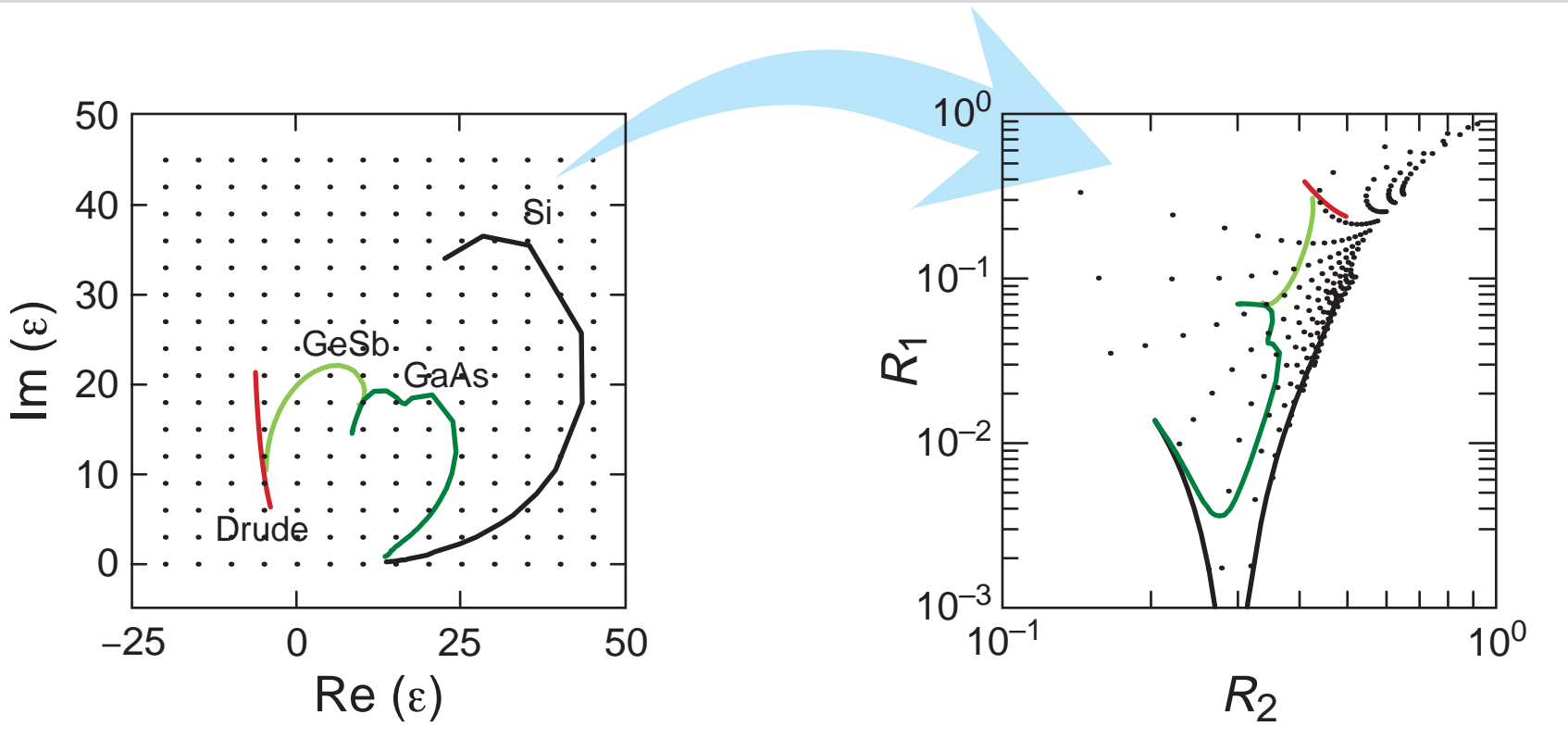
## choice of angles



$$R_1 = 78^\circ \text{ p-pol}, R_2 = 45^\circ \text{ p-pol}$$

# Technique

## choice of angles

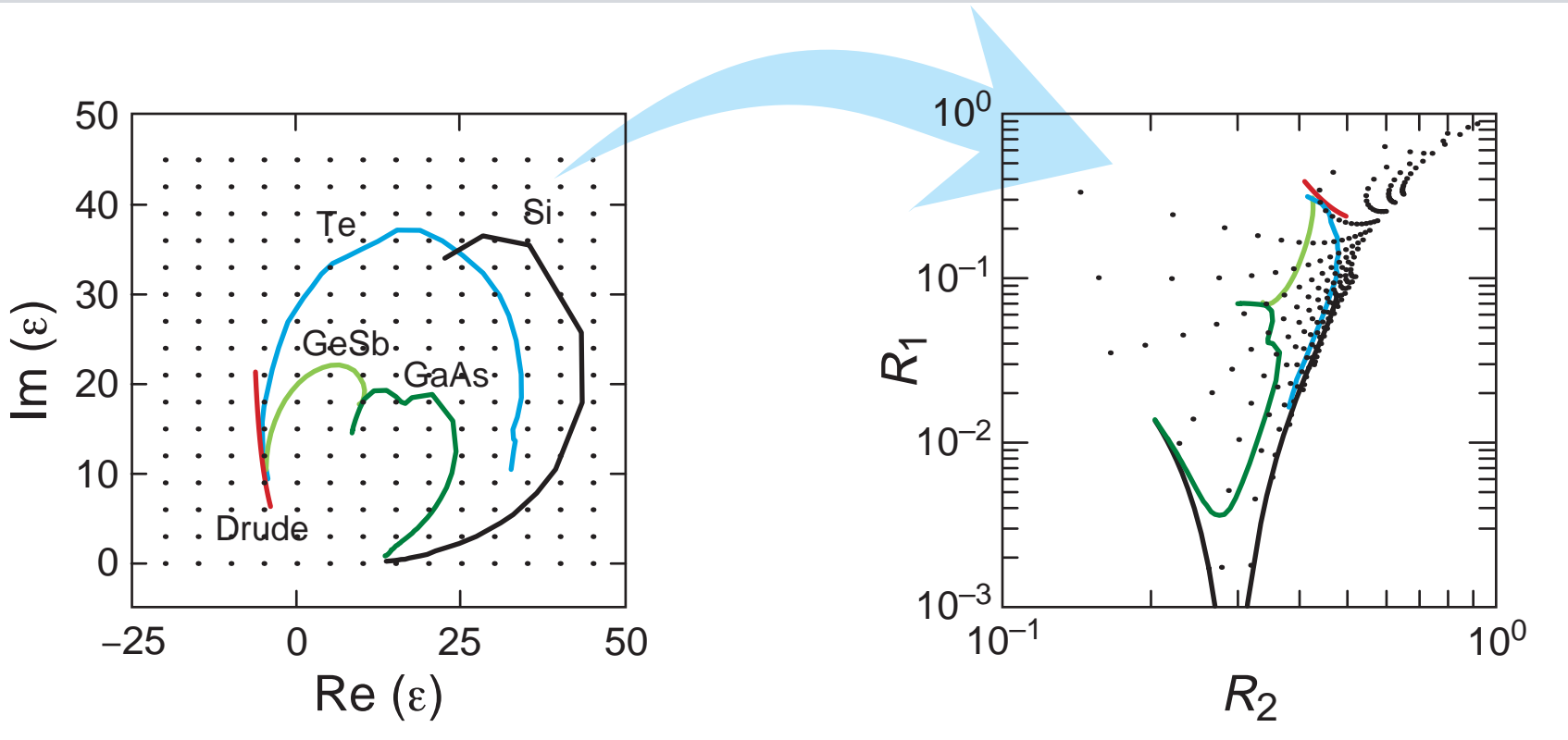


$$R_1 = 78^\circ \text{ p-pol}, R_2 = 45^\circ \text{ p-pol}$$



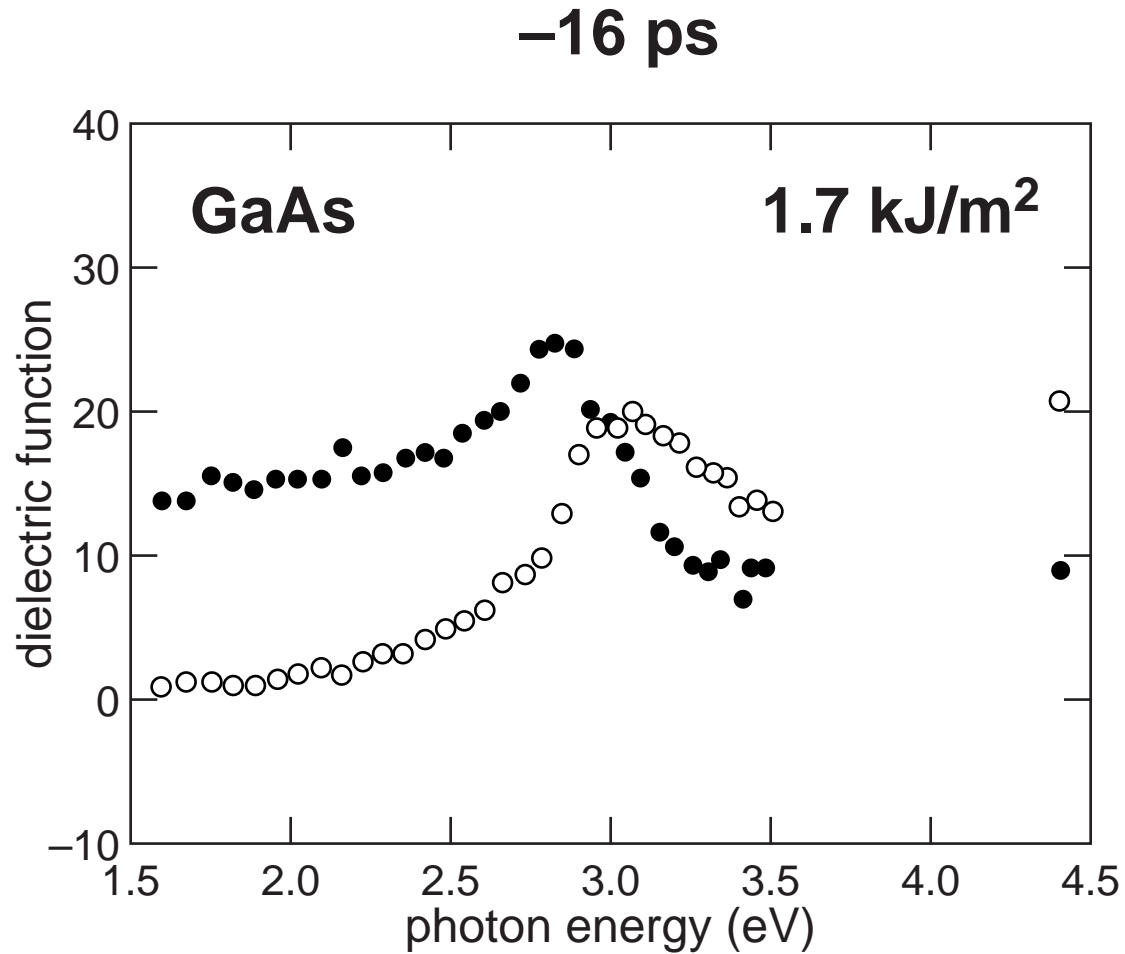
# Technique

## choice of angles

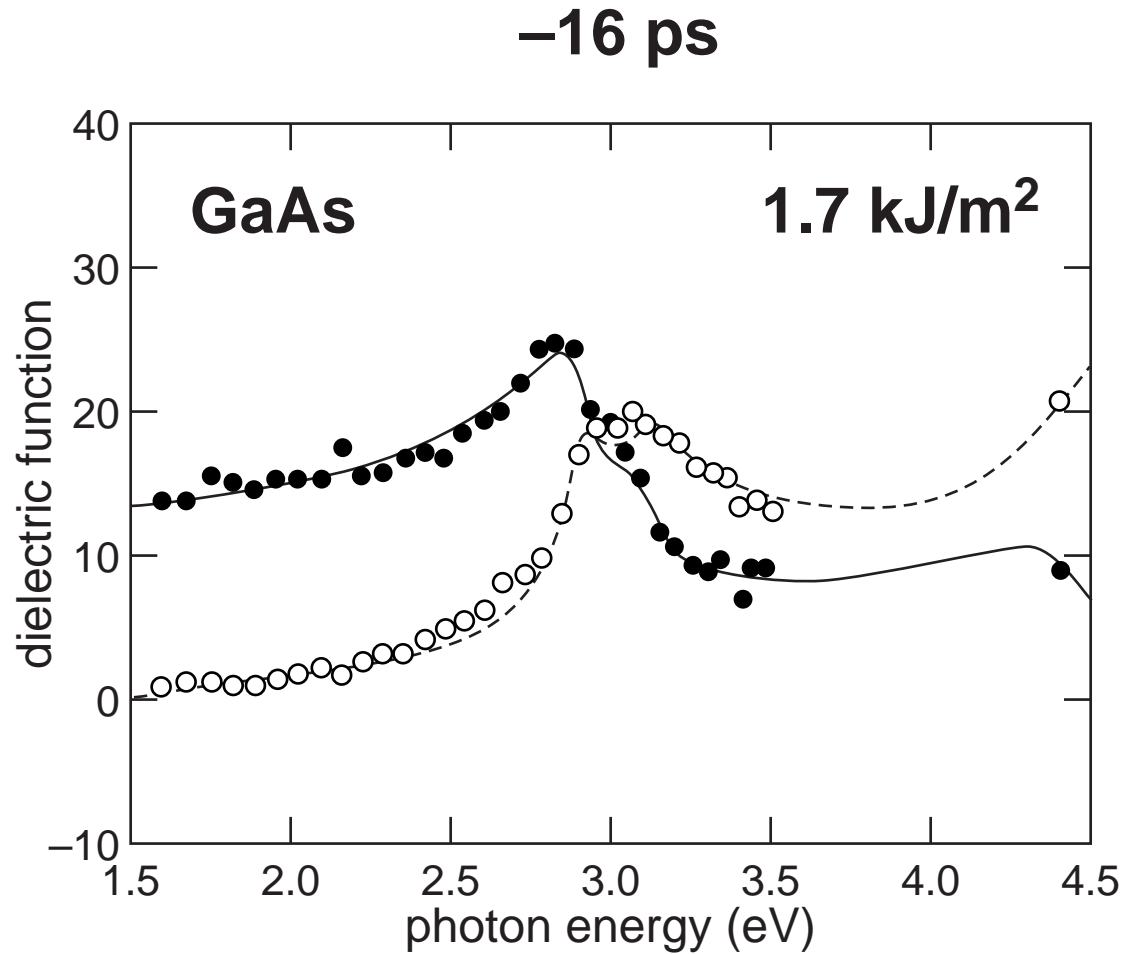


$$R_1 = 78^\circ \text{ p-pol}, R_2 = 45^\circ \text{ p-pol}$$

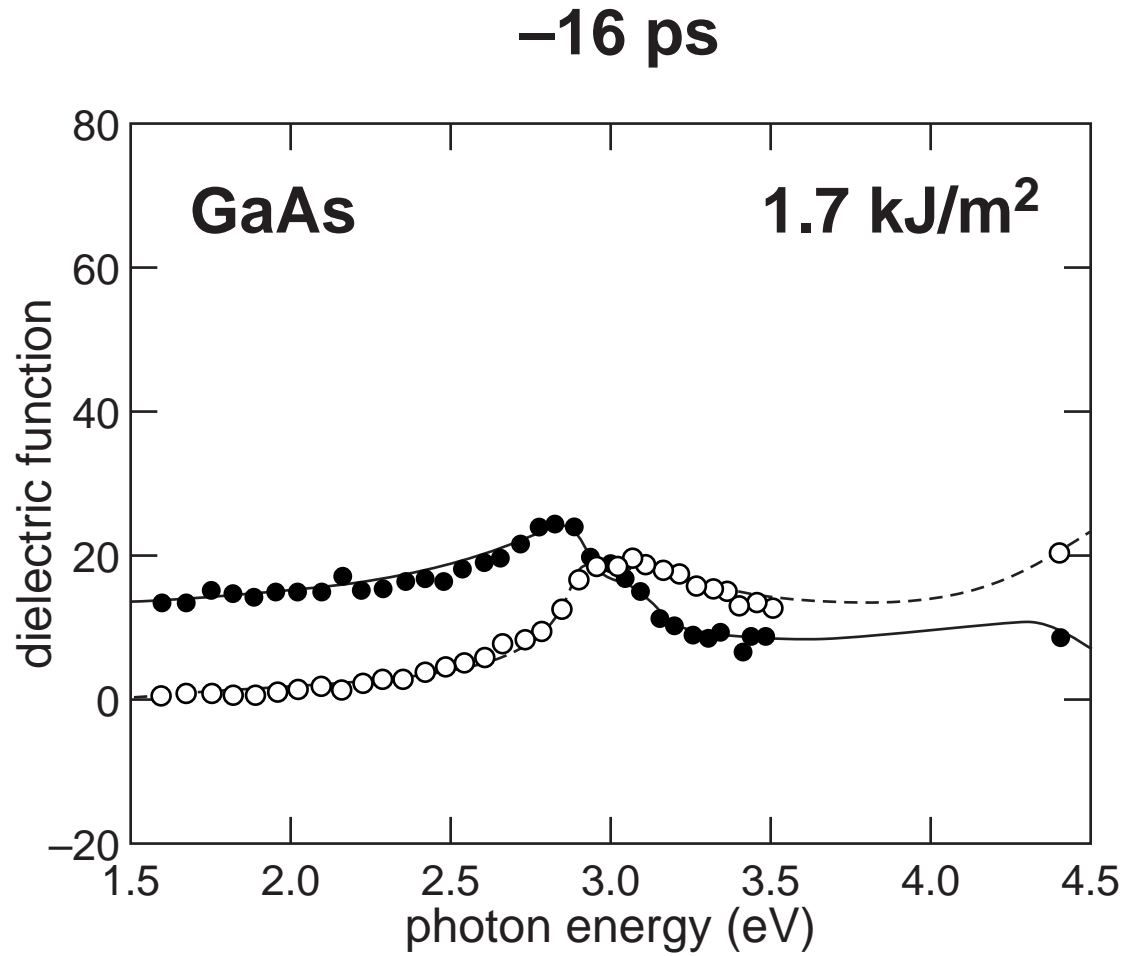
# Technique



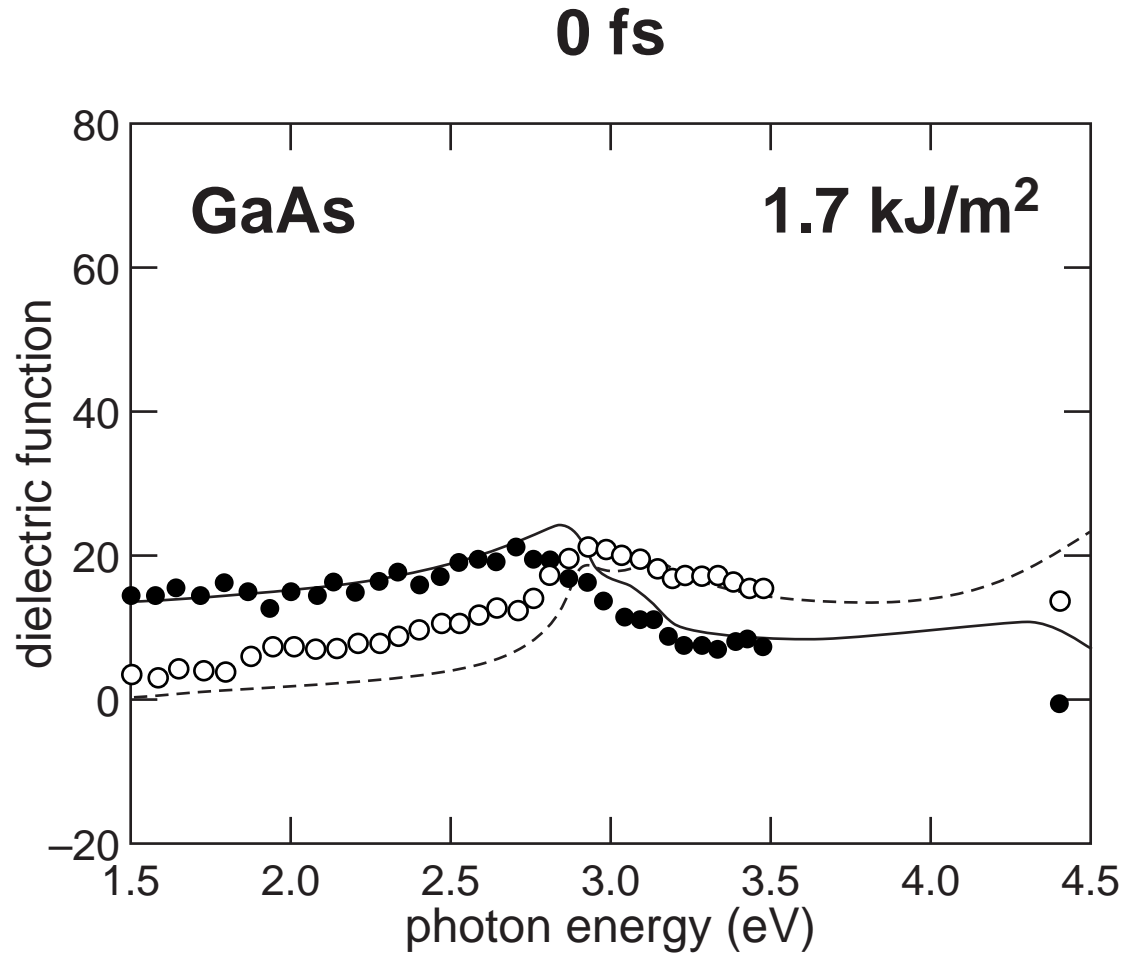
# Technique



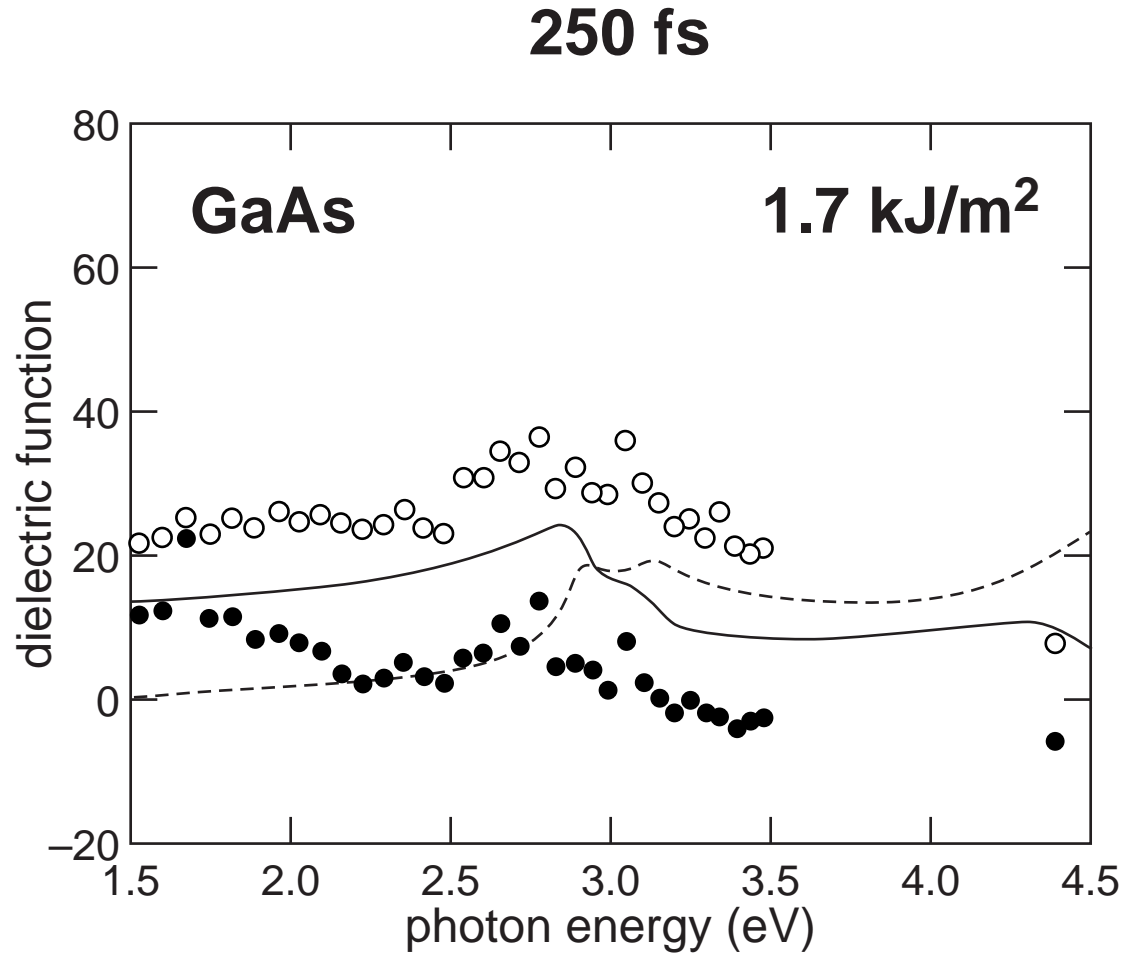
# Technique



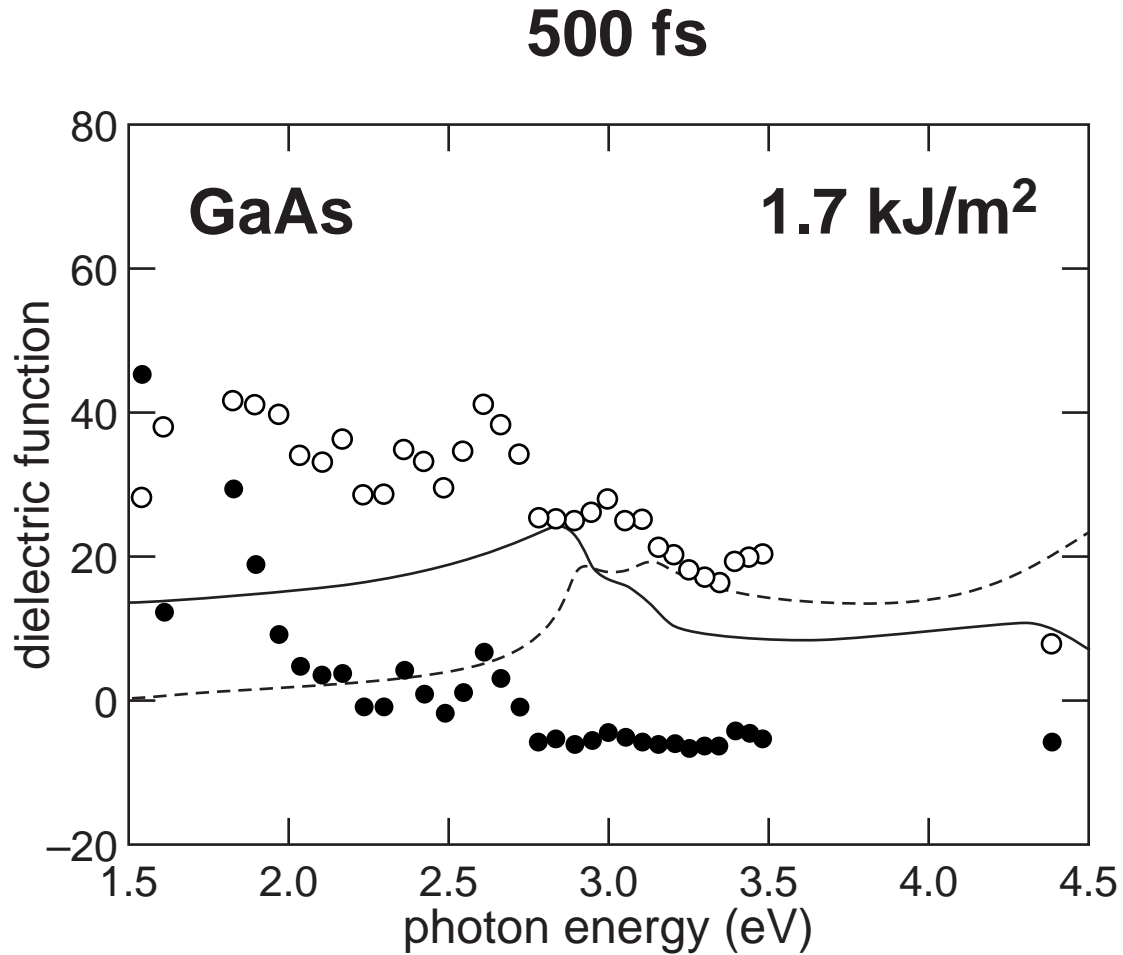
# Technique



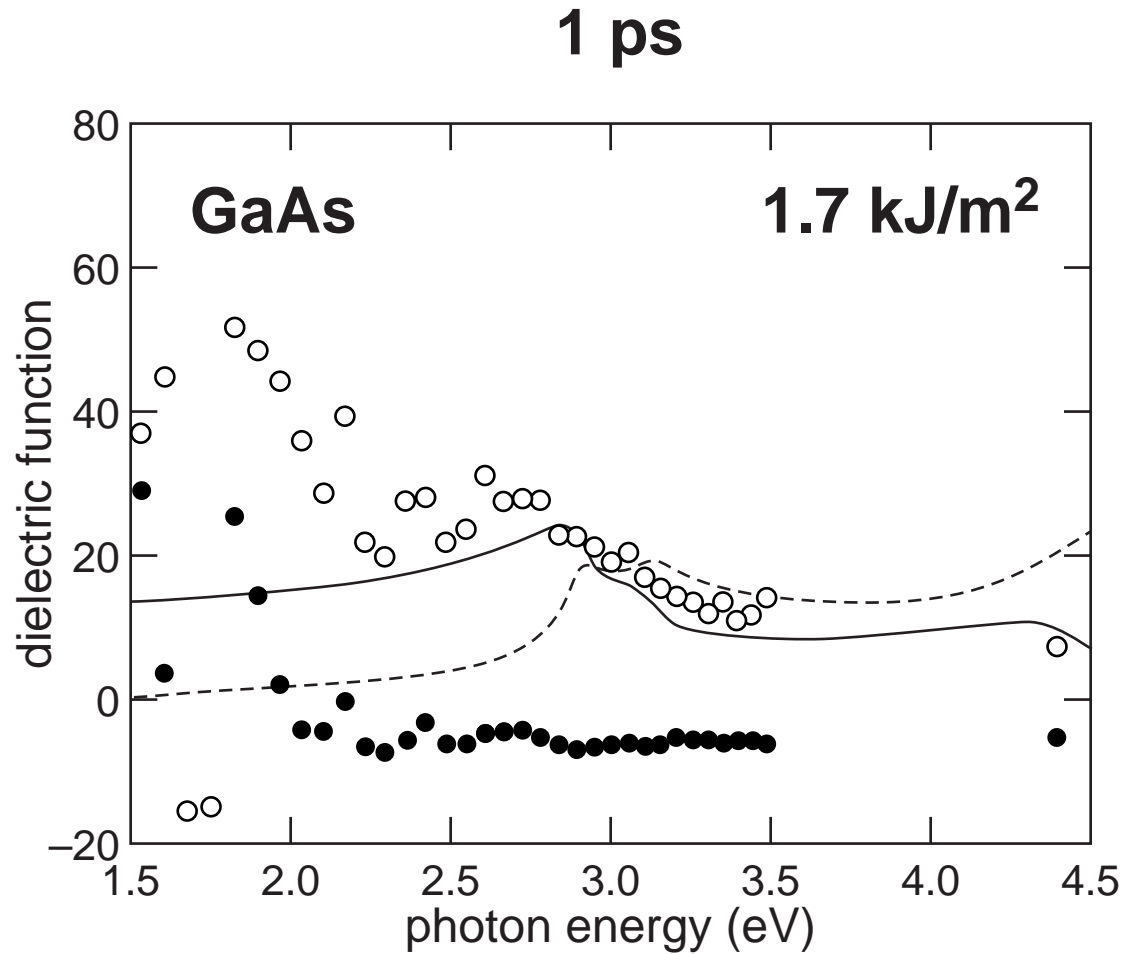
# Technique



# Technique

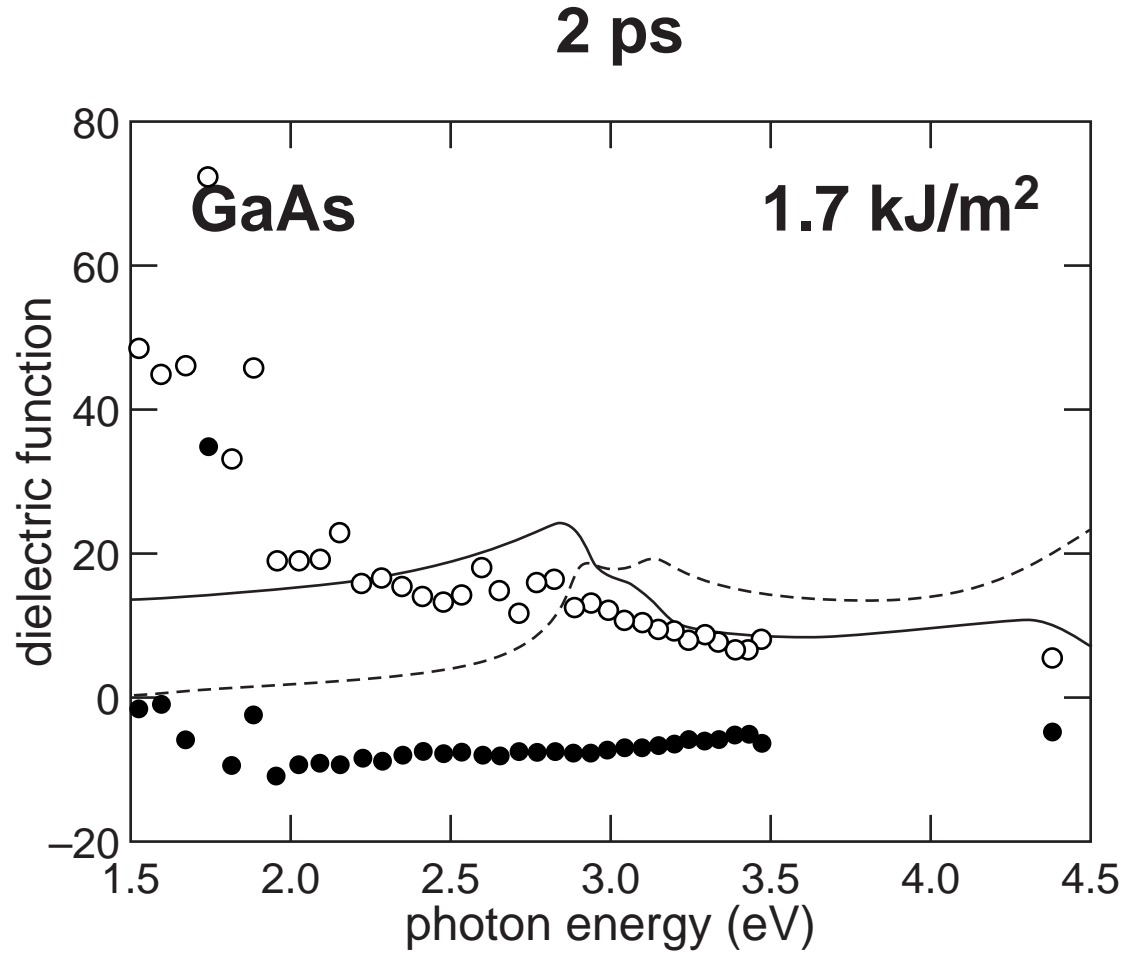


# Technique

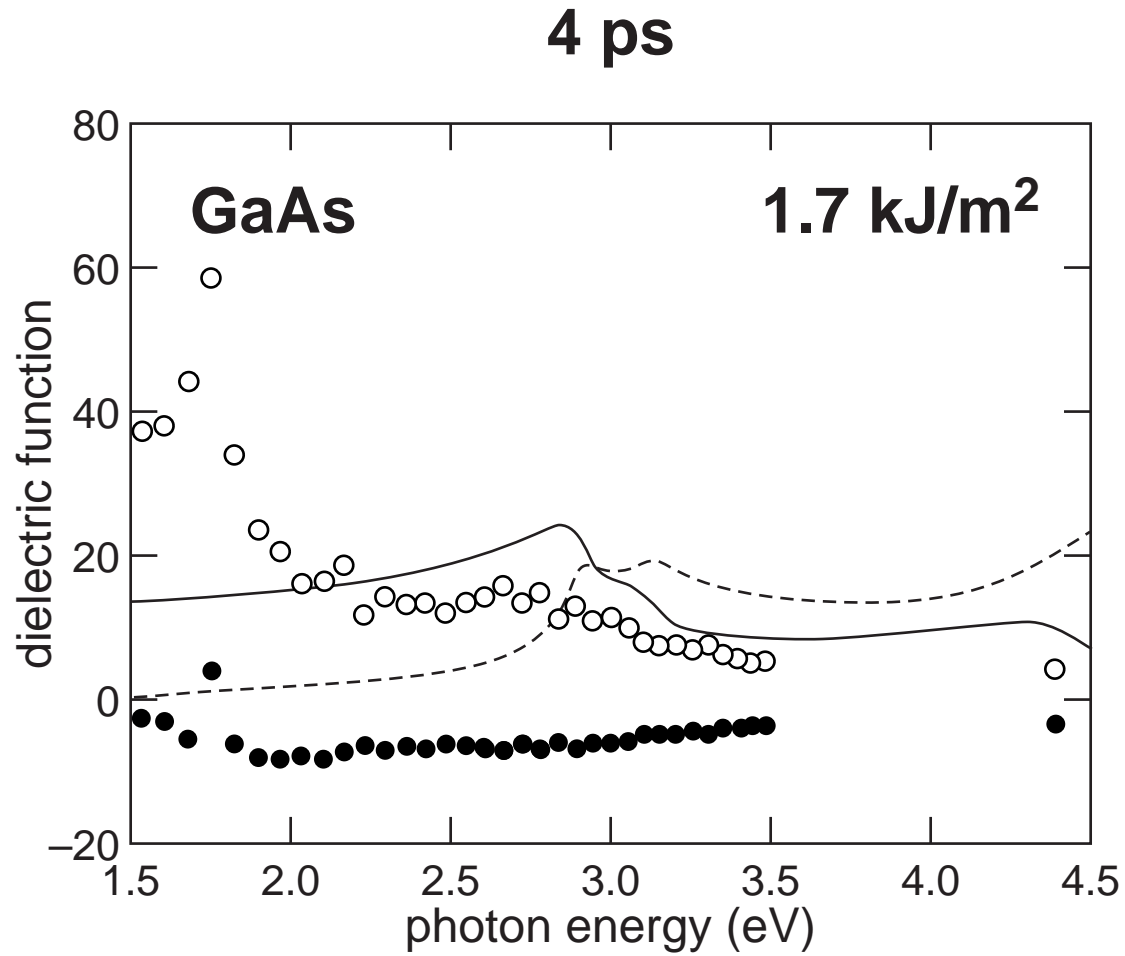




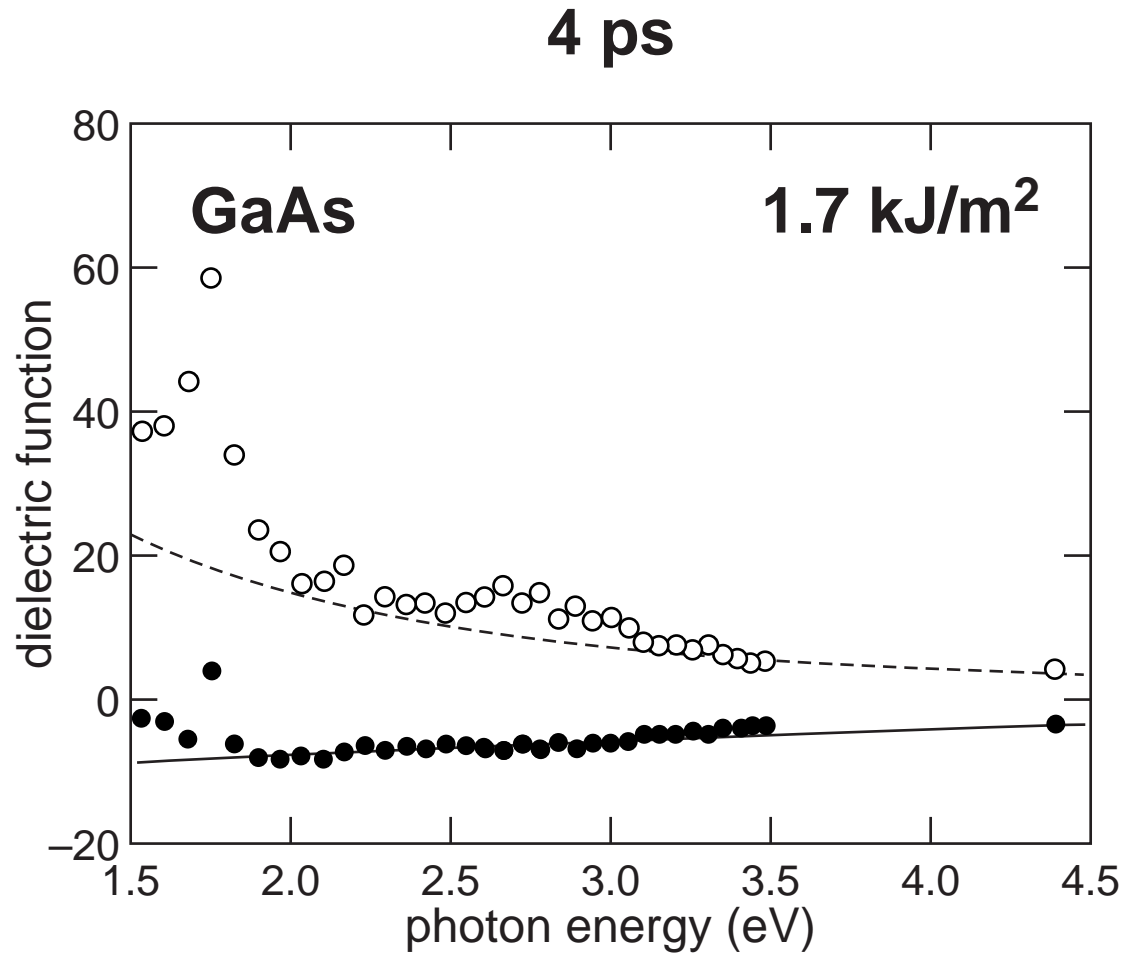
# Technique



# Technique



# Technique

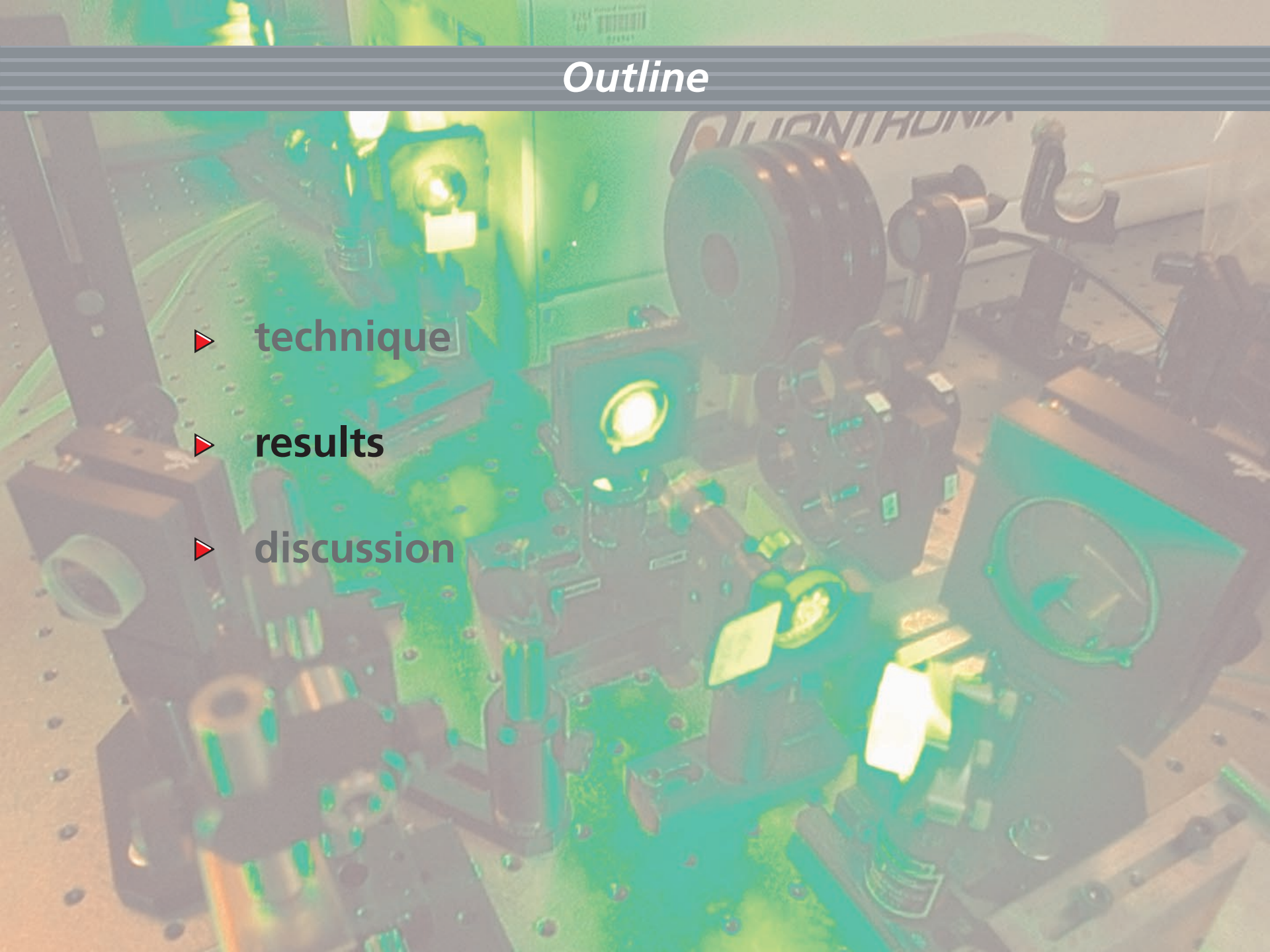


# *Technique*

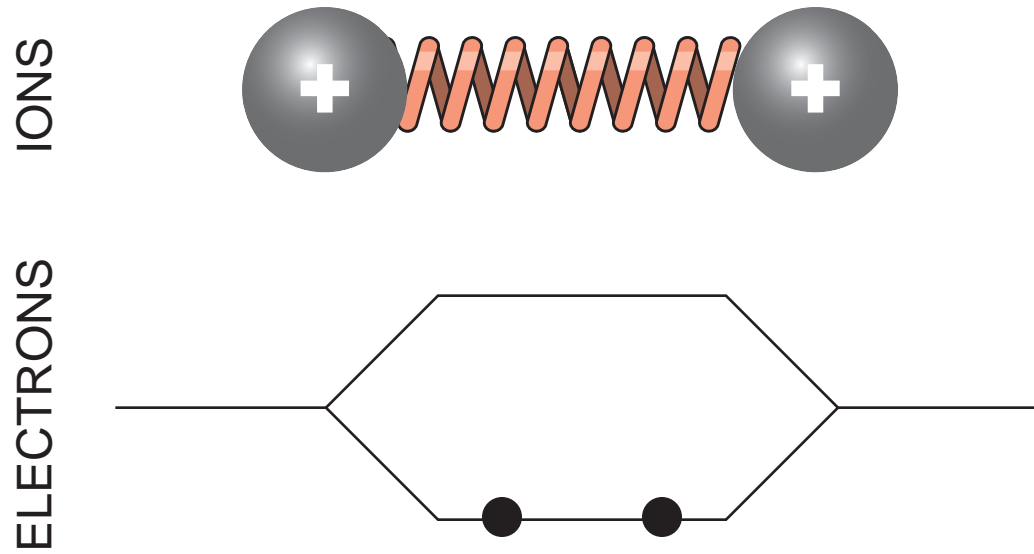
- ▶ **direct observation of semiconductor-to-metal transition**
- ▶ **order-disorder transition**
- ▶ **transition structural, not electronic**

# Outline

- ▶ **technique**
- ▶ **results**
- ▶ **discussion**

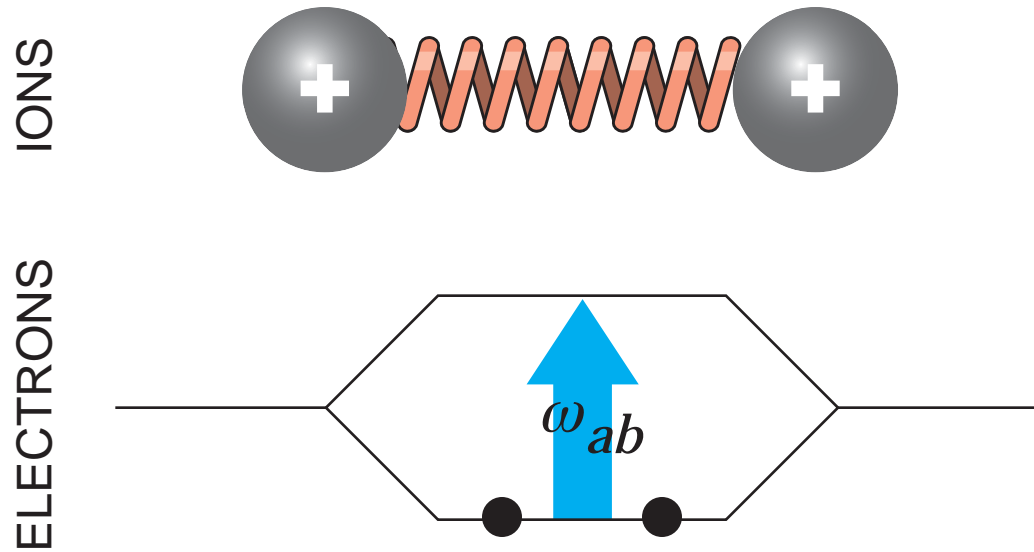


# *Displacive excitation*



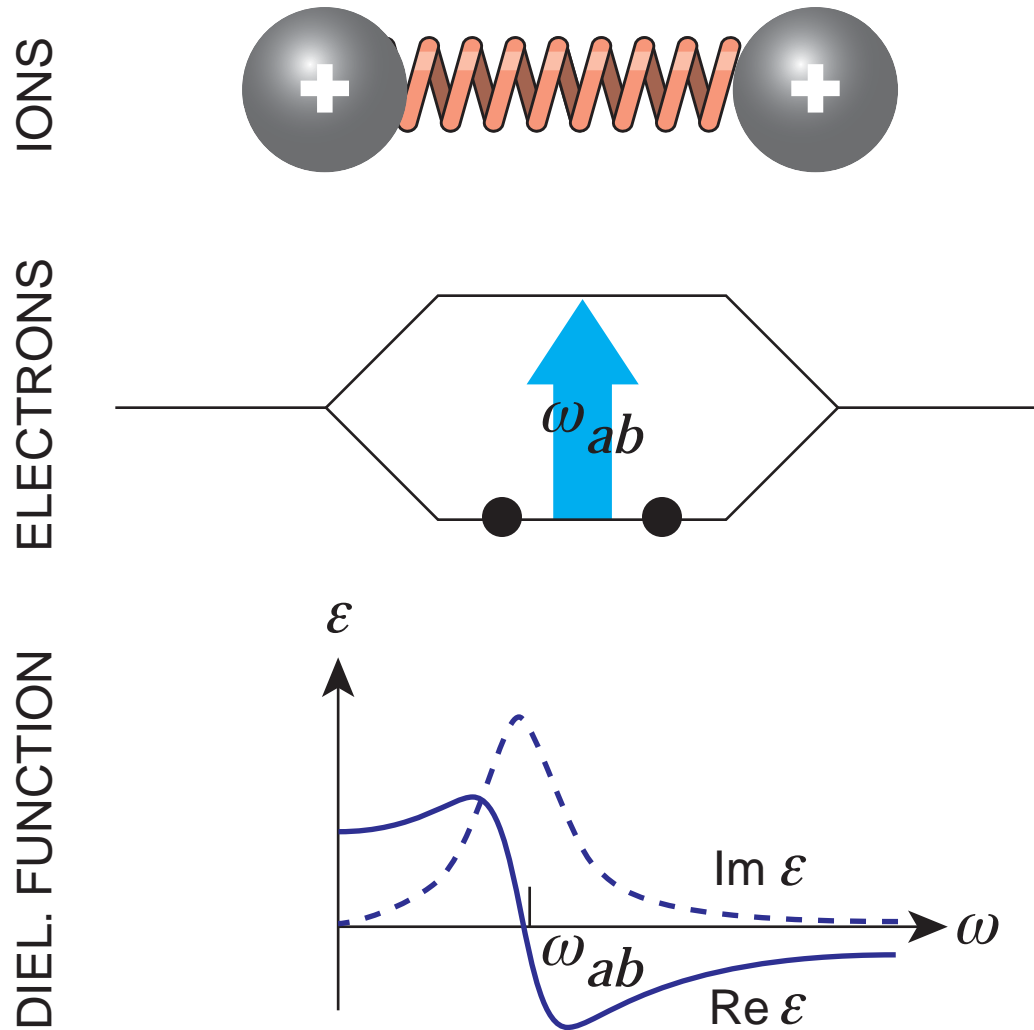
**“two-atom model”**

# *Displacive excitation*



**bonding-antibonding splitting**

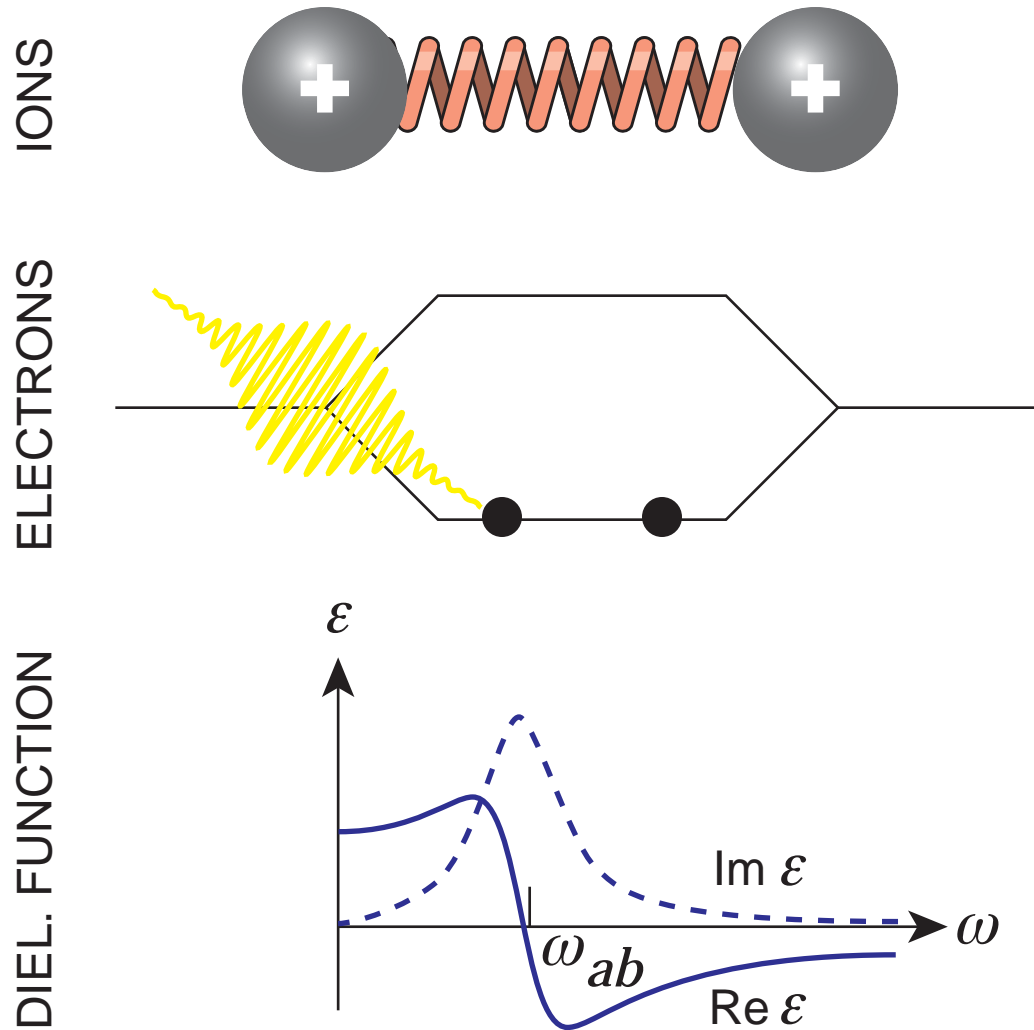
# Displacive excitation



**Lorentz model**

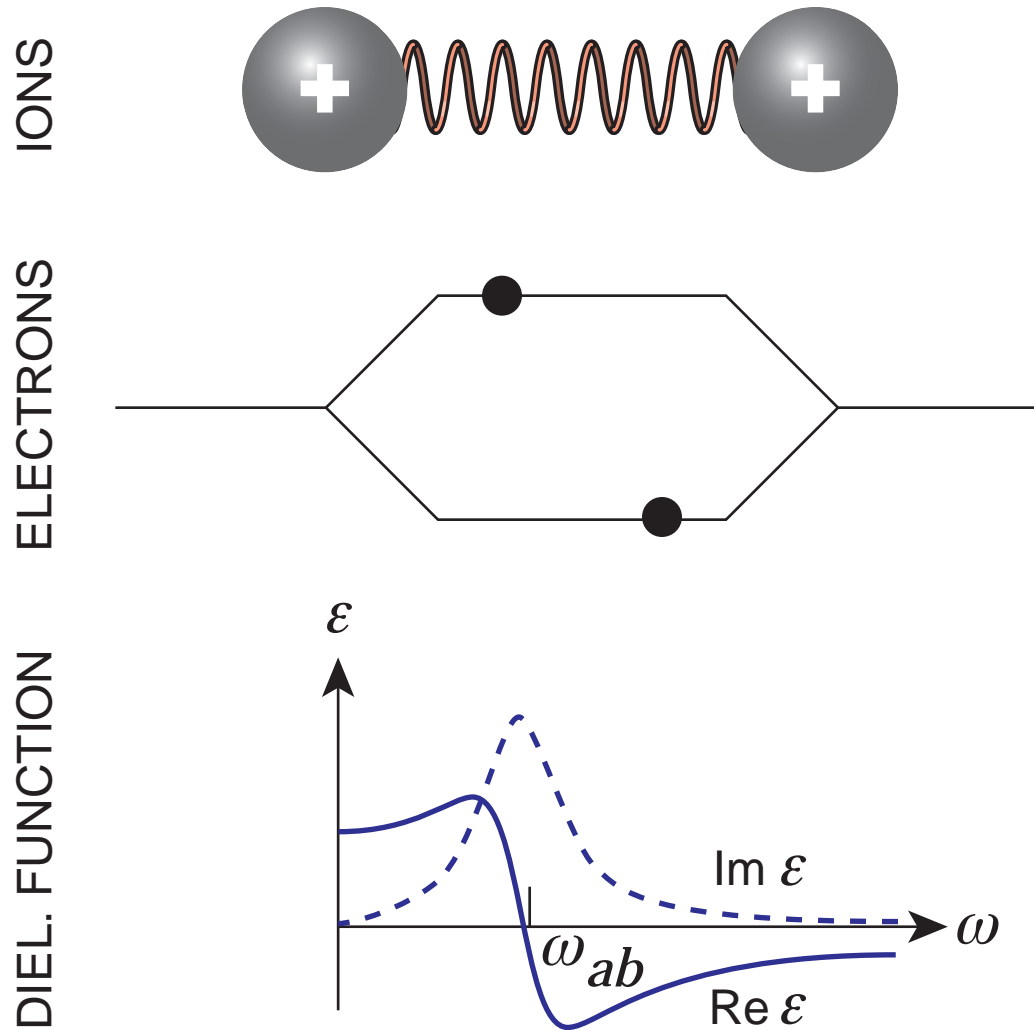


# Displacive excitation



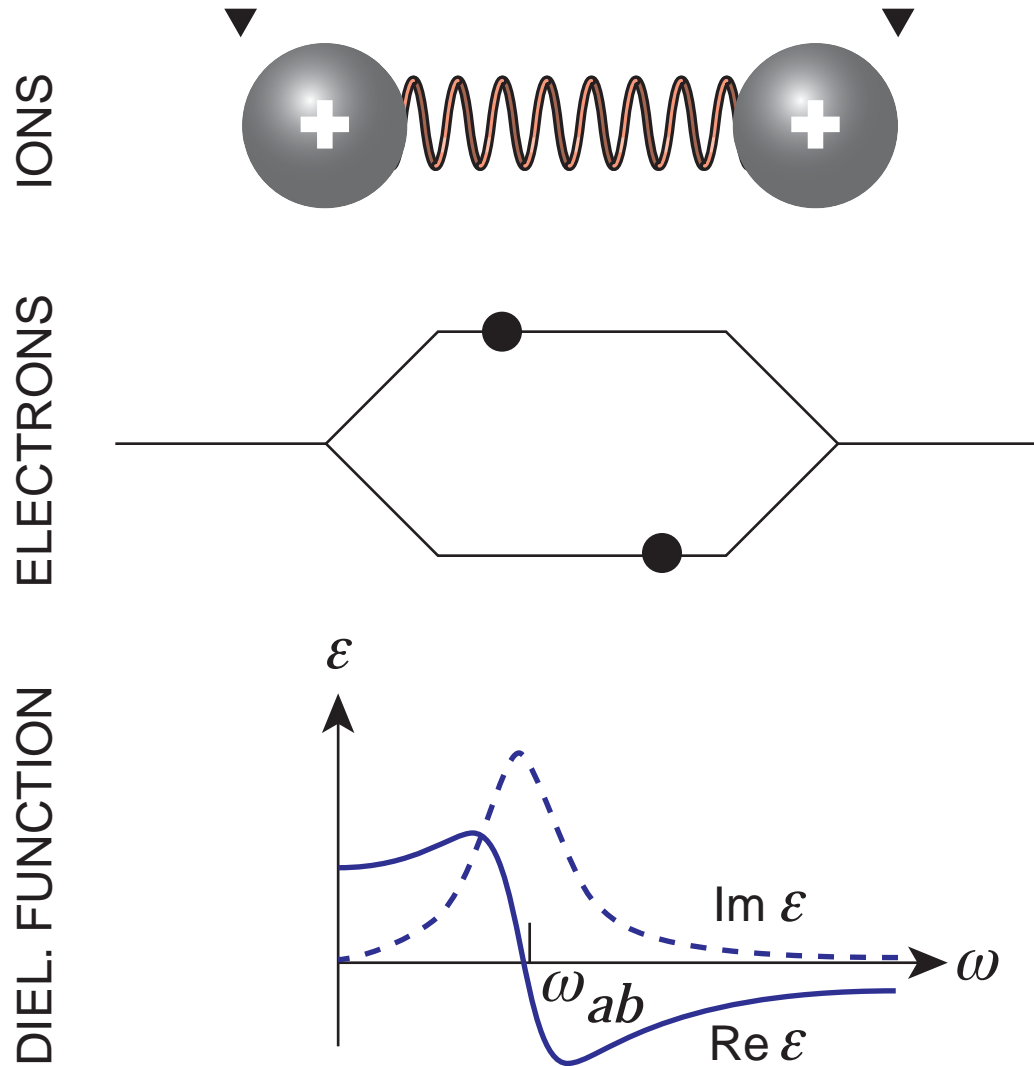
photon promotes electron...

# Displacive excitation



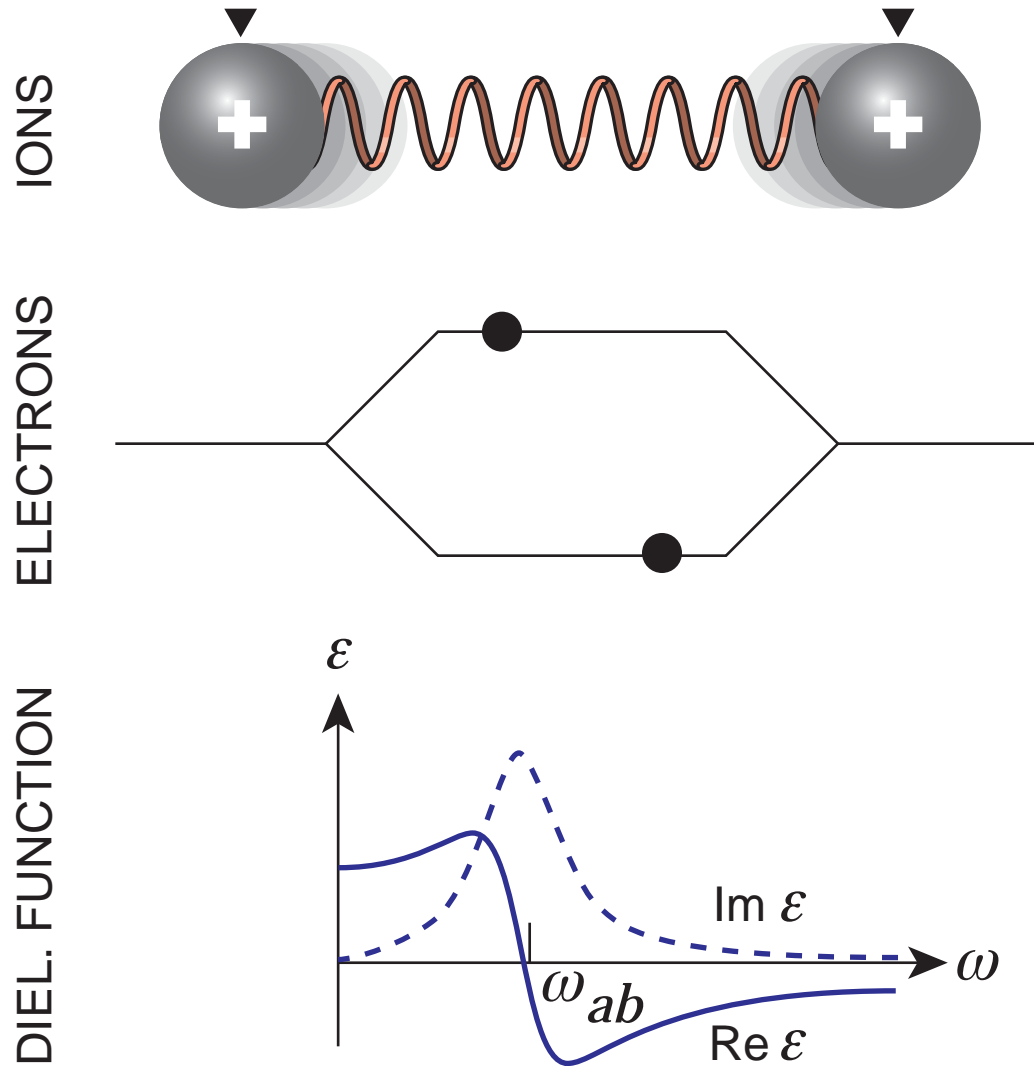
... weakening binding force...

# Displacive excitation



... establishing new equilibrium positions

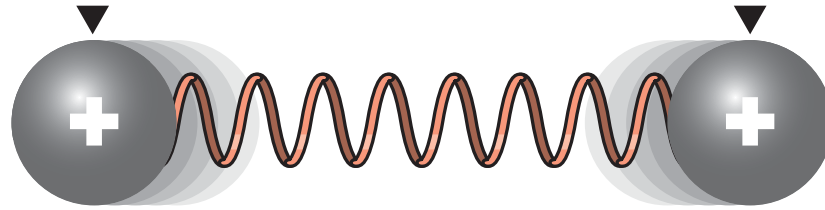
# Displacive excitation



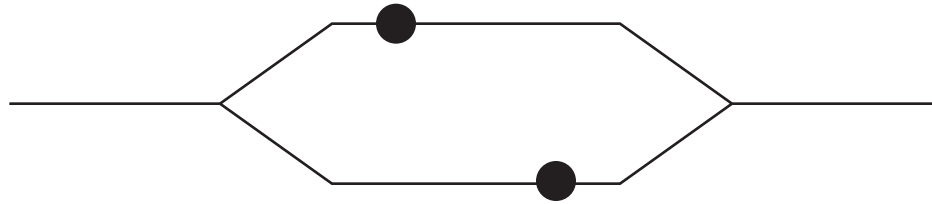
ions move to new equilibrium positions...

# Displacive excitation

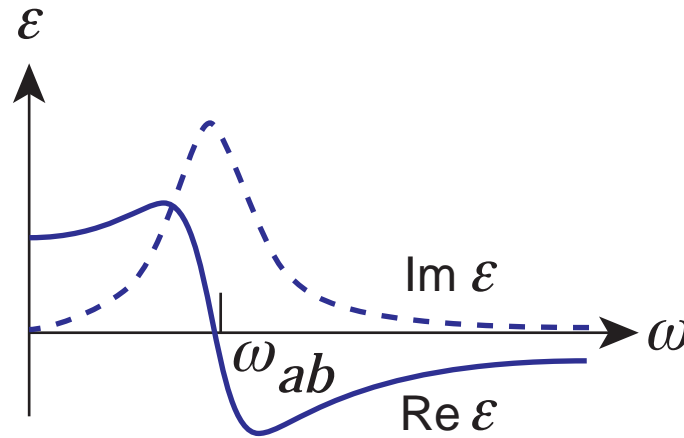
IONS



ELECTRONS



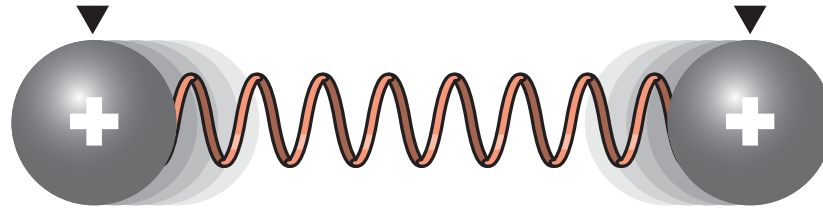
DIEL. FUNCTION



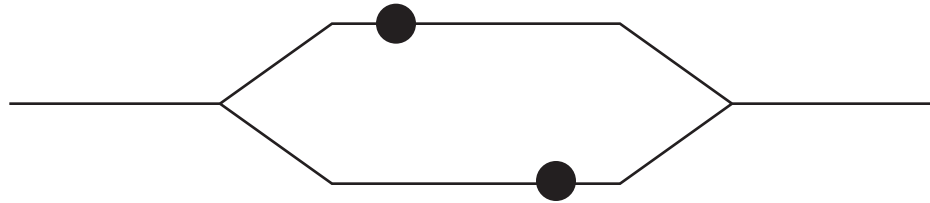
... diminishing splitting...

# Displacive excitation

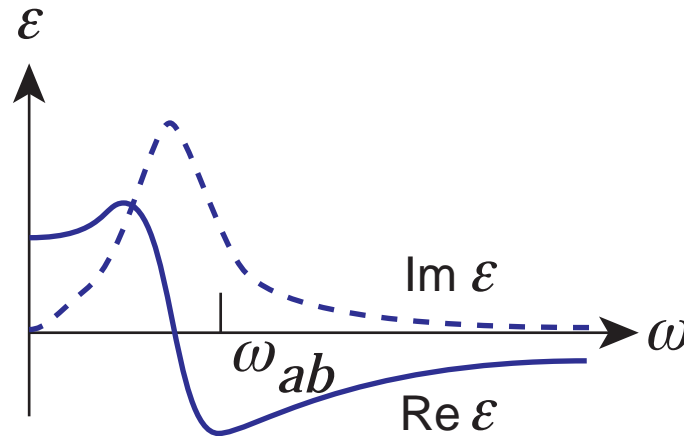
IONS



ELECTRONS

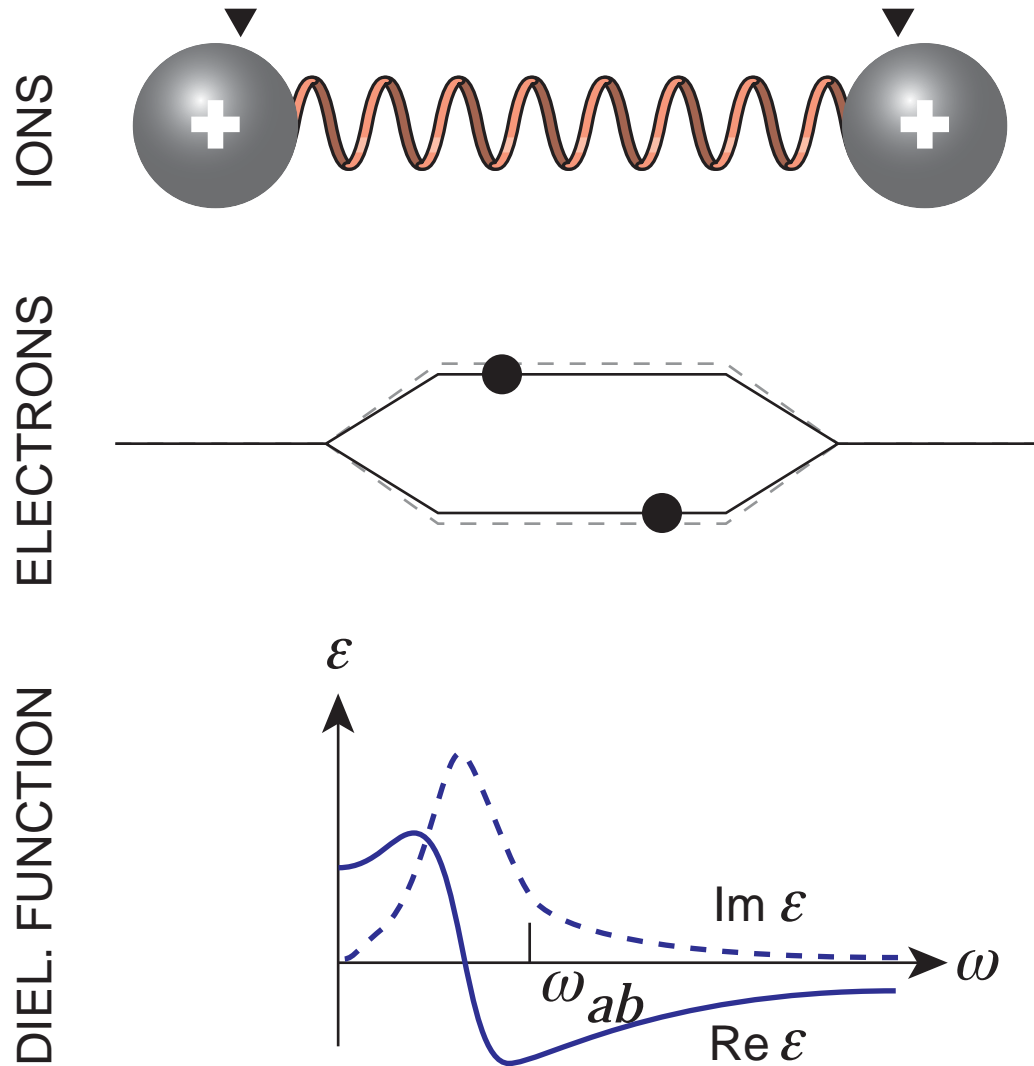


DIEL. FUNCTION



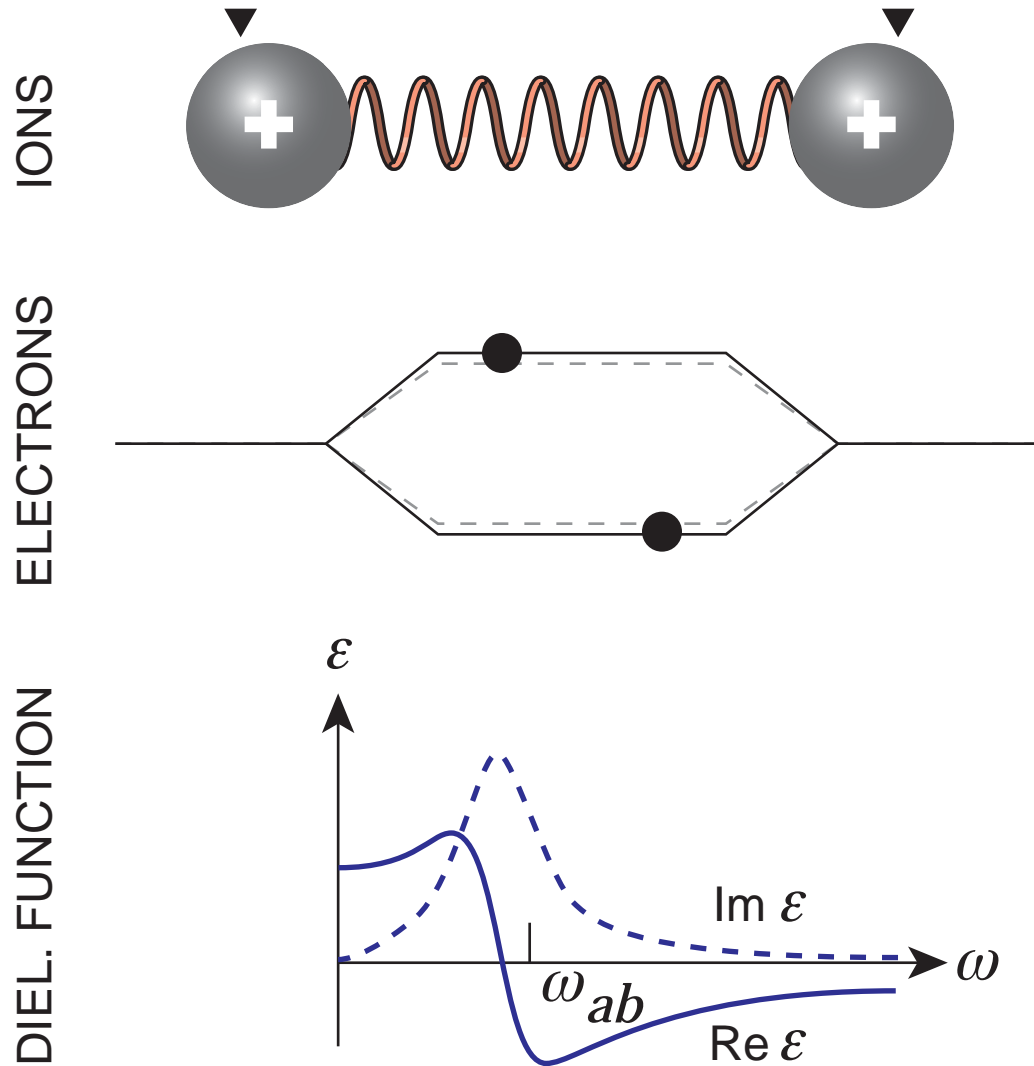
... and red-shifting the dielectric function

# Displacive excitation



ions overshoot equilibrium position...

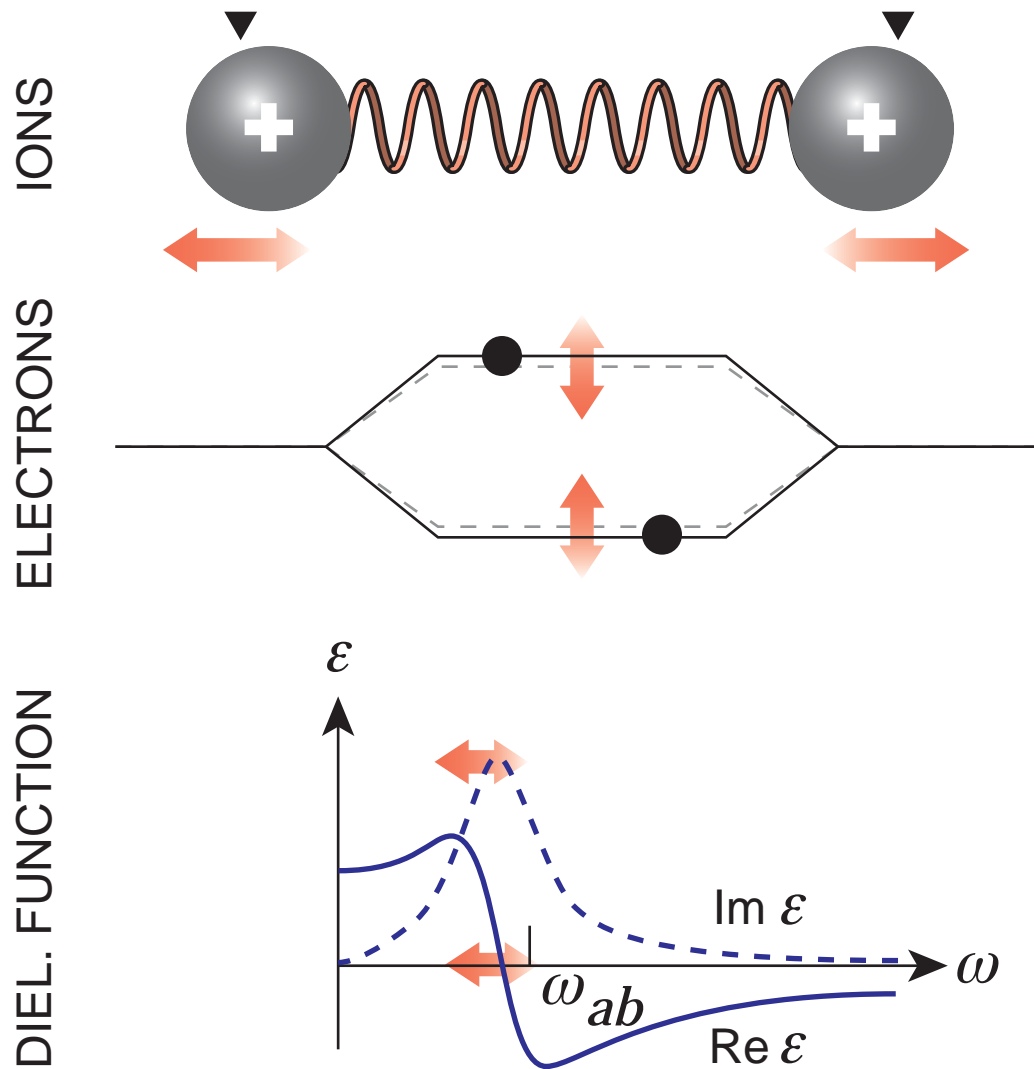
# Displacive excitation



... reversing travel and overshooting again



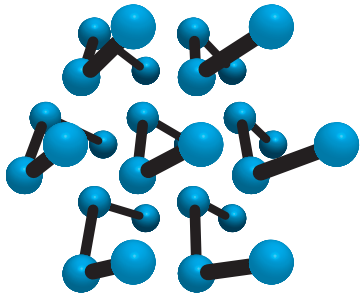
# Displacive excitation



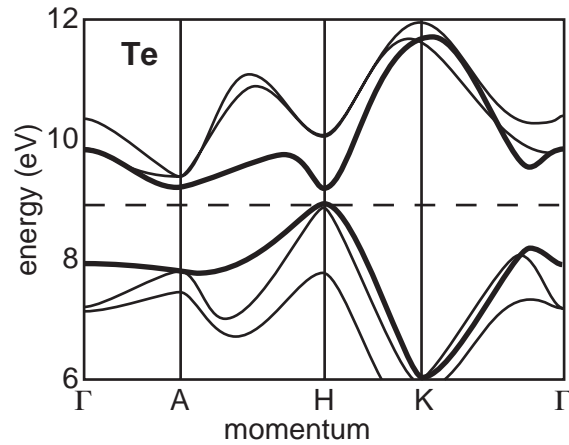
oscillation around "displaced" equilibrium position

# Displacive excitation

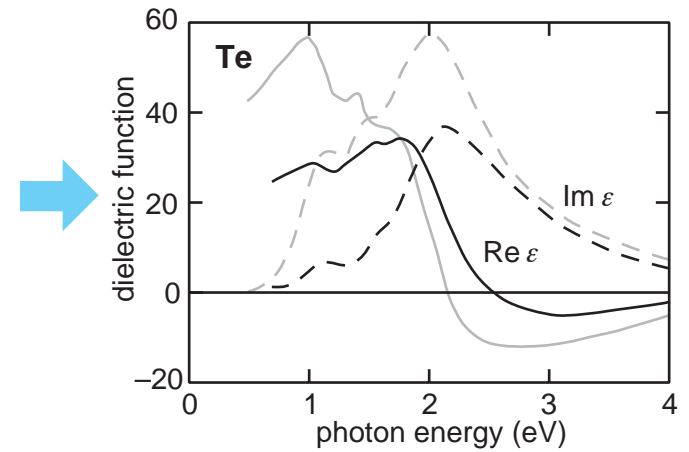
structure



band structure

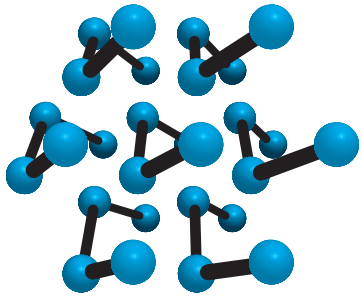


dielectric function

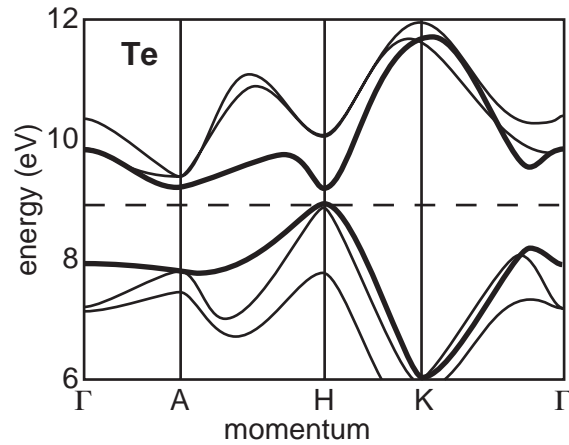


# Displacive excitation

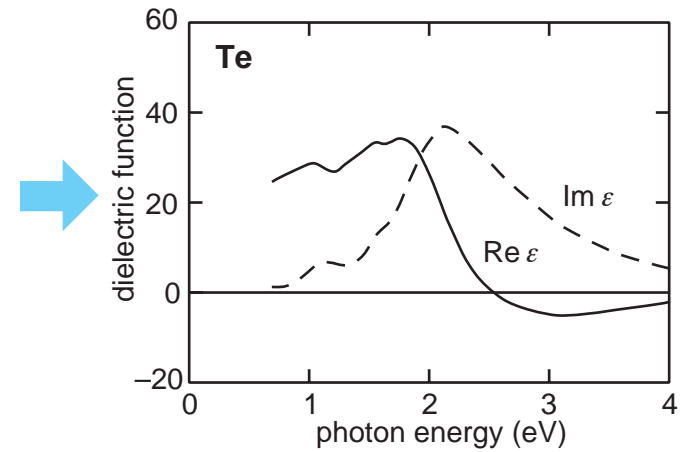
structure



band structure

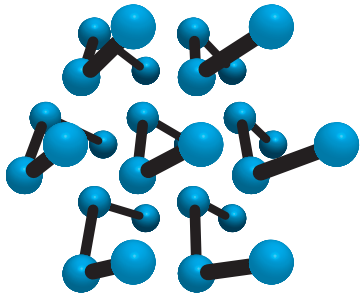


dielectric function

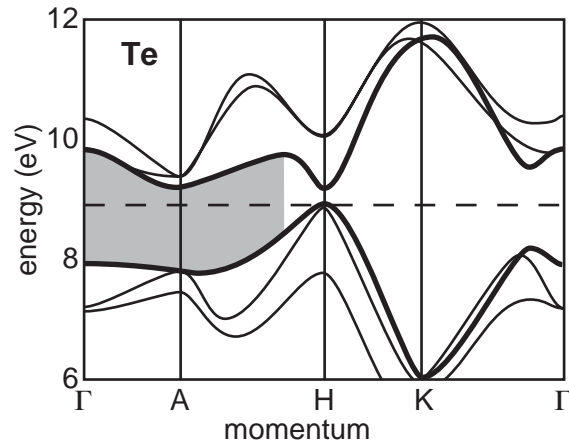


# Displacive excitation

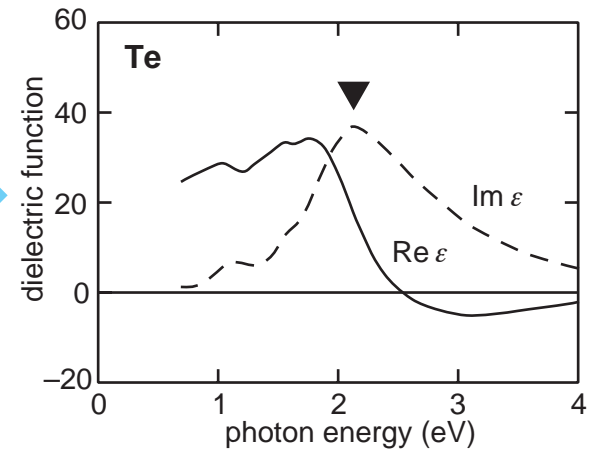
structure



band structure

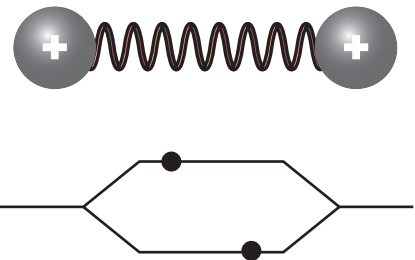


dielectric function

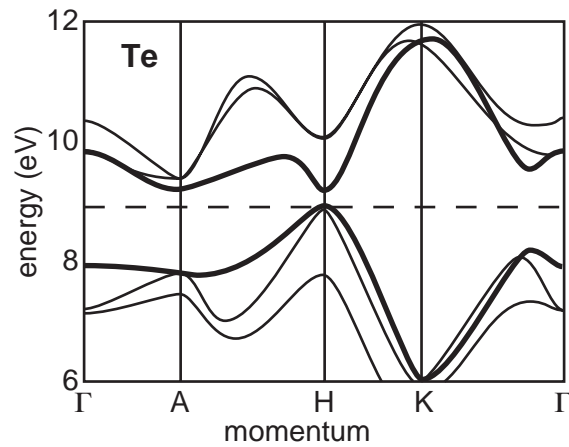


# Displacive excitation

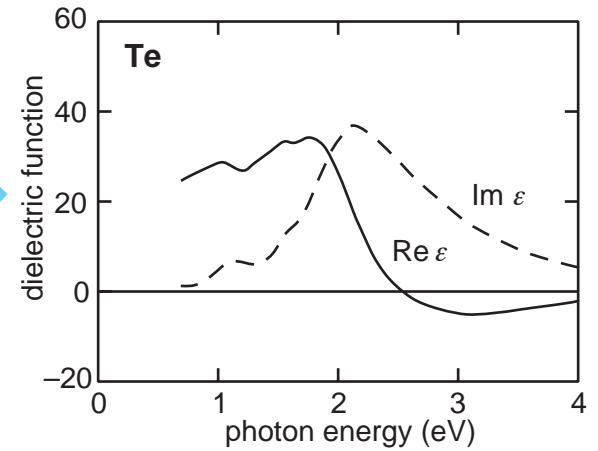
two-atom model



band structure

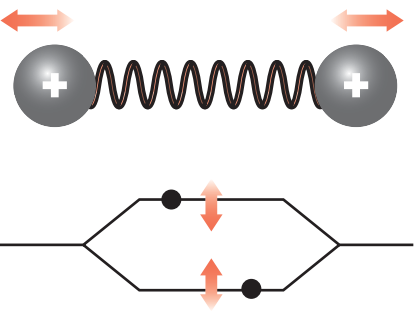


dielectric function

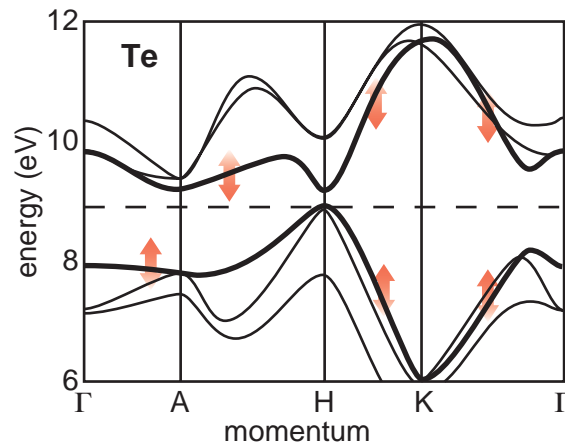


# Displacive excitation

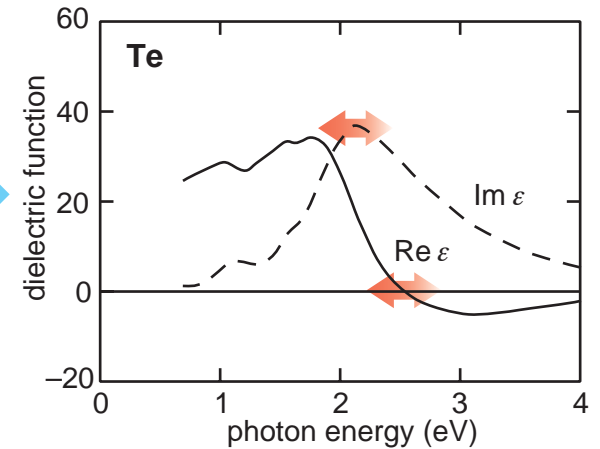
two-atom model



band structure



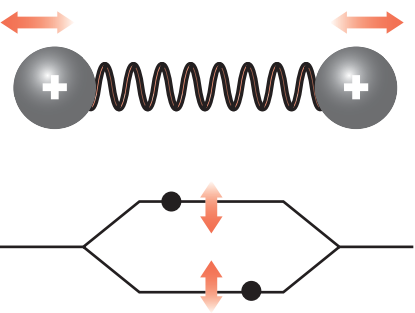
dielectric function



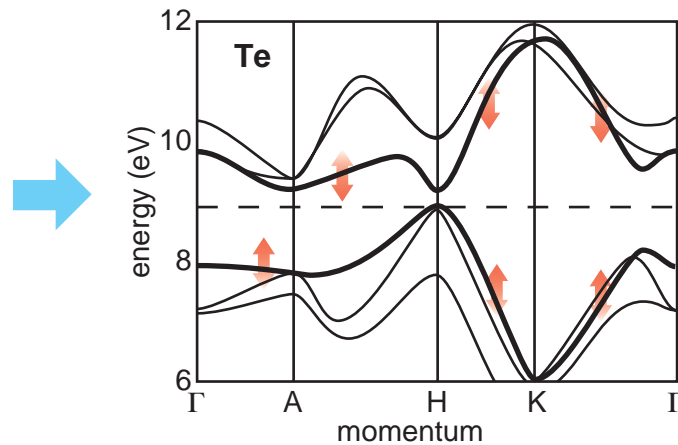
red-shift followed by oscillation

# Displacive excitation

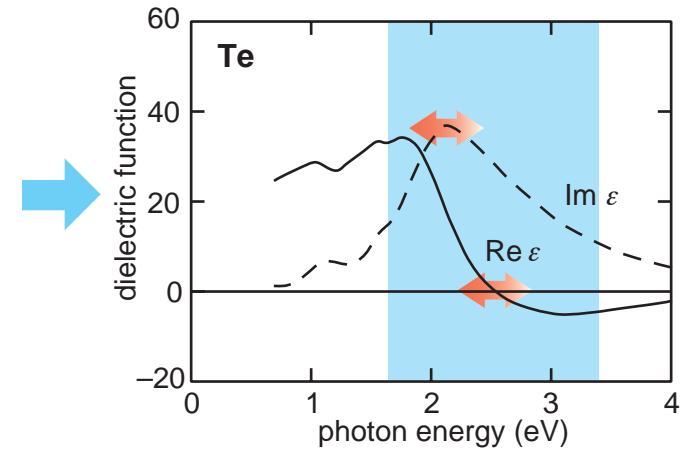
two-atom model



band structure

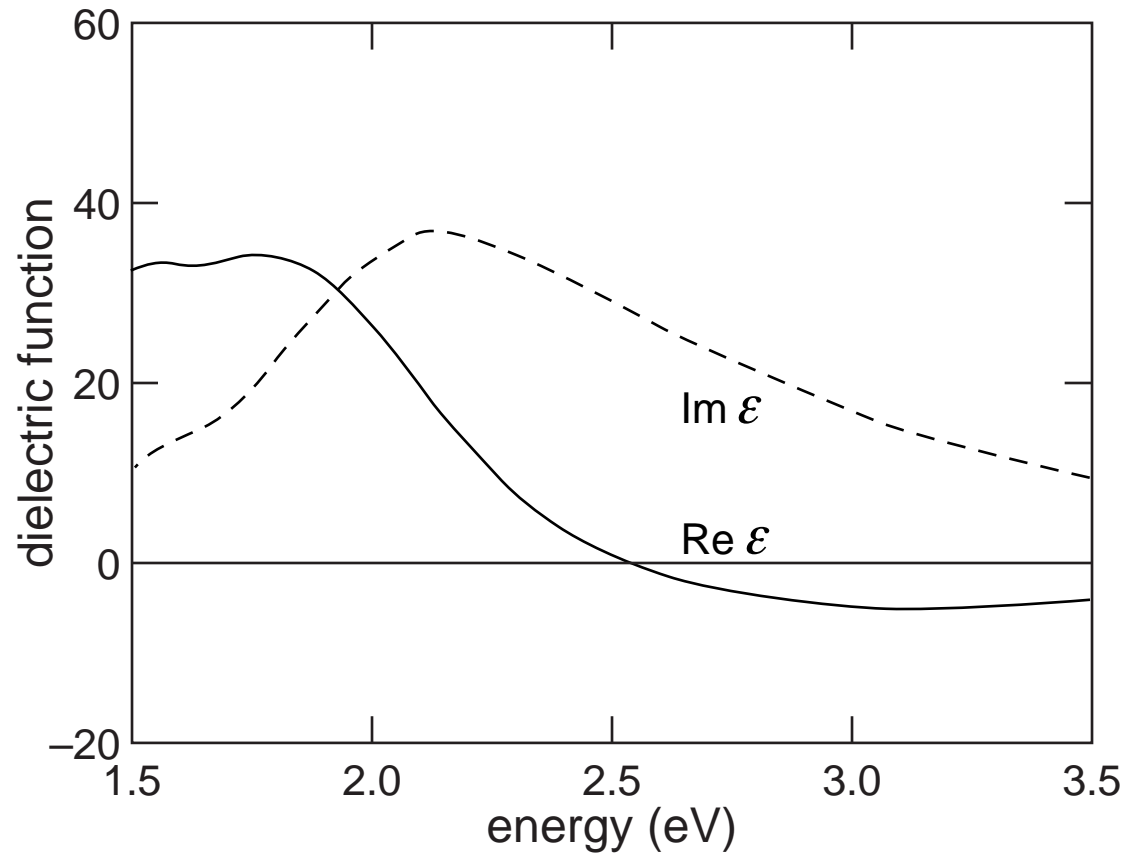


dielectric function



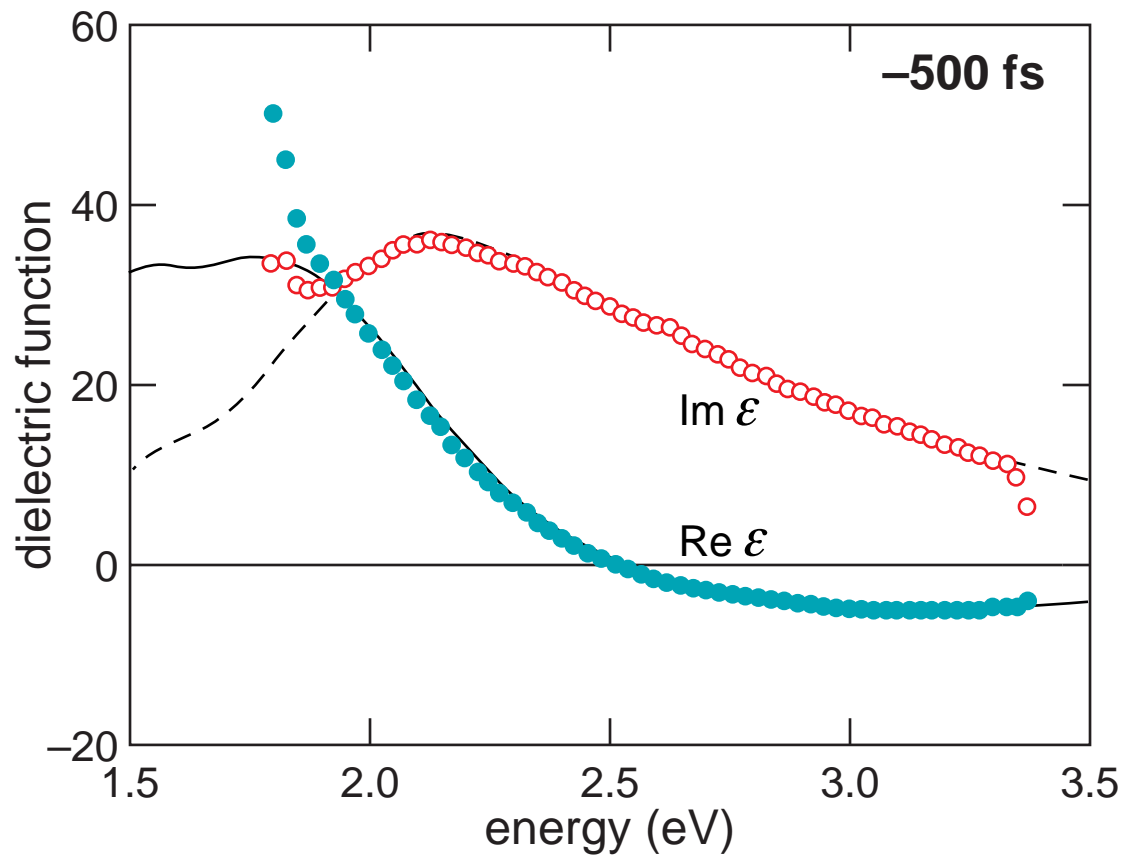
red-shift followed by oscillation

# Results

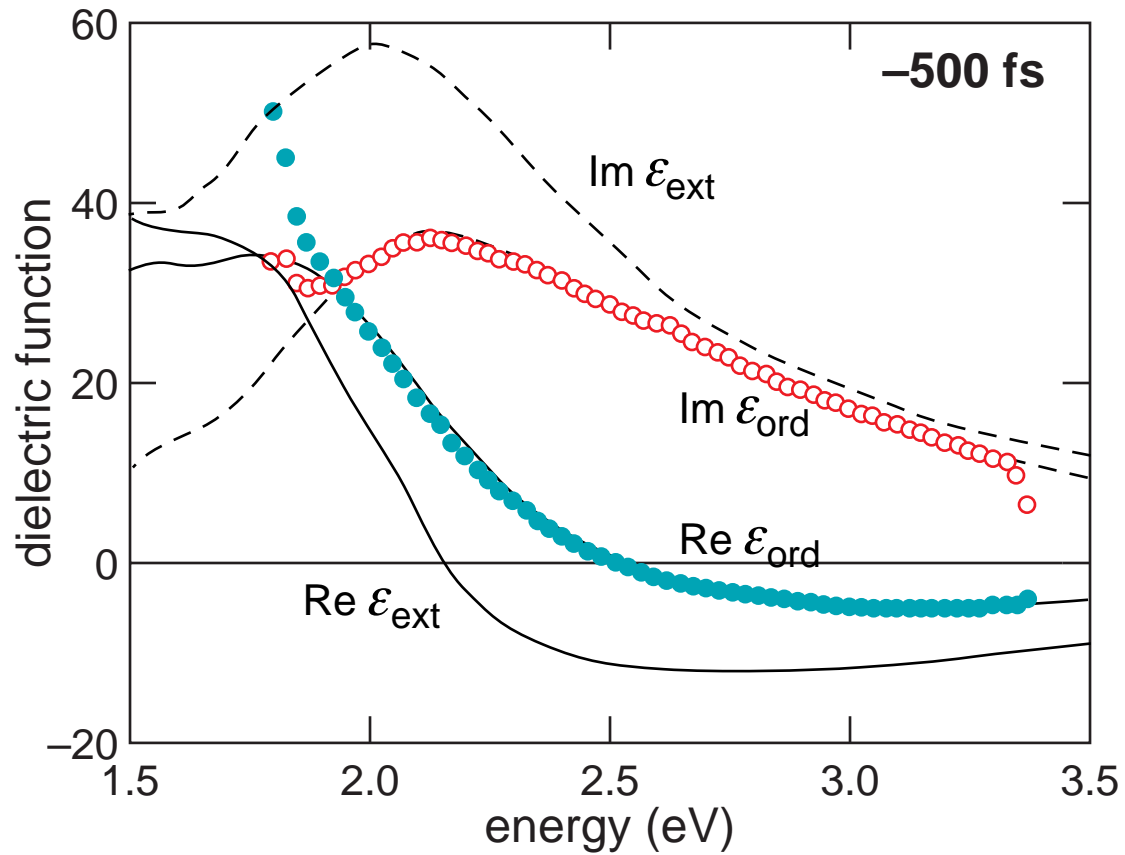




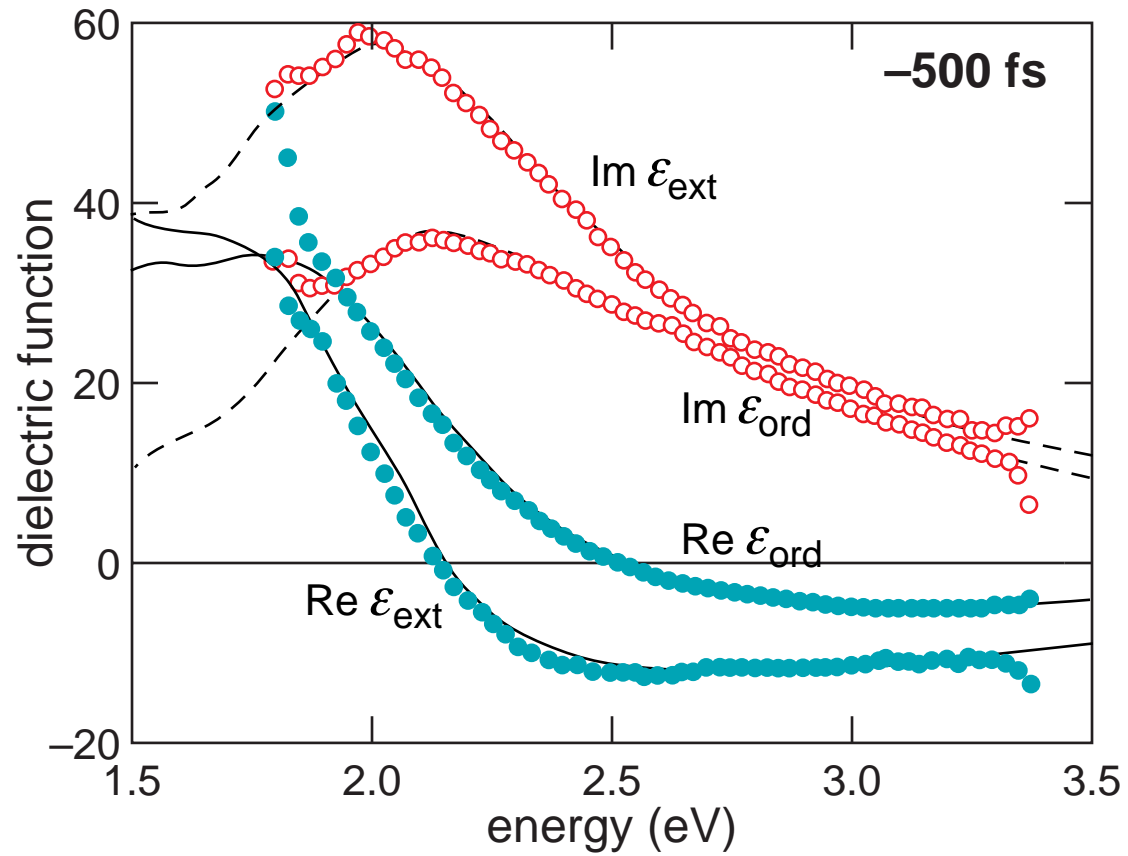
# Results



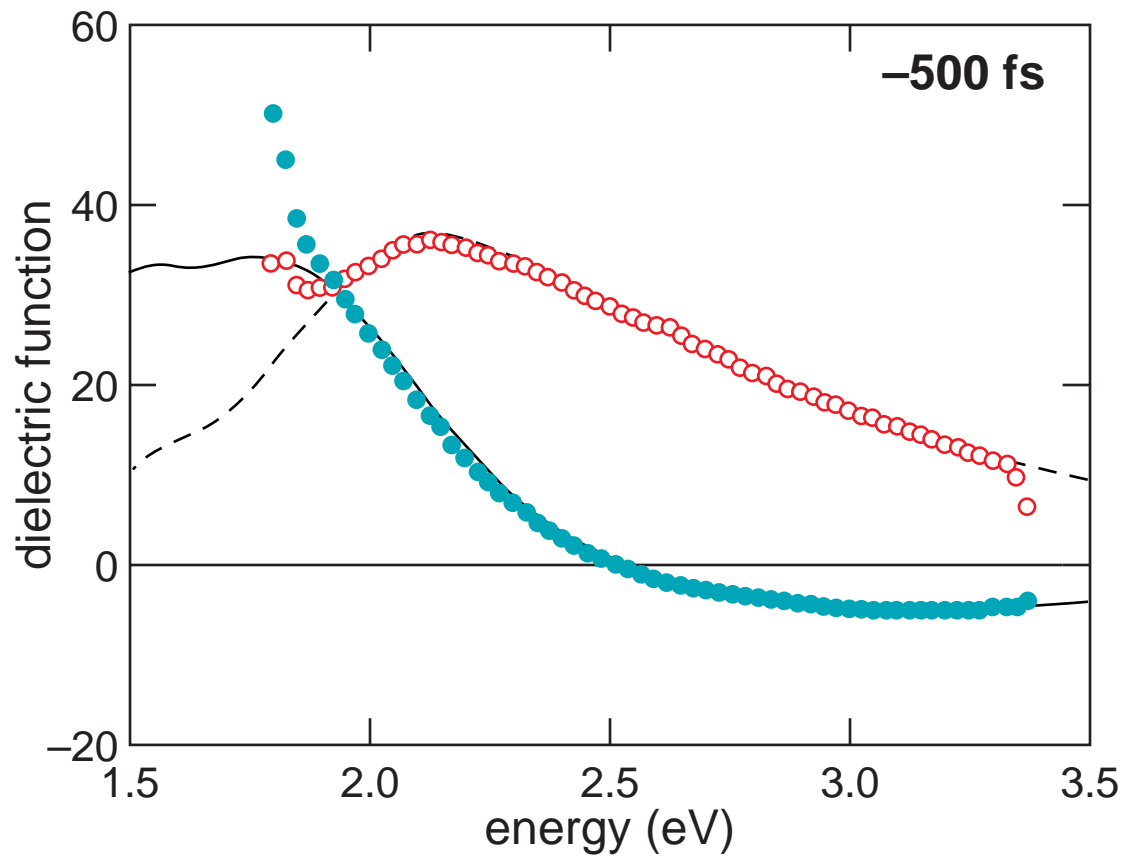
# Results



# Results

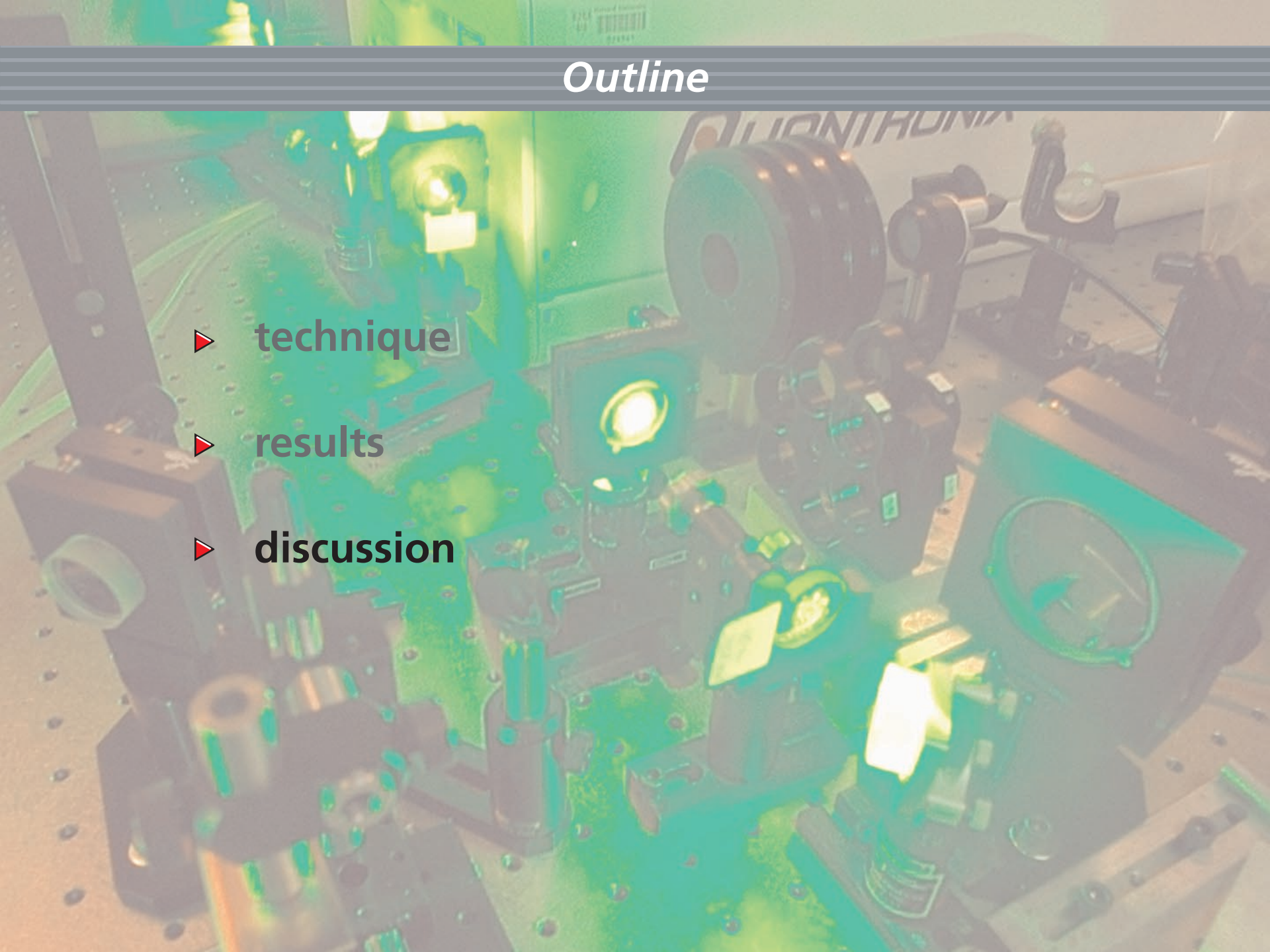


# Results

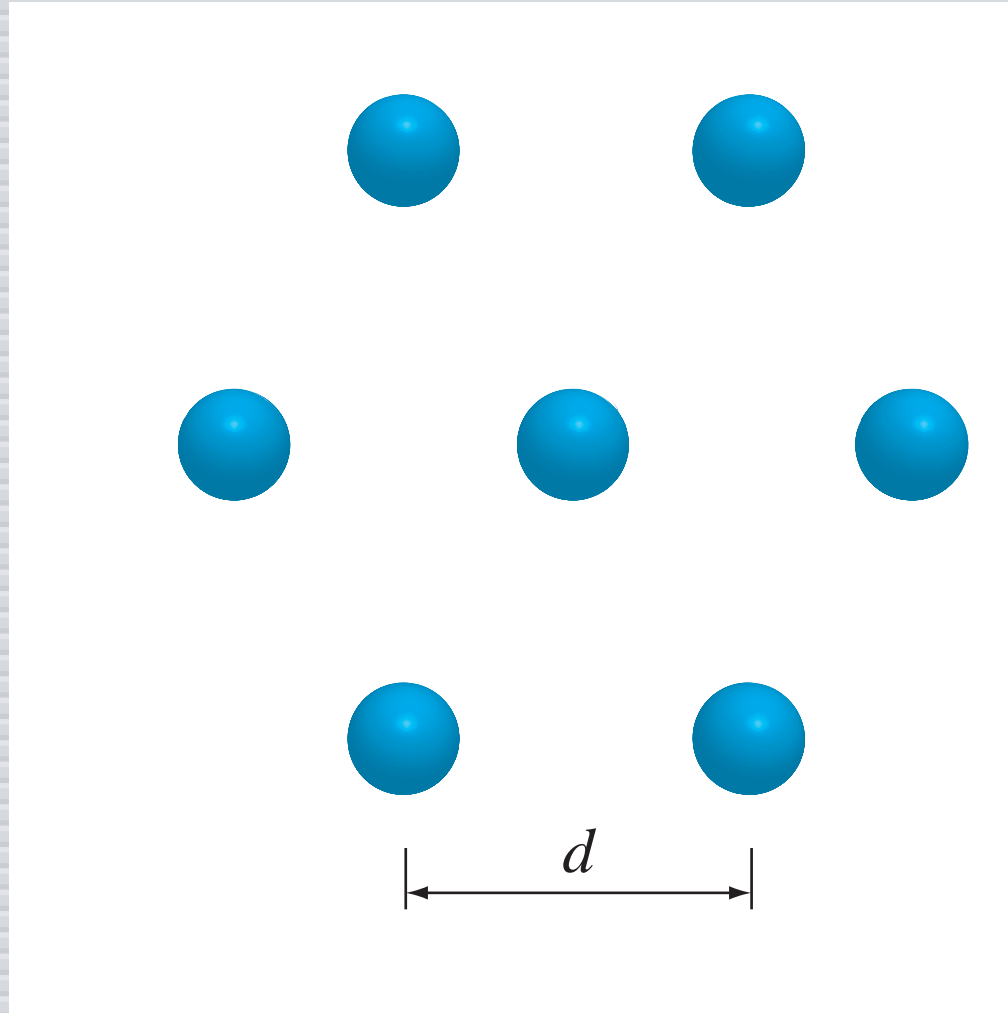


# Outline

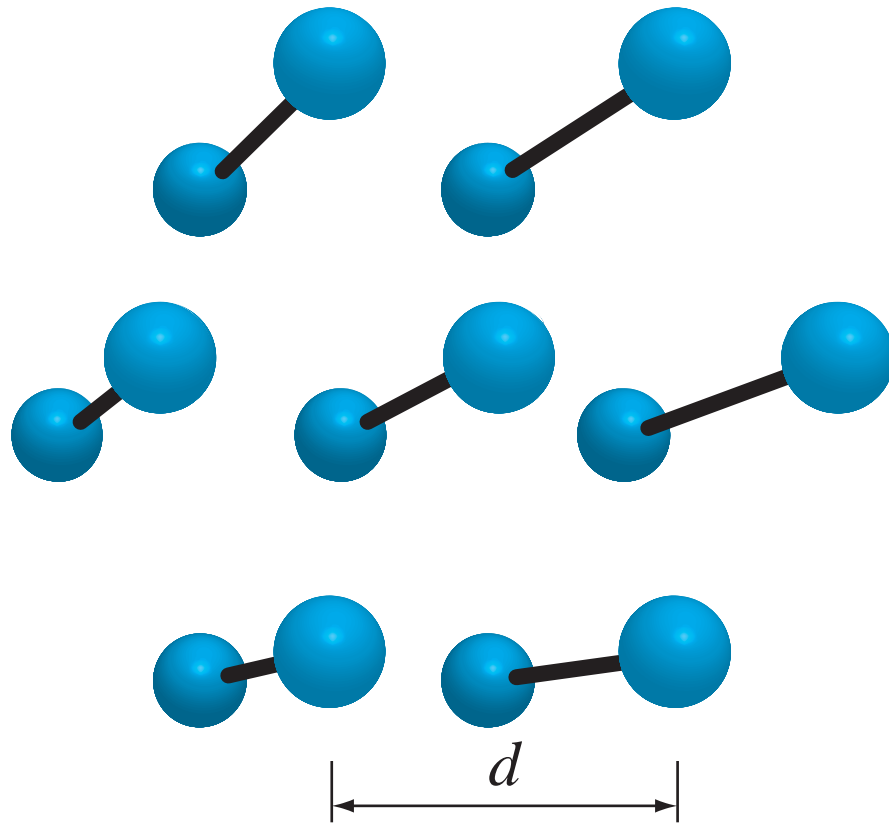
- ▶ **technique**
- ▶ **results**
- ▶ **discussion**



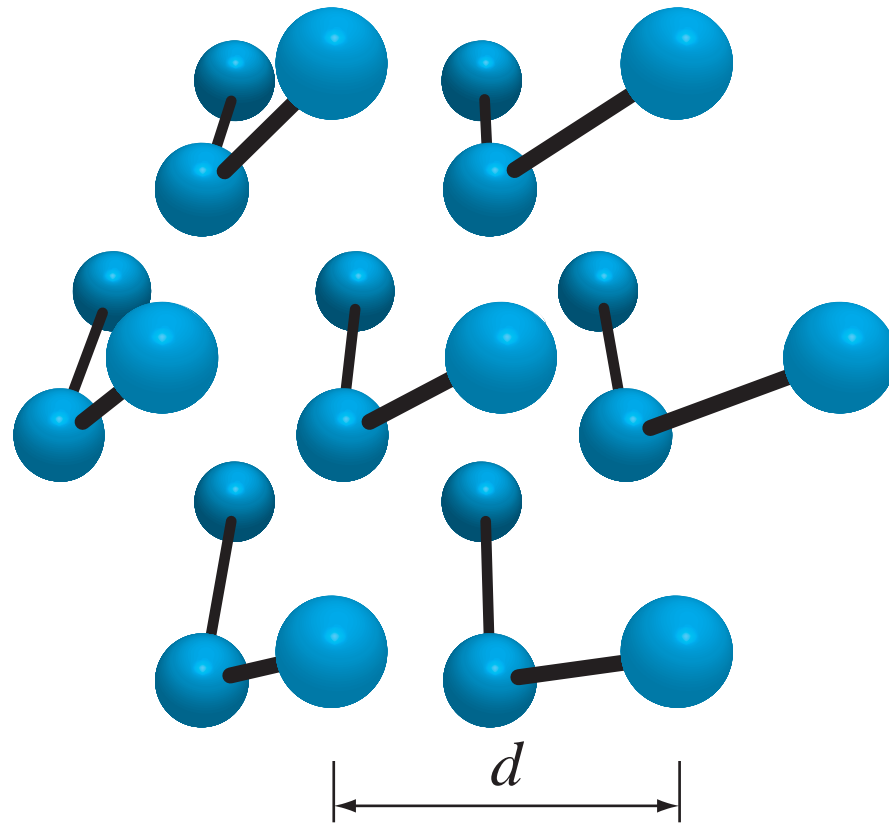
# Tellurium structure



# Tellurium structure

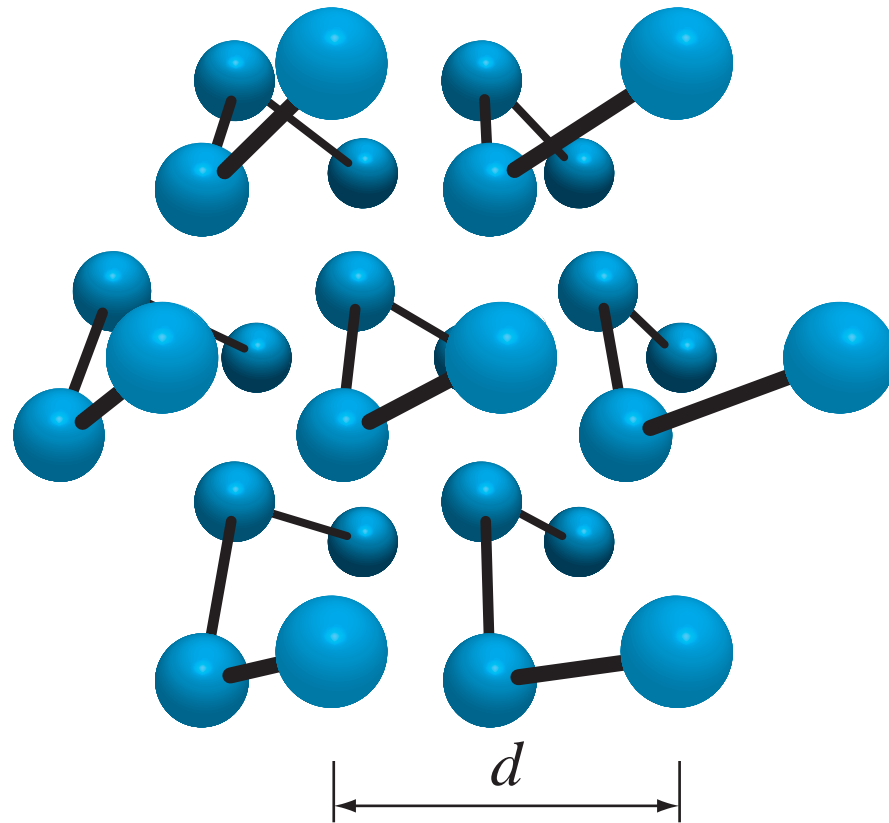


# Tellurium structure

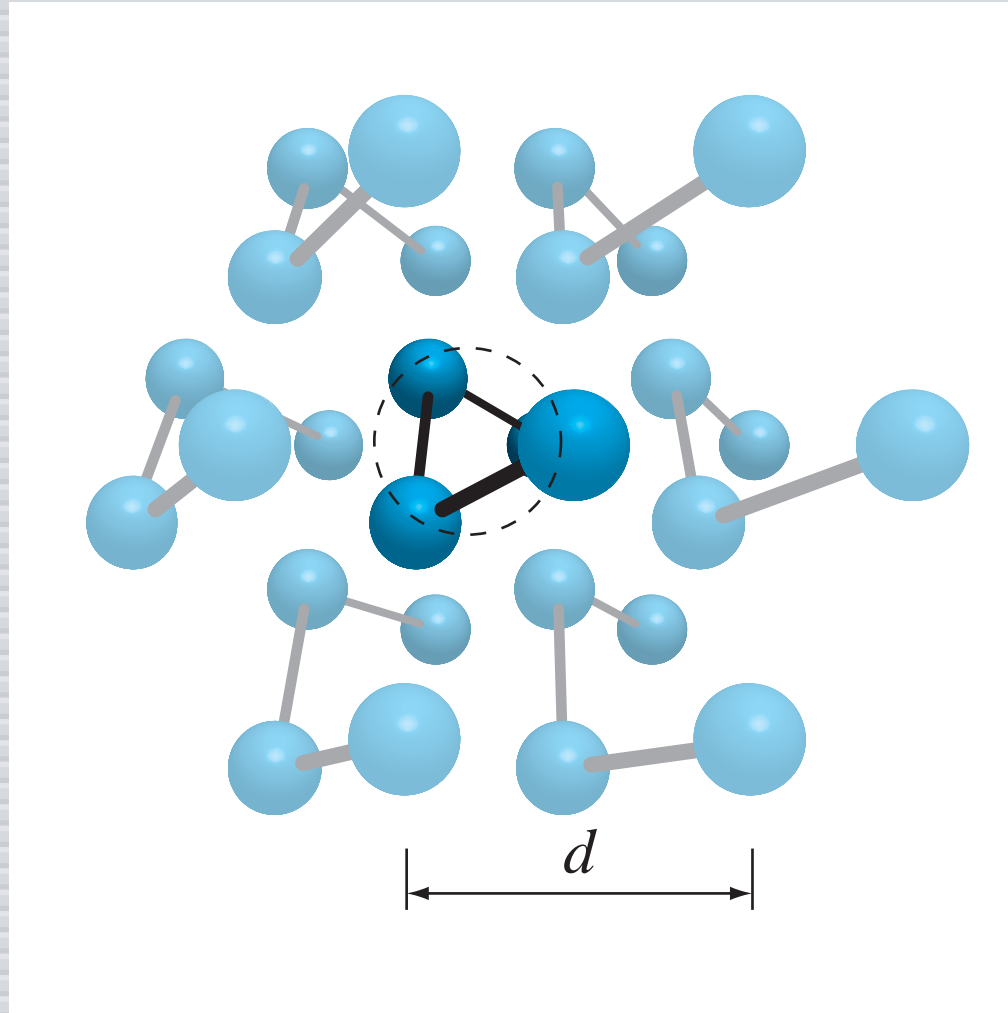




# Tellurium structure

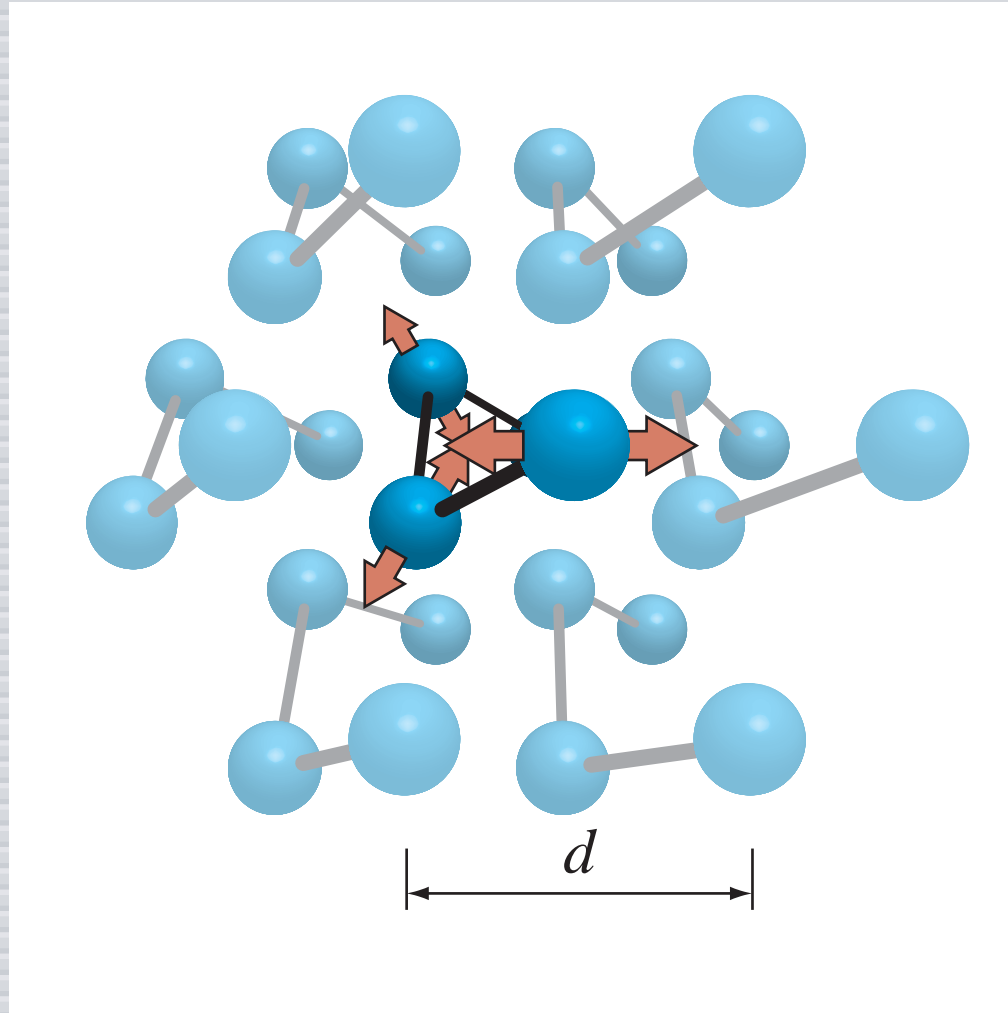


# Tellurium structure



helical radius  $x = 0.26d$

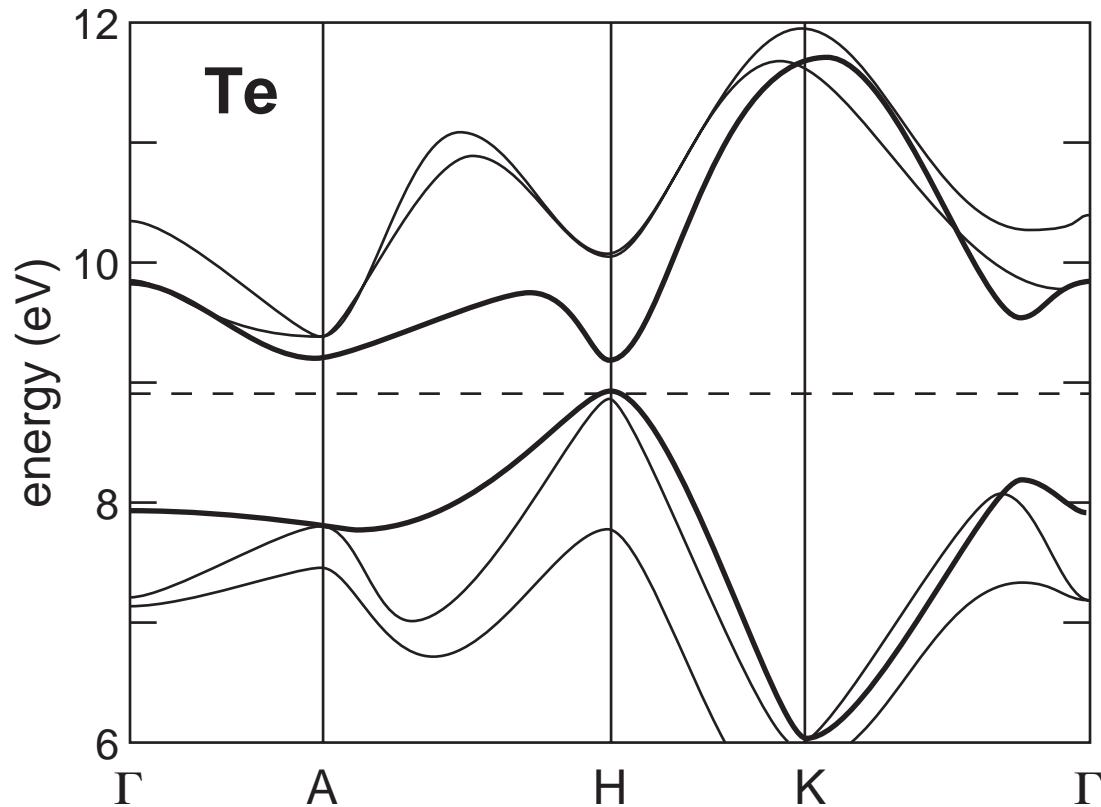
# Tellurium structure



**$A_1$  mode modulates  $x$**

# Tellurium band structure

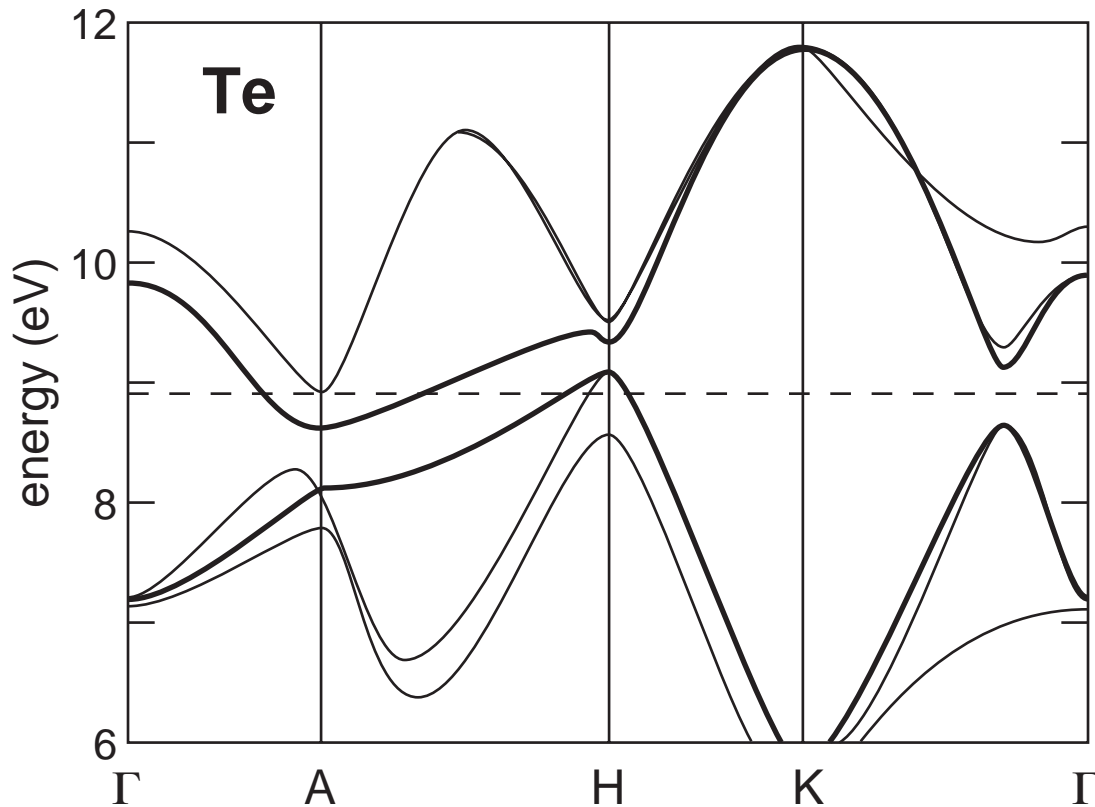
band structure very sensitive to  $x$



P. Tangney (Princeton) and S. Fahey (Cork), *private communication*

# Tellurium band structure

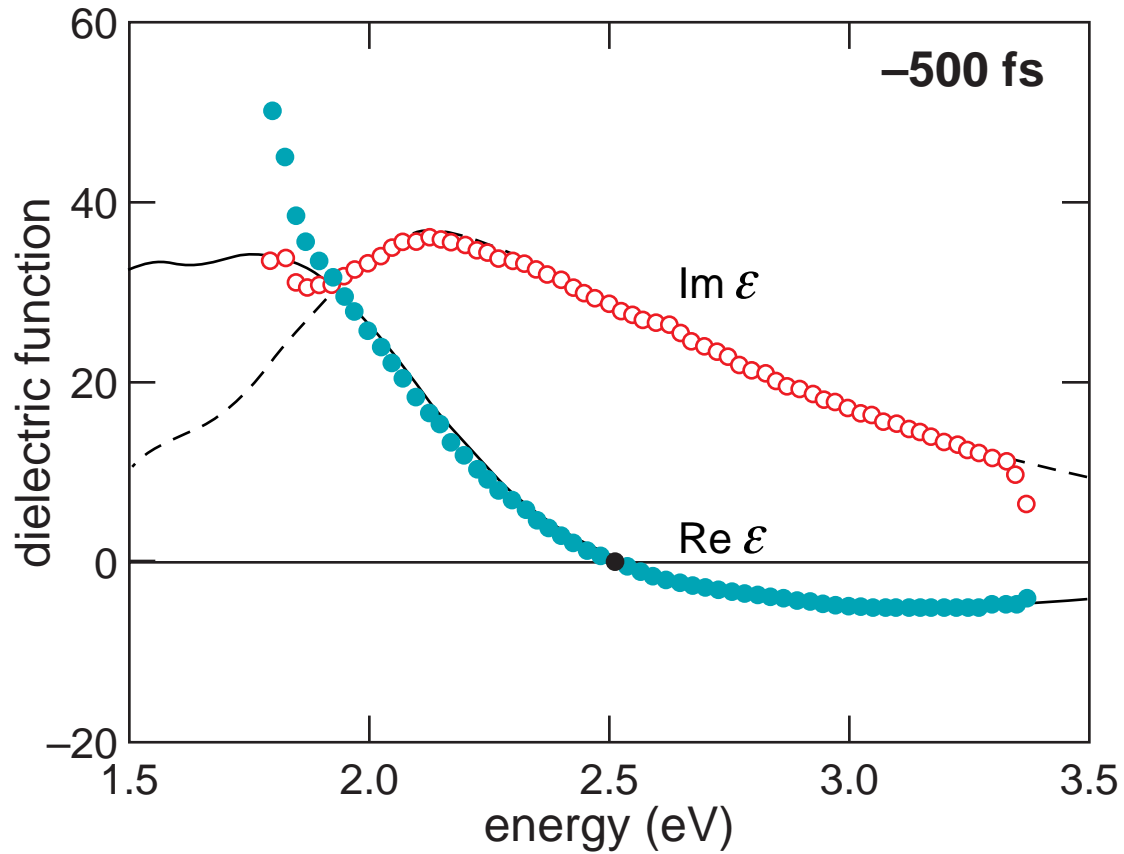
bands cross when  $x$  changes by 6%



P. Tangney (Princeton) and S. Fahey (Cork), *private communication*

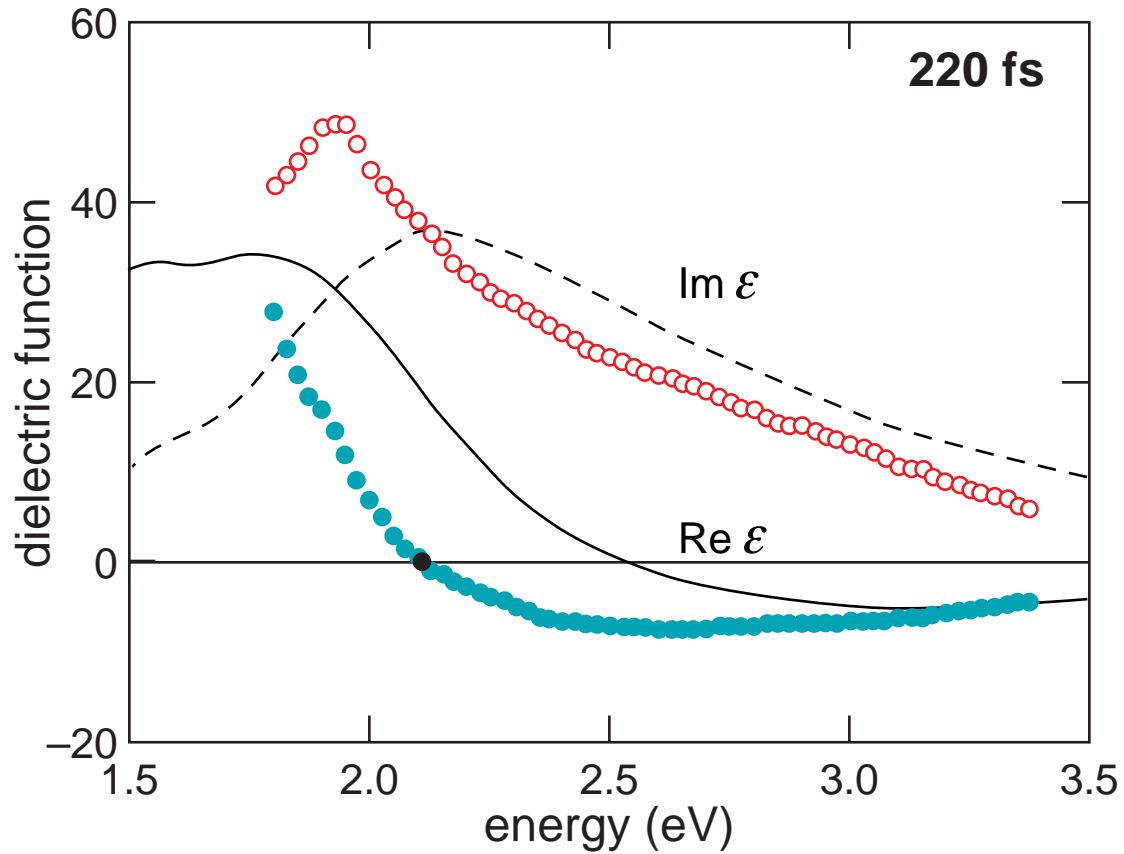
# Discussion

## track zero-crossing of real part



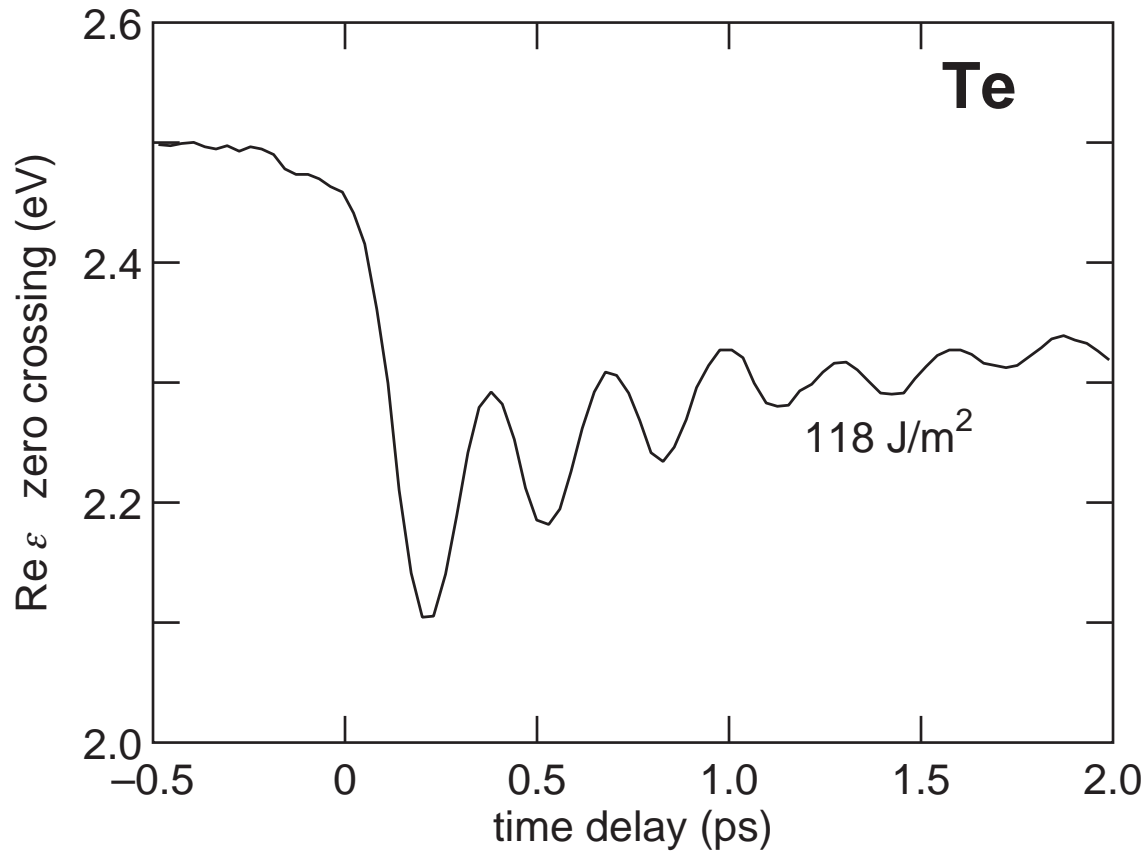
# Discussion

## track zero-crossing of real part



# Discussion

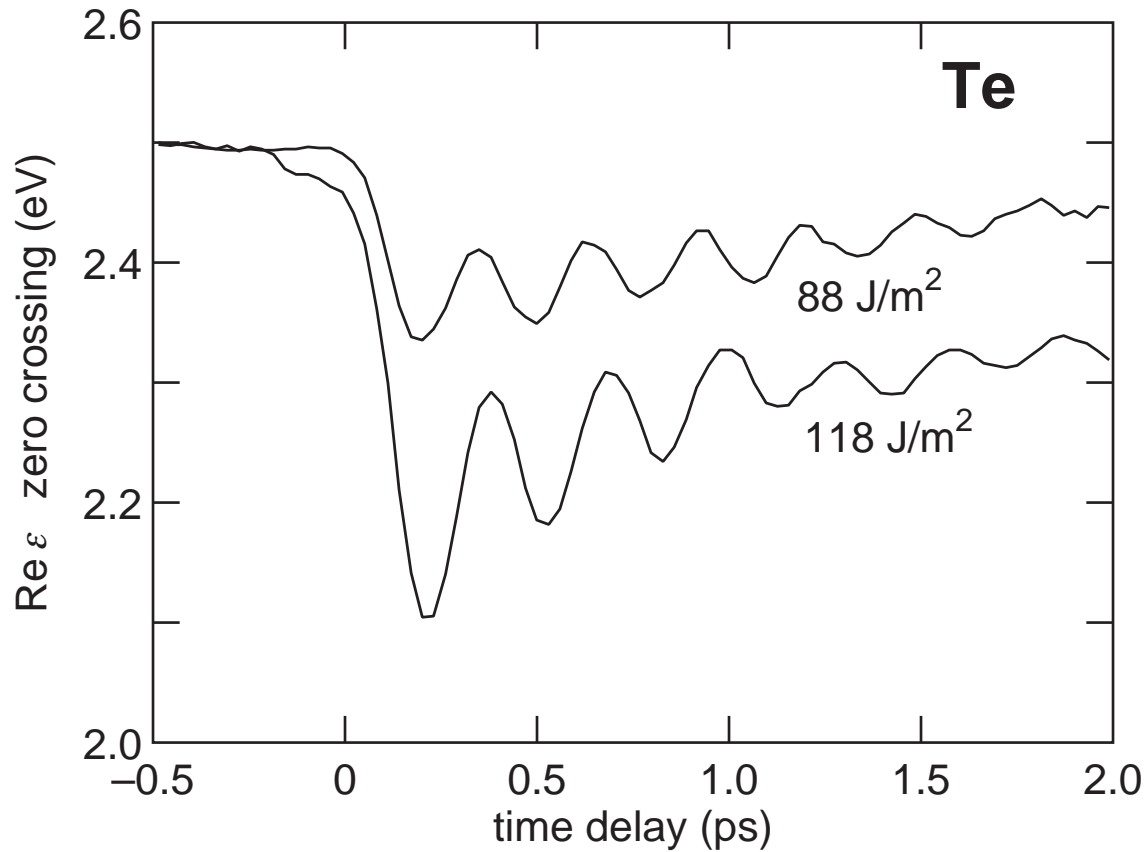
## track zero-crossing of real part





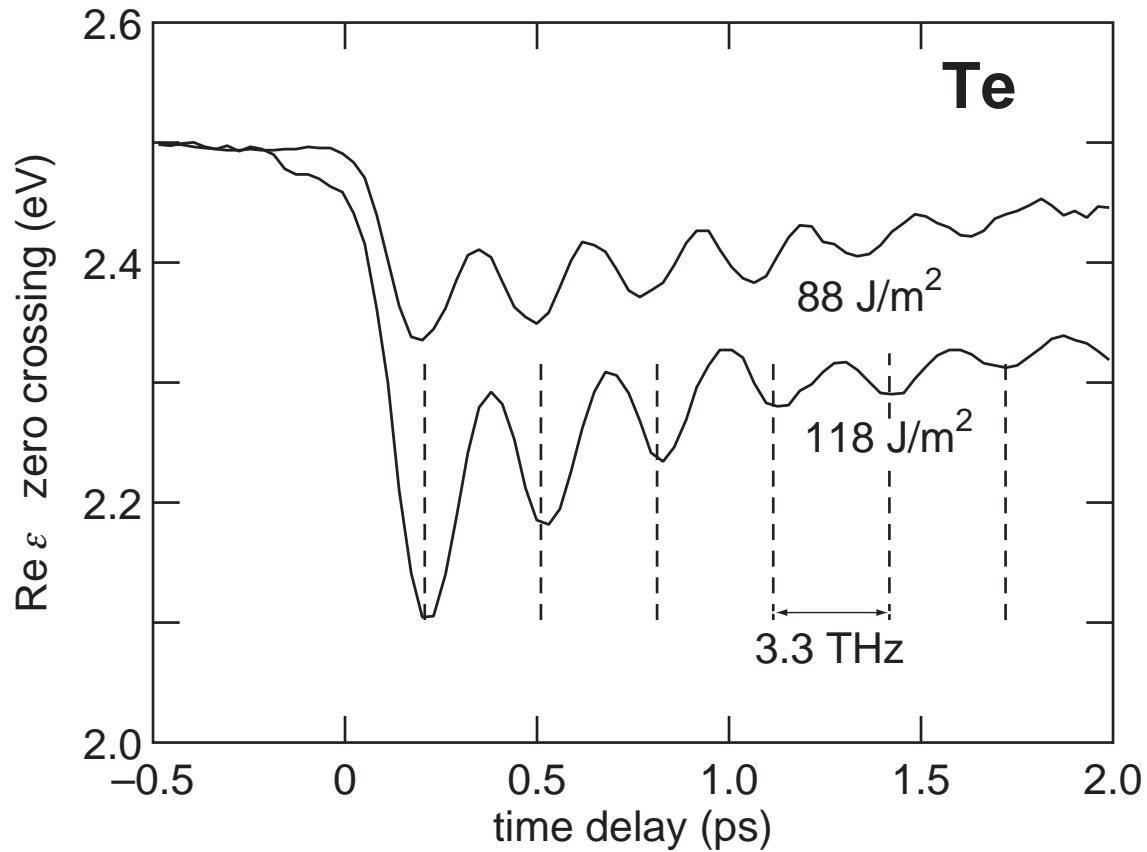
## Discussion

higher fluence: larger amplitude oscillations



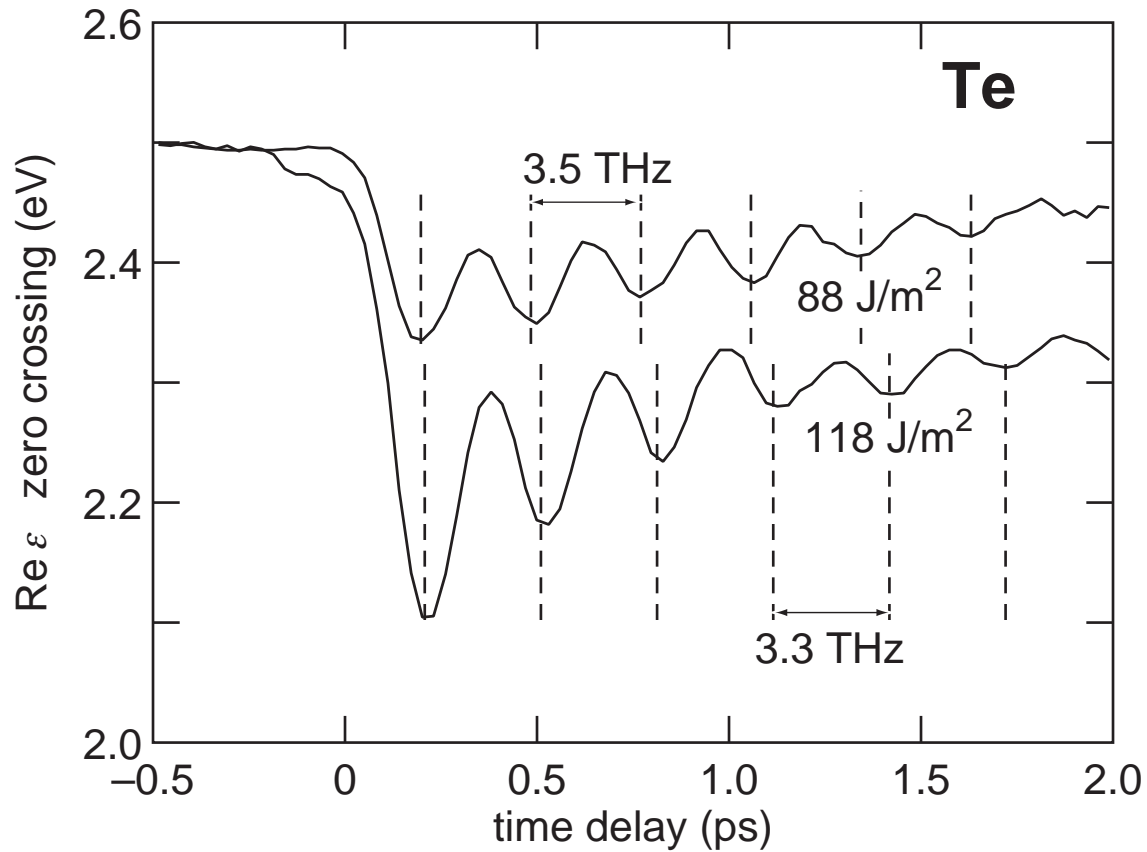
## Discussion

frequency less than 3.6 THz equilibrium value



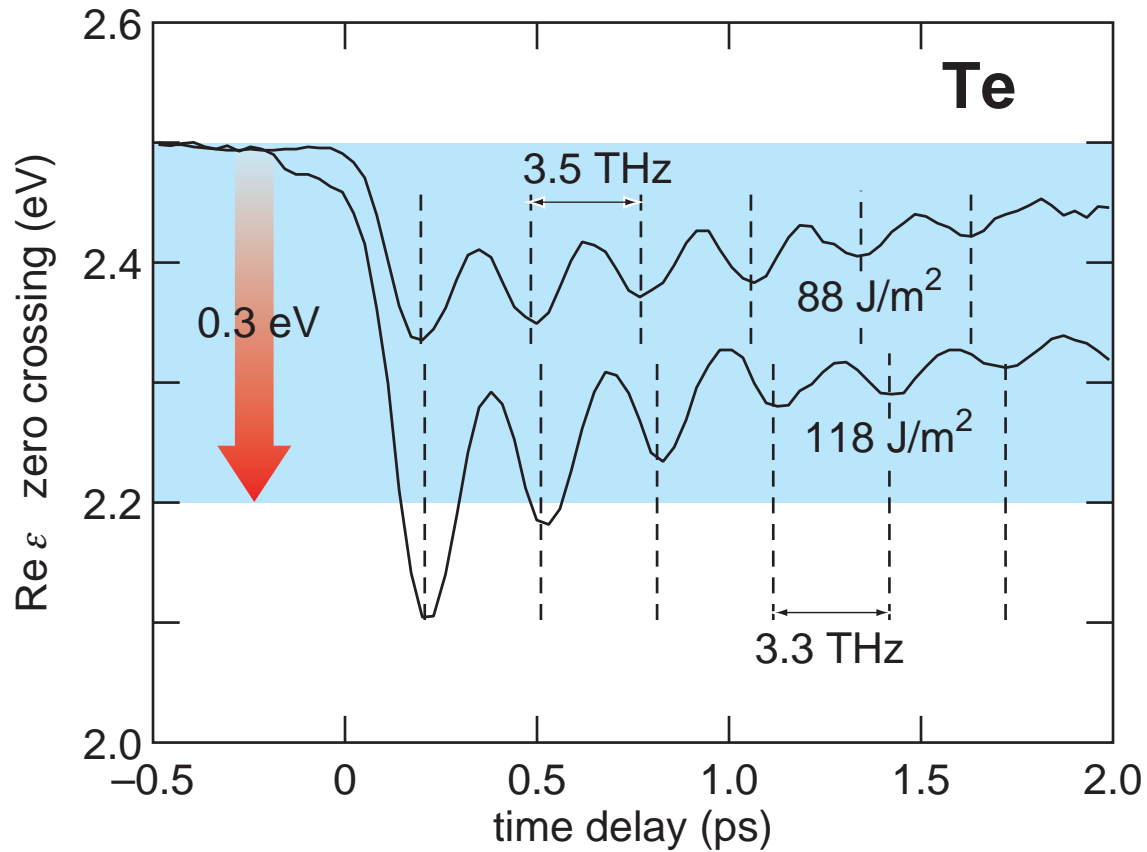
# Discussion

## softening of phonon mode



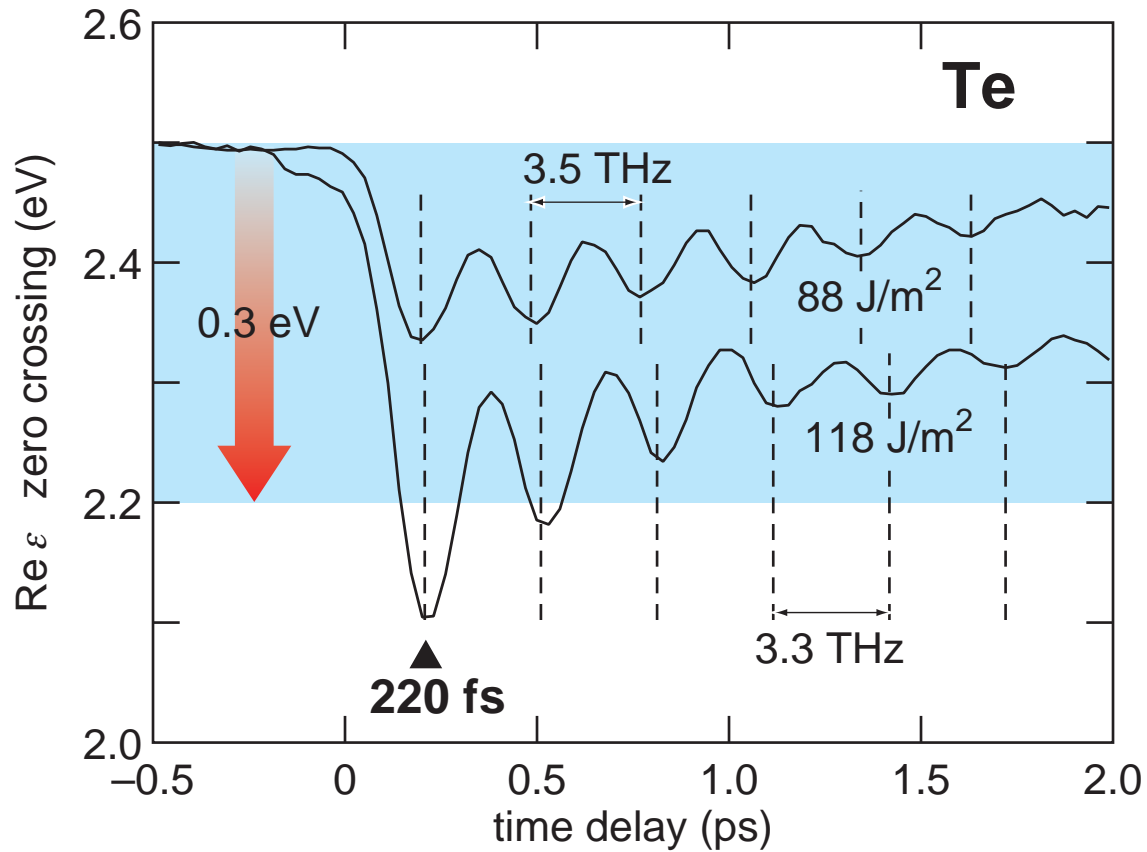
# Discussion

compare shift to band gap



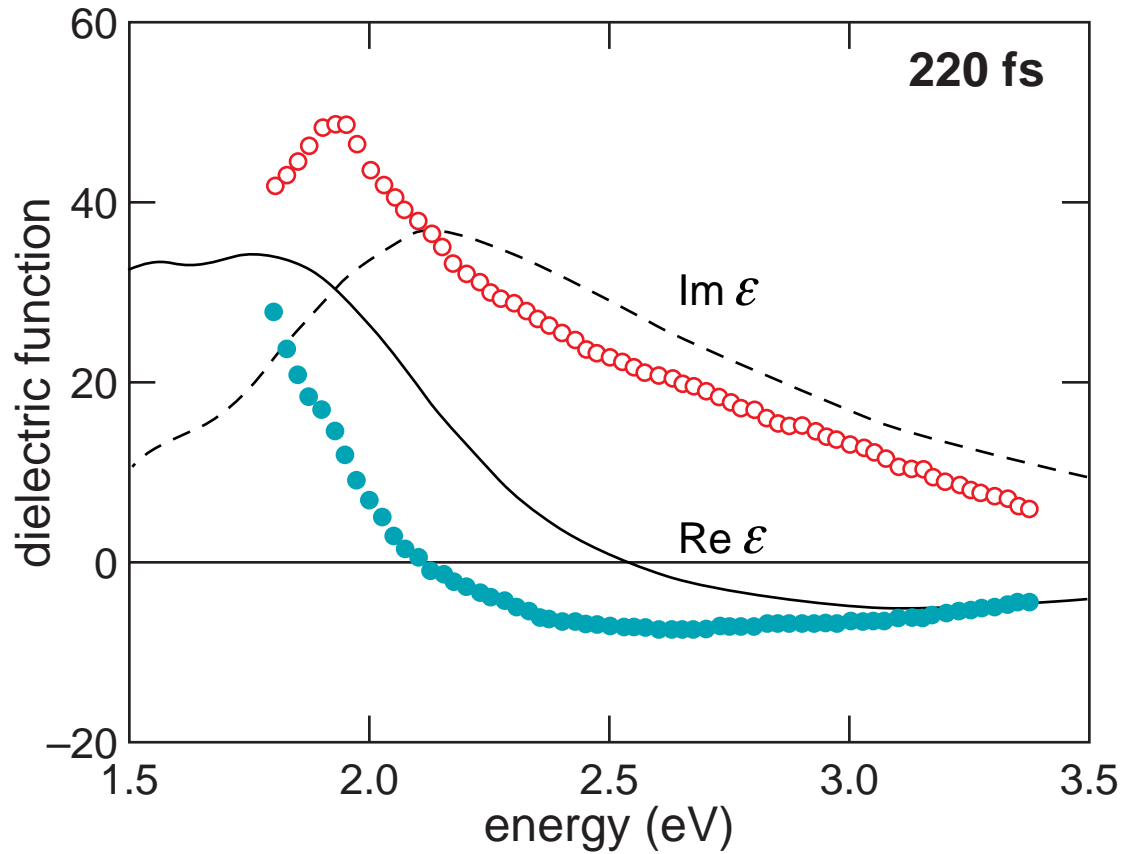
# Discussion

shift exceeds band gap at 220 fs...

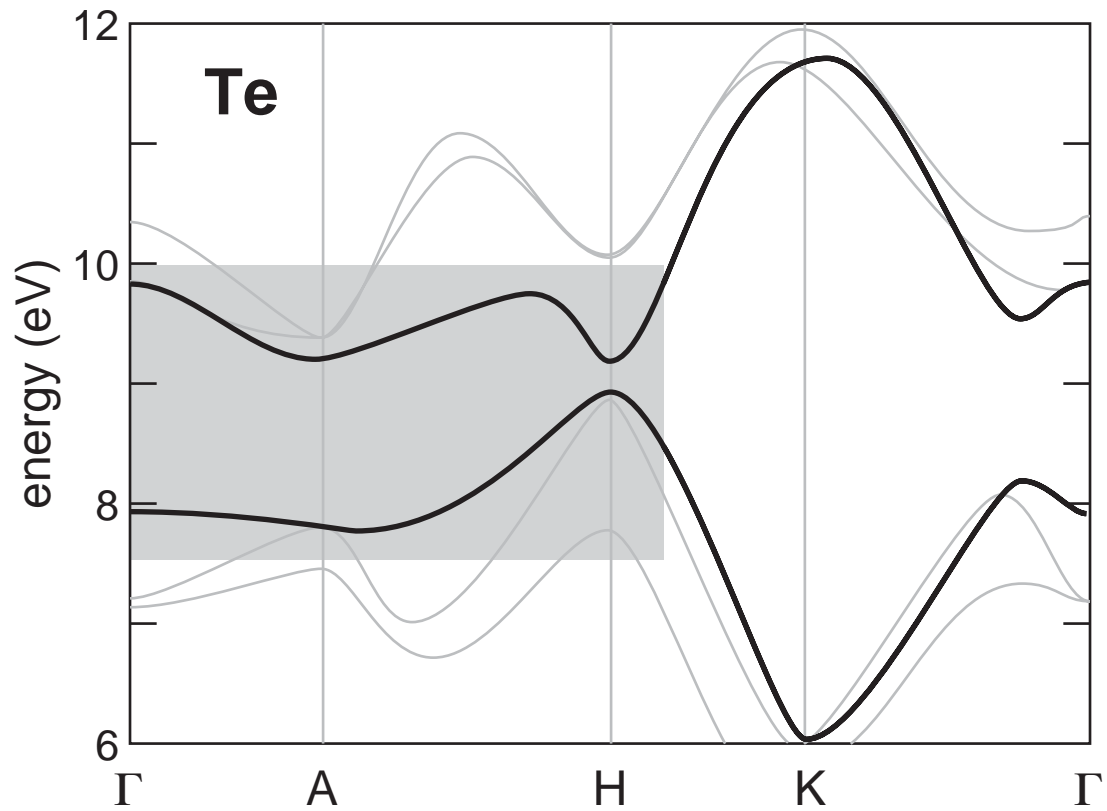


## Discussion

... but dielectric function non-metallic!

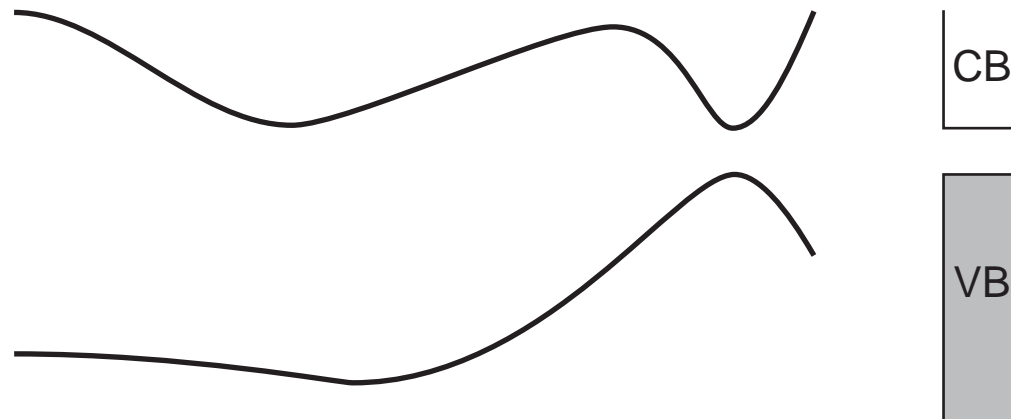


# Discussion



## *Discussion*

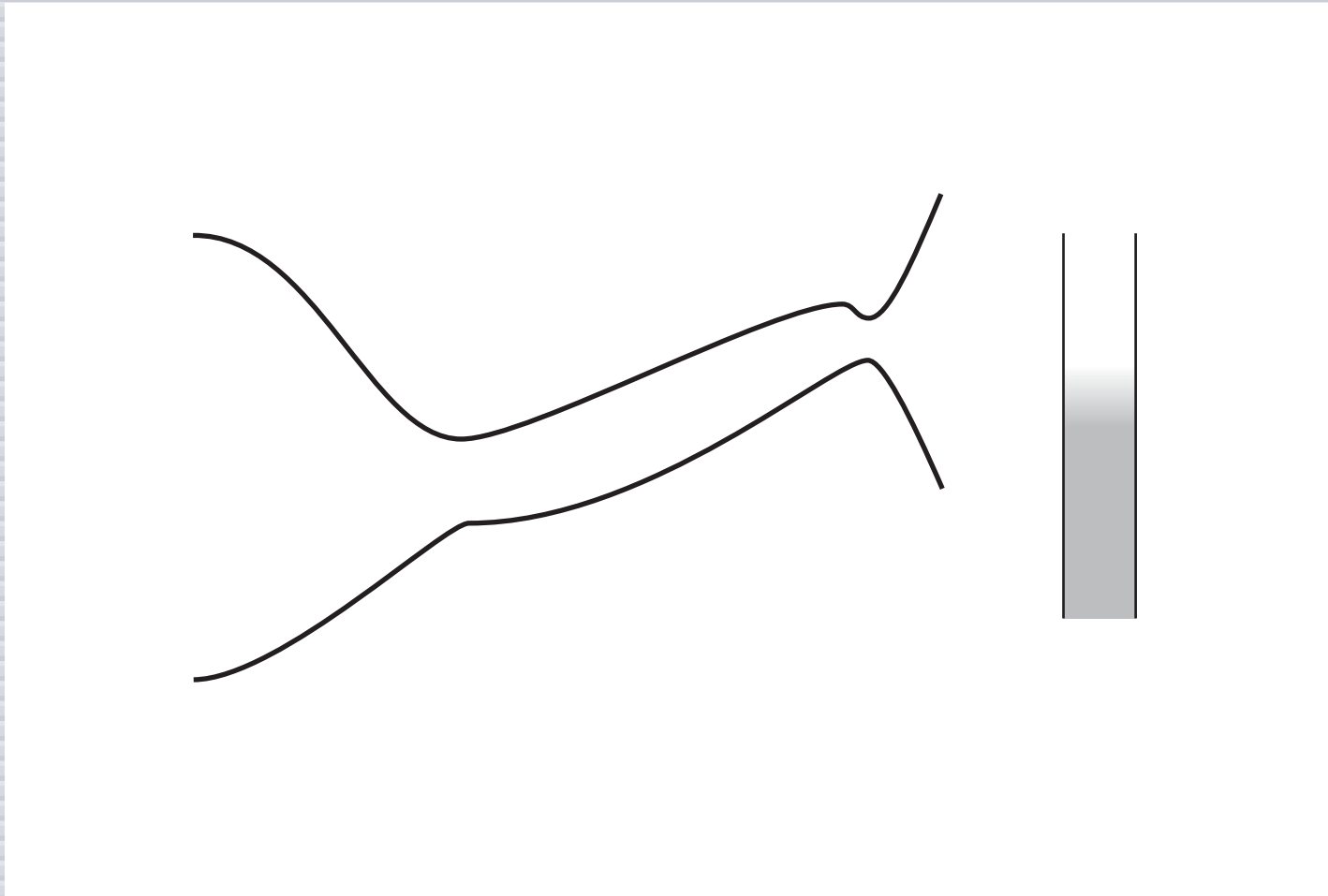
**semiconducting because of 0.3 eV gap**





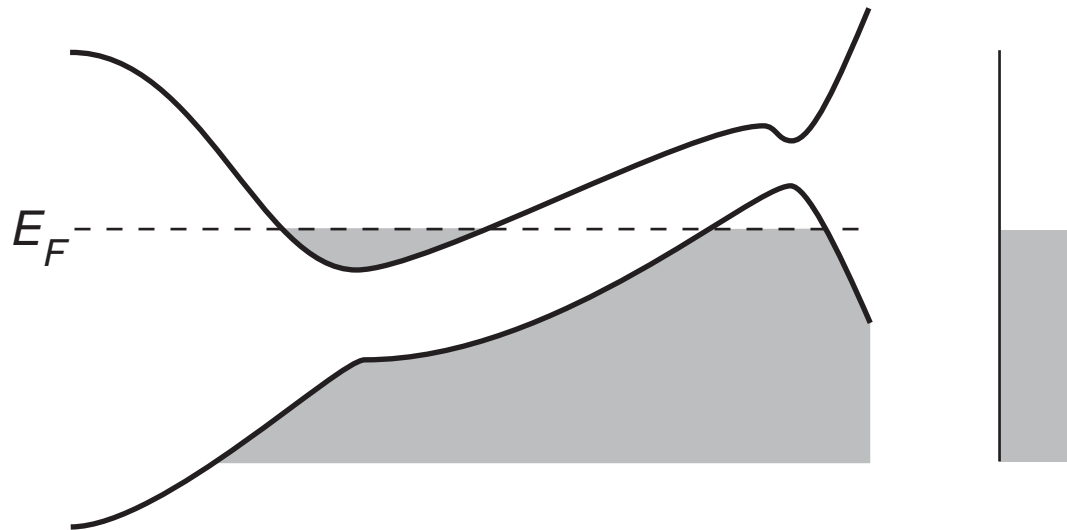
# *Discussion*

**after bands cross...**



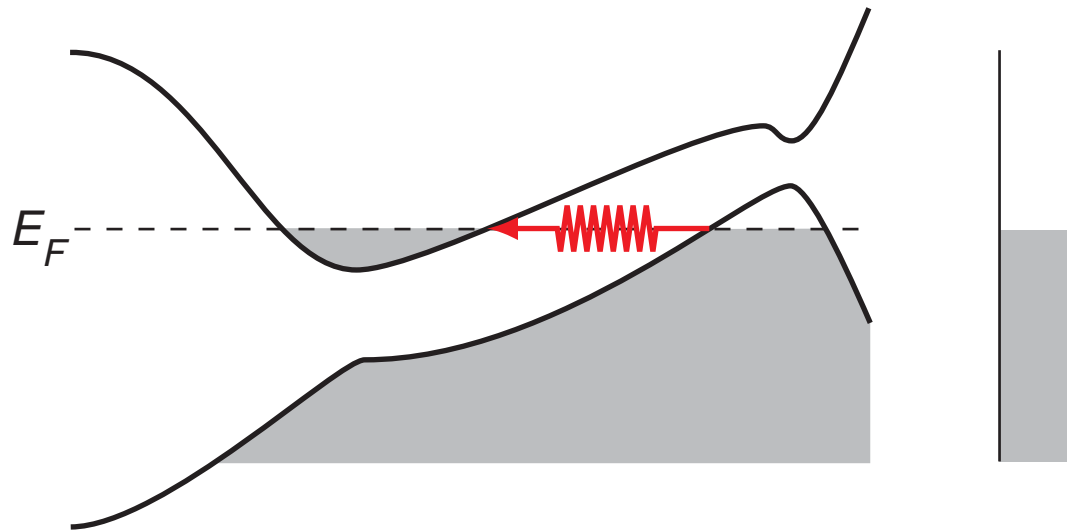
## *Discussion*

**... tellurium can become metallic...**



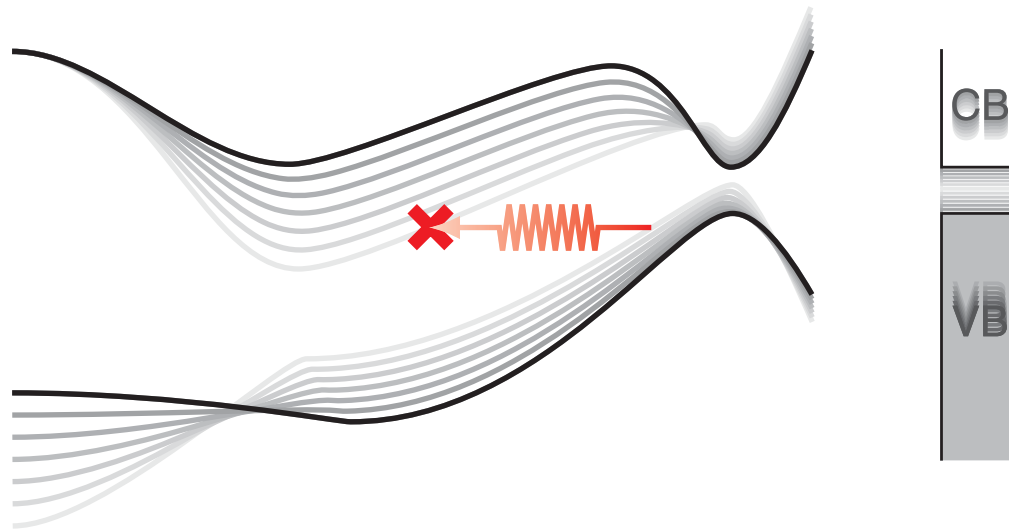
## Discussion

... provided phonons scatter electrons



# Discussion

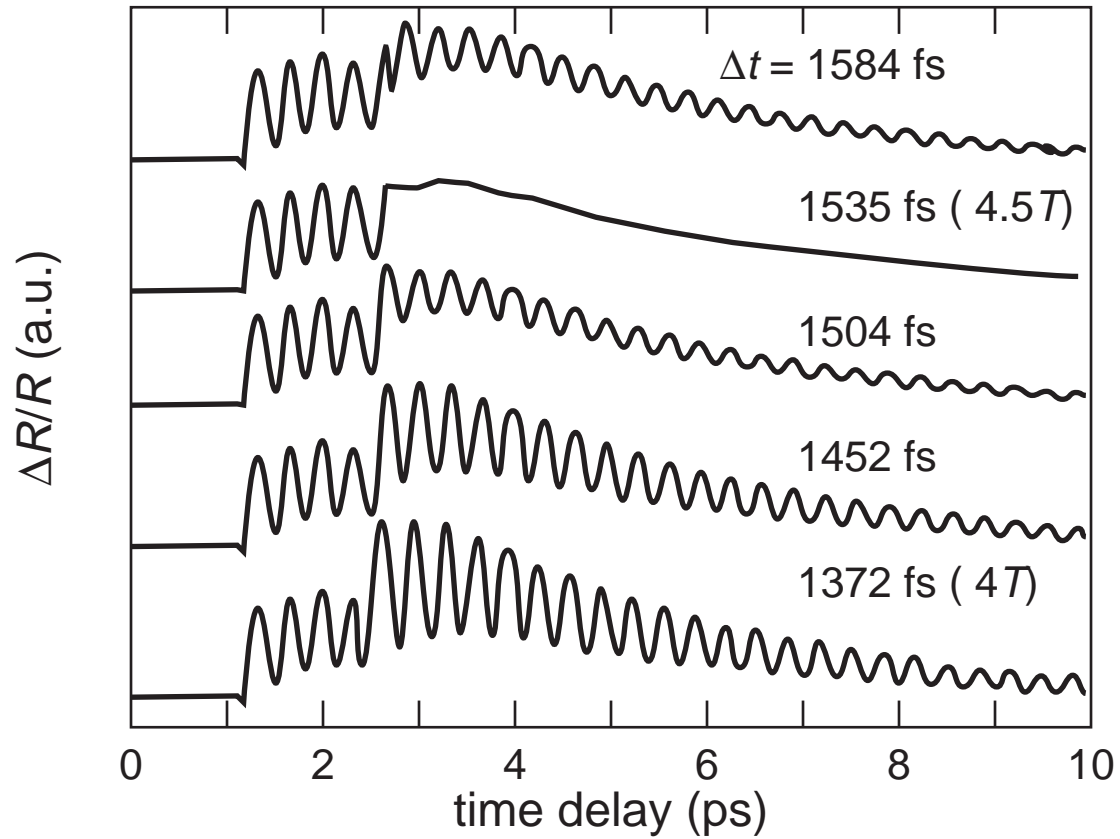
if  $\tau_{scatter} > T_{phonon}$ , 'frustrated' metal



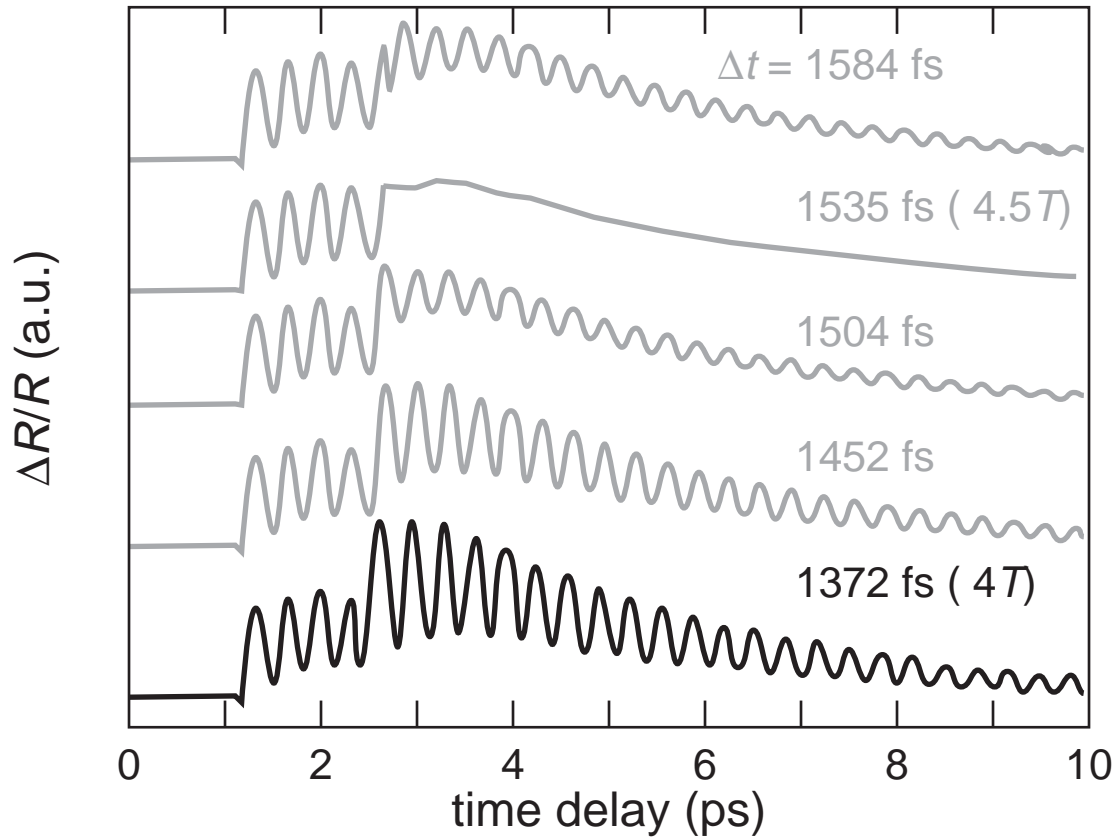
## *What's next?*

- ▶ **larger amplitude phonons**
- ▶ **different materials**
- ▶ **density functional theory modeling**
- ▶ **multiple pulse excitation for coherent control**

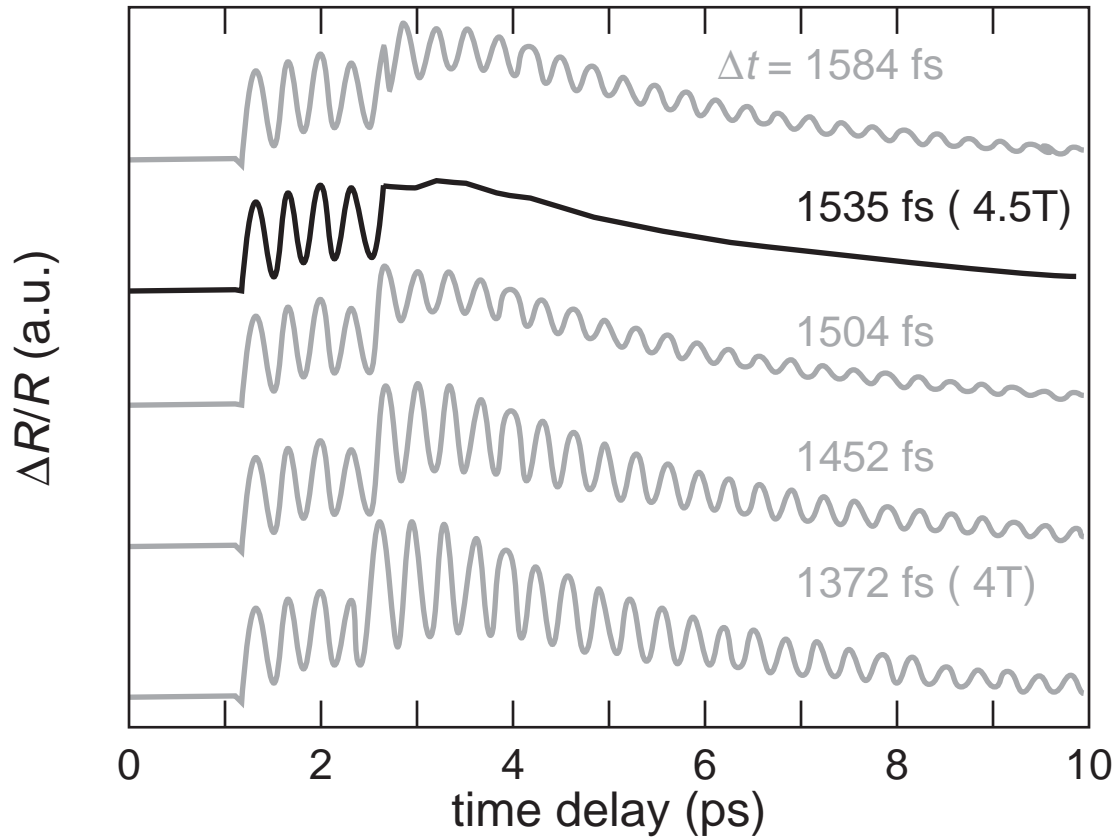
# What's next?



# What's next?



# What's next?





# Summary

- ▶ **femtosecond ellipsometry:**  
**observe transitions *as they occur***

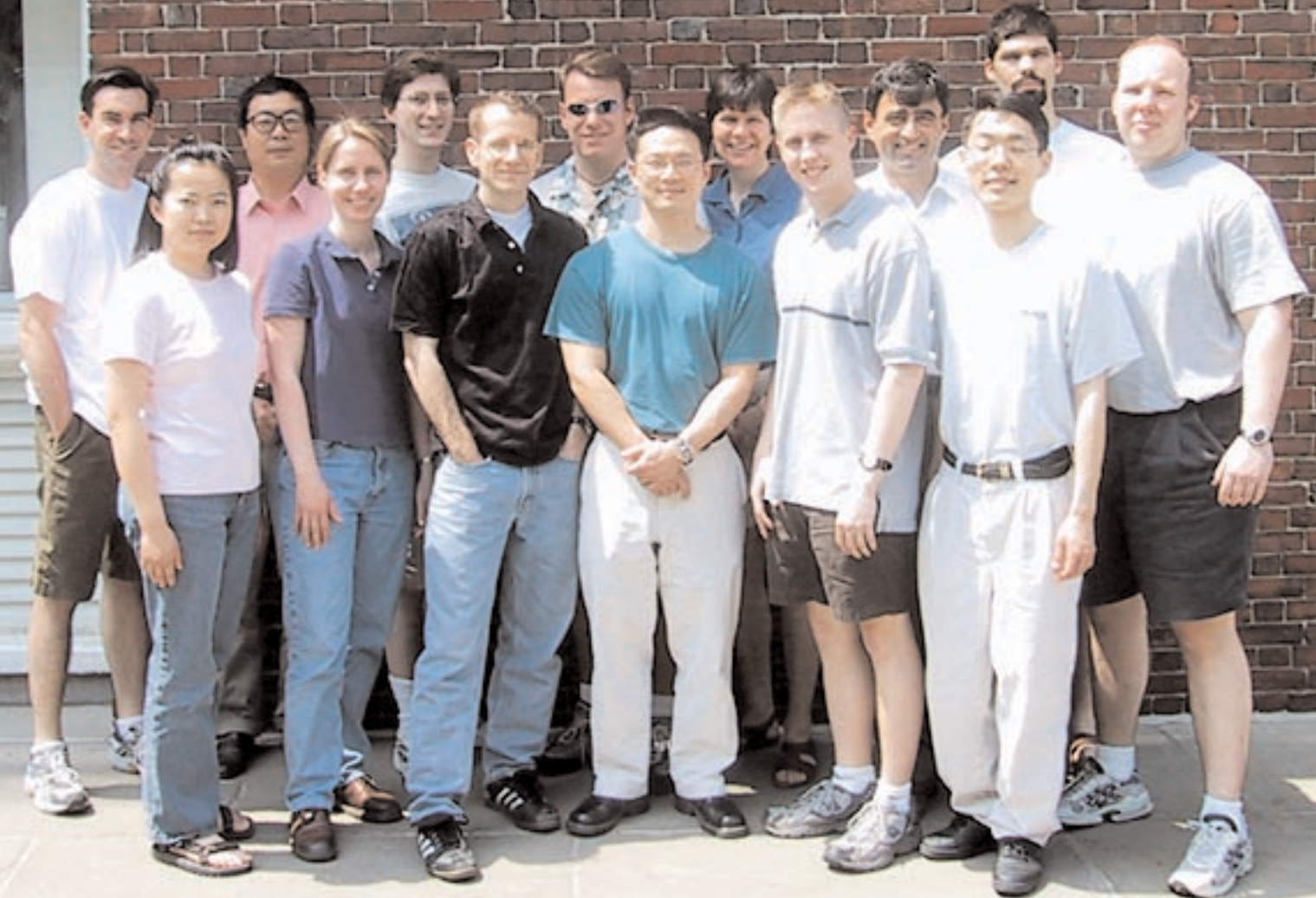
# Summary

- ▶ **femtosecond ellipsometry:**  
**observe transitions *as they occur***
- ▶ **dielectric function shows dispersive  
excitation of coherent phonons**

# Summary

- ▶ **femtosecond ellipsometry:  
observe transitions *as they occur***
- ▶ **dielectric function shows dispersive  
excitation of coherent phonons**
- ▶ **no electronic transition in spite of  
structural change**

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APPLIED SCIENCE



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**Nick Choly (Harvard University)**

**Prof. Tim Kaxiras (Harvard University)**

**For a copy of this talk and  
additional information, see:**

**<http://mazur-www.harvard.edu>**